Smart Power Systems, Renewable Energies and Markets: the Optimization Challenge

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 $\operatorname{CerMICS}$, France

January 25, 2015

During the night of 16 June 2013, electricity prices were negative



Outline of the talk

- In 2000, the *Optimization and Systems* team was created at École des Ponts ParisTech and, since then, we have *trained PhD students* in stochastic optimization, mostly with *Électricité de France Research and Development*
- Since 2011, we witness a growing demand from energy firms for stochastic optimization, fueled by a *deep and fast transformation of power systems*
- Renewable energies penetration, telecommunication technologies and markets remold power systems and challenge optimization
- $\bullet \ \, {\sf More\ renewable\ energies} \to {\sf more\ unpredicability} + {\sf more\ variability} \to$
 - $\bullet\,$ more storage \rightarrow more dynamic optimization, optimal control
 - more stochastic optimization

hence, stochastic optimal control

- We shed light on the two main new issues in stochastic control in comparison with deterministic control: risk attitudes and online information
- We cast a glow on two snapshots highlighting *ongoing research* in the field of stochastic control applied to energy

- Long term industry-academy cooperation
- 2 The remolding of power systems seen from an optimizer perspective
- Moving from deterministic to stochastic dynamic optimization
- 4 Two snapshots on ongoing research
- 5 A need for training and research

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Long term industry-academy cooperation

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- Long term industry-academy cooperation
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 - Industry partners of the Optimization and Systems Group
 - The remolding of power systems seen from an optimizer perspective
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Two snapshots on ongoing research

- Decomposition-coordination optimization methods under uncertainty
- Risk constraints in optimization

5 A need for training and research

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École des Ponts ParisTech is one of the world's oldest engineering institutes

- The École nationale des ponts et chaussées was founded in 1747 and is one of the world's oldest engineering institutes
- École des Ponts ParisTech is traditionally considered as belonging to the 5 leading engineering schools in France
- Young graduates find positions in professional sectors like transport and urban planning, banking, finance, consulting, civil works, industry, environnement, energy...
- Faculty and staff
 - 217 employees (including 50 subsidaries).
 - 165 module leaders, including 68 professors.
 - 1509 students.
- École des Ponts ParisTech is part of University Paris-Est

École des Ponts ParisTech hosts a substantial research activity

- Figures on research
 - Research personnel: 220
 - About 40 École des Ponts PhDs students graduate each year
- I0 research centers
 - * CEREA (atmospheric environment), joint École des Ponts-EDF R&D
 - * CEREVE (water, urban and environment studies)
 - * CERMICS (mathematics and scientific computing)
 - * CERTIS (information technologies and systems)
 - * CIRED (international environment and development)
 - * LATTS (techniques, regional planning and society)
 - * LVMT (city, mobility, transport)
 - * UR Navier (mechanics, materials and structures of civil engineering, geotechnic)
 - * Saint-Venant laboratory (fluid mechanics), joint École des Ponts-EDF R&D
 - * Paris School of Economic PSE

The CERMICS is the Centre d'enseignement et de recherche en mathématiques et calcul scientifique

- The scientific activity of CERMICS covers several domains in
 - scientific computing
 - modelling
 - optimization
- 15 senior researchers
 - 15 PhD
 - 12 habilitation à diriger des recherches
- Three missions
 - Teaching and PhD training
 - Scientific publications
 - Contracts
- 550 000 euros of contracts per year with
 - research and development centers of large industrial firms: CEA, CNES, EADS, EDF, Rio Tinto...
 - public research contracts

The Optimization and Systems Group comprises 3 senior researchers, as well as PhD students and external associated researchers

- Three senior researchers
 - J.-P. CHANCELIER
 - M. DE LARA
 - F. MEUNIER
- Between four and eight PhD students
- Four associated researchers
 - P. CARPENTIER (ENSTA ParisTech)
 - L. ANDRIEU (EDF R&D)
 - K. BARTY (EDF R&D)
 - A. DALLAGI (EDF R&D)

Optimization and Systems Group research specialities

- Methods
 - Stochastic optimal control (discrete-time)
 - Large-scale systems
 - Discretization and numerical methods
 - Probability constraints
 - Discrete mathematics; combinatorial optimization
 - System control theory, viability and stochastic viability
 - Numerical methods for fixed points computation
 - Uncertainty and learning in economics
- Applications
 - Optimized management of power systems under uncertainty (production scheduling, power grid operations, risk management)
 - Transport modelling and management
 - Natural resources management (fisheries, mining, epidemiology)
- Softwares
 - Scicoslab, NSP
 - Oadlibsim

Publications since 2000

- 24 publications in peer-reviewed international journals
- 3 publications in collective works
- 4 books
 - Modeling and Simulation in Scilab/Scicos with ScicosLab 4.4
 - (2e édition, Springer-Verlag)
 - Introduction à SCILAB (2e édition, Springer-Verlag)
 - Sustainable Management of Natural Resources. Mathematical Models and Methods (Springer-Verlag)
 - Control Theory for Engineers (Springer-Verlag)
- 1 book to be published by Springer-Verlag
 - Stochastic Optimization. At the Crossroads between Stochastic Control and Stochastic Programming

Teaching

Masters

- Master Parisien de Recherche Opérationnelle
- Optimisation & Théorie des Jeux. Modélisation en Economie
- Mathématiques, Informatique et Applications
- Économie du Développement Durable, de l'Environnement et de l'Énergie
- Renewable Energy Science and Technology Master ParisTech

• École des Ponts ParisTech

- Introduction à la recherche opérationnelle (F. MEUNIER)
- Optimisation et contrôle (J.-P. CHANCELIER)
- Modéliser l'aléa (J.-P. CHANCELIER)
- Modélisation pour la gestion durable des ressources naturelles (M. DE LARA)

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Industrial contracts mostly deal with energy issues, public ones touch on biodiversity management

Industrial contracts

- Conseil français de l'énergie (CFE)
- SETEC Energy Solutions
- Électricité de France (EDF R&D)
- Thales
- Institut français de l'énergie (IFE)
- Gaz de France (GDF)
- PSA
- Public contracts
 - STIC-AmSud (CNRS-INRIA-Affaires étrangères)
 - Centre d'étude des tunnels
 - CNRS ACI Écologie quantitative
 - RTP CNRS

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Two snapshots on ongoing research

- Decomposition-coordination optimization methods under uncertainty
- Risk constraints in optimization

5 A need for training and research

We cooperate with industry partners, looking for longlasting research relations through training and capacity building

- As academics, we cooperate with industry partners, looking for longlasting close relations
- We are not consultants working for clients, but focus en capacity building
- Our job consists mainly in
 - training Master and PhD students, working within the company and interacting with us, on subjects designed jointly
 - developing methods, algorithms
 - contributing to computer codes developed within the company
 - training professional engineers in the company

Électricité de France R & D / Département OSIRIS

• Électricité de France is the French electricity main producer

- 159 000 collaborateurs dans le monde
- 37 millions de clients dans le monde
- 65,2 milliards d'euros de chiffre d'affaire
- 630,4 TWh produits dans le monde
- Électricité de France Research & Development
 - 486 millions d'euros de budget
 - 2 000 personnes
- Département OSIRIS

Optimisation, simulation, risques et statistiques pour les marchés de l'énergie Optimization, simulation, risks and statistics for the energy markets

- 145 salariés (dont 10 doctorants)
- 25 millions d'euros de budget

What is "optimization"?

Optimizing is obtaining the best compromise between needs and resources Marcel Boiteux (président d'honneur d'Électricité de France)

- Resources: portfolio of assets
 - production units
 - costly/not costly: thermal/hydropower
 - stock/flow, predictable/unpredictable: thermal/wind
 - tariffs options, contracts
- Needs: energy, safety, environment
 - energy uses
 - safety, quality, resilience (breakdowns, blackout)
 - environment protection (pollution) and alternative uses (dam water)
- Best compromise: minimize socio-economic costs (including externalities)

The Optimization and Systems Group has trained 10 PhD from 2004 to 2014, most of them related with EDF and energy management

- * Laetitia ANDRIEU, former PhD student at EDF, now researcher EDF
- * Kengy BARTY, former PhD student at EDF, now researcher EDF
- * Daniel CHEMLA, former PhD student
- * Anes DALLAGI, former PhD student at EDF, now researcher EDF
- * Laurent GILOTTE, former PhD student with IFE, researcher EDF
- * Pierre GIRARDEAU, former PhD student at EDF, now with ARTELYS
- * Eugénie LIORIS, former PhD student
- * Babacar SECK, former PhD student at EDF
- * Cyrille STRUGAREK, former PhD student at EDF, now with Munich-Ré
- * Jean-Christophe ALAIS, former PhD student at EDF, now with ARTELYS
- * Vincent LECLERE, former PhD student (partly at EDF), now with CERMICS

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PhD subjects reflect academic issues raised by industrial problems

- Contributions to the Discretization of Measurability Constraints for Stochastic Optimization Problems,
- Optimization under Probability Constraint,
- Uncertainty, Inertia and Optimal Decision. Optimal Control Models Applied to Greenhouse Gas Abatment Policies Selection,
- Variational Approaches and other Contributions in Stochastic Optimization,
- Particular Methods in Stochastic Optimal Control,
- From Risk Constraints in Stochastic Optimization Problems to Utility Functions,
- Resolution of Large Size Problems in Dynamic Stochastic Optimization and Synthesis of Control Laws,
- Evaluation and Optimization of Collective Taxis Systems,
- Risk and Optimization for Energies Management,
- Risk, Optimization, Large Systems,

Recently, contacts have expanded with small companies

- ARTELYS is a company specializing in optimization, decision-making and modeling. Relying on their high level of expertise in quantitative methods, the consultants deliver efficient solutions to complex business problems. They provide services to diversified industries: Energy & Environment, Logistics & Transportation, Telecommunications, Finance and Defense.
- Créée en 2011, SETEC Energy Solutions est la filiale du groupe SETEC spécialisée dans les domaines de la production et de la maîtrise de l'énergie en France et à l'étranger. SETEC Energy Solutions apporte à ses clients la maîtrise des principaux process énergétiques pour la mise en œuvre de solutions innovantes depuis les phases initiales de définition d'un projet jusqu'à son exploitation.
- SUN'R Smart Energy is a Paris based company with a focus on building smarter solutions for distributed energy resources in the context of emerging deregulated energy markets and a solid political will towards the development of both renewables and energy storage. The company is part of a larger group founded in 2007 and is a growing, well-funded early stage business.

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French Energy Council, member of the World Energy Council, contracted the Optimization and Systems group to report on Optimization methods for smart grids

- Formed in 1923, the World Energy Council (WEC) is the UN-accredited global energy body, representing the entire energy spectrum, with more than 3000 member organisations located in over 90 countries and drawn from governments, private and state corporations, academia, NGOs and energy-related stakeholders
- WEC informs global, regional and national energy strategies by hosting high-level events, publishing authoritative studies, and working through its extensive member network to facilitate the world's energy policy dialogue
- In 2012, the French Energy Council contracted the Optimization and Systems group to produce a report on Optimization methods for smart grids

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Summary

The following slides on the remolding of power systems express a viewpoint

- from an optimizer perspective
- working in an optimization research group
- in an applied mathematics research center
- in a French engineering institute
- having contributed to train students now working in energy
- having contacts and contracts with energy/environment firms

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 - Handling online information
 - Discussing framing and resolution methods
 - Two snapshots on ongoing research
 - Decomposition-coordination optimization methods under uncertainty
 - Risk constraints in optimization
 - A need for training and research

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5 A need for training and research

Three key drivers are remolding power systems





- Environment
- Markets
- Technology



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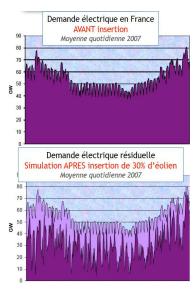
Distributed Generation
 Renewable Generation
 Storage

Michel DE LARA (CERMICS, France)

Workshop STORY, Berkeley, 26 January 2015

January 25, 2015 26 / 125

Key driver: environmental concern



The European Union climate and energy package materializes an environmental concern with three 20-20-20 objectives for 2020

- a 20% improvement in the EU's energy efficiency
- a 20% reduction in EU greenhouse gas emissions from 1990 levels
- raising the share of EU energy consumption produced from renewable resources to 20%

↓ Successfully integrating renewable energy sources has become critical, and made especially difficult because they are unpredictable and highly variable, hence triggering the use of local storage

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Key driver: economic deregulation

• A power system (generation/transmission/distribution)

- less and less vertical (deregulation of energy markets)
- hence with many players with their own goals
- with some new players
 - industry (electric vehicle)
 - regional public authorities (autonomy, efficiency)
- with a network in horizontal expansion

(the Pan European electricity transmission system counts 10,000 buses, 15,000 power lines, 2,500 transformers, 3,000 generators, 5,000 loads)

• with more and more exchanges (trade of commodities)

A change of paradigm for management from centralized to more and more decentralized

Key driver: telecommunication technology



A power system with more and more technology due to evolutions in the fields of metering, computing and telecoms

- smart meters
- sensors
- controllers
- grid communication devices...

Linky

A huge amount of data which, one day, will be a new potential for optimized management

The remolding of power systems seen from an optimizer perspective

The "smart grid"? An infrastructure project with promises to be fulfilled by a "smart power system"





- Hardware / infrastructures / smart technologies
 - Renewable energies technologies
 - Smart metering
 - Storage
- Promises
 - Quality, tariffs
 - More safety
 - More renewables (environmentally friendly)
- Software / smart management (energy supply being less flexible, make the demand more flexible)

smart management, smart operation, smart meter management, smart distributed generation, load management, advanced distribution management systems, active demand management, diffuse effacement, distribution management systems, storage management, smart home, demand side management...

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Michel DE LARA (CERMICS, France)

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We witnessed a call from EDF to optimizers

- Every three years, Électricité de France (EDF) organizes an international Conference on Optimization and Practices in Industry (COPI)
- At COPI'11, Jean-François Faugeras from EDF R&D opened the conference with a plenary talk entitled "Smart grids: a wind of change in power systems and new opportunities for optimization"
- He claimed that "power system players are facing high level problems to solve requiring new optimization methods and tools", with "not only a 'smart(er)' grid but a 'smart(er)' power system" and called on the optimizers to develop new methods
- In 2012, EDF R&D has sponsored a new program Gaspard Monge pour l'Optimisation et la recherche opérationnelle (PGMO) to support academic research in the field of optimization

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- Resources: portfolio of assets
 - production units
 - costly/not costly: thermal/hydropower
 - stock/flow, predictable/unpredictable: thermal/wind
 - tariffs options, contracts
- Needs: energy, safety, environment
 - energy uses
 - safety, quality, resilience (breakdowns, blackout)
 - environment protection (pollution) and alternative uses (dam water)
- Best compromise: minimize socio-economic costs (including externalities)

Electrical engineers metiers and skills are evolving

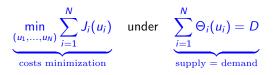
- Unit commitment, optimal dispatch of generating units: finding the least-cost dispatch of available generation resources to meet the electrical load
 - $\bullet\,$ which unit? 0/1 variables
 - which power level? continuous variables

subject to more unpredictable energy flows (solar, wind) and demand (electrical devices, cars)

- Markets: day-ahead, intra-day (balancing market): dispatcher takes bids from the generators, demand forecasts from the distribution companies and clears the market subject to more unpredictability, more players
- Long term planning subject to more unpredictability (technologies, climate), more players
- ... Without even speaking of voltage, frequency and phase control

Let us have a look at economic dispatch (static) as a cost-minimization problem under supply-demand balance

Consider energy production units i = 1, ..., N, like coal, gas, nuclear...

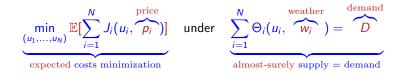


where

- u_i is the decision (production level) made for each unit *i*
- $J_i(u_i)$ is the cost of making decision u_i for unit *i*
- $\Theta_i(u_i)$ is the production induced by making decision u_i for unit *i*
- D is the demand

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Inviting in uncertainty gives economic dispatch new suits of clothes



- Mathematical description of sources of uncertainties (prices p_i, weather w_i, demand D, failures...): statistics? bounds?
- Mathematical formulation of the criterion under uncertainty: in expectation (E)? worst case (max)?
- Mathematical formulation of the constraints under uncertainty: in expectation? in probability? almost surely? robust? by penalization?

With uncertainty come stages, hence a dynamics

- In electricity, the supply matches demand equation
 "is like gravity, you cannot negociate" (who claimed that?)
- One way or another, we are driven to add a new instantaneous source u_{N+1}



- The control $u_{N+1} = D \sum_{i=1}^{N} \Theta_i(u_i, w_i)$ depends on the uncertain variables D and w_1, \ldots, w_N
- Whereas u_1, \ldots, u_N are decisions made before knowing their realizations
- To cut to the point, we now have two stages

Piecing things together, we started from static economic dispatch and, on the path of making allowance for uncertainty, we have been quite naturally led to dynamic economic dispatch under risk

Optimization skills will follow the power system evolution

We focus on generation and trading, not on transmission and distribution

- Less base production and more wind and photovoltaic fatal generation makes supply more unpredictible
 - \rightarrow stochastic optimization
- Hence more storage (batteries, pumping stations)
 → dynamical optimization, reserves dimensioning
- The shape of the load is changing due to electric vehicle penetration
 → demand-side management, "peak shaving", adaptive tariffs
- New subsystems emerge with local information and means of action: smart meters, new producers, micro-grid, virtual power plant → agregation, coordination, decentralized optimization
- Markets (day-ahead, intra-day)
 - \rightarrow optimization under uncertainty
- Environmental constraints on production (CO2) and resources usages (water)
 → risk constraints

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Summary

- Three major key factors environmental concern, deregulation, telecommunication, metering and computing technology drive the power systems remolding
- This remolding induces a change of paradigm for management: from vertical centralized predictible "stock" energies to more horizontal decentralized unpredictible variable "flow" energies
- Specific optimization skills will be required. because a deterministic optimal solution is balancing on a knife edge, hence might perform poorly under off-nominal conditions, like a too much adjusted suit cracking at the first move

Roger Wets' illuminating example: deterministic vs. robust

of a furniture manufacturer deciding how many dressers of each of 4 types to produce, with carpentry and finishing man-hours as constraints; when the ten parameters become random, the stochastic optimal solution considers all $pprox 10^6$ possibilities and provides a robust solution (257; 0; 665; 34), whereas the deterministic solution (1, 333; 0; 0; 67) does not point in the right direction

Outline of the presentation

- Long term industry-academy cooperation
- 2 The remolding of power systems seen from an optimizer perspective

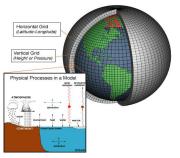
Moving from deterministic to stochastic dynamic optimization

- 4) Two snapshots on ongoing research
- 5 A need for training and research

Michel DE LARA (CERMICS, France)

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We distinguish two polar classes of models: knowledge models *versus* decision models

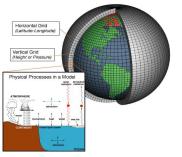


Knowledge models: $1/1\ 000\ 000 \rightarrow 1/1\ 000 \rightarrow 1/1\ maps$

Office of Oceanic and Atmospheric Research (OAR) climate model

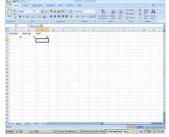
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We distinguish two polar classes of models: knowledge models *versus* decision models



Knowledge models: $1/1\ 000\ 000 \rightarrow 1/1\ 000 \rightarrow 1/1\ maps$

Office of Oceanic and Atmospheric Research (OAR) climate model



Action/decision models: economic models are fables designed to provide insight

William Nordhaus economic-climate model

Outline of the presentation

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 - Expliciting risk attitudes
 - Handling online information
 - Discussing framing and resolution methods

Two snapshots on ongoing research

- Decomposition-coordination optimization methods under uncertainty
- Risk constraints in optimization

5 A need for training and research

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Let us work out a toy example of economic dispatch as a cost-minimization problem under supply-demand balance

Production: consider two energy production units

- a "cheap" limited one with which we can produce quantity q_0 , with $0 \le q_0 \le q_0^{\sharp}$, at cost $c_0 q_0$
- an "expensive" unlimited one with which we can produce quantity q_1 , with $0 \le q_1$, at cost c_1q_1 , with $c_1 > c_0$
- Consumption: the demand is $D \ge 0$
- Balance: ensuring at least the demand

 $D \leq q_0 + q_1$

• Optimization: total costs minimization



(a)

When the demand D is deterministic, the optimization problem is well posed

• The deterministic demand D is a single number, and we consider

 $\min_{q_0,q_1} c_0 q_0 + c_1 q_1$

$$\begin{array}{lll} & 0 & \leq q_0 \leq q_0^{\sharp} \\ \text{under the constraints} & 0 & \leq q_1 \\ & D & \leq q_0 + q_1 \end{array}$$

- The solution is $q_0^\star = \min\{q_0^\sharp, D\}$, $q_1^\star = [D q_0^\sharp]_+$, that is,
 - if the demand D is below the capacity q_0^{\sharp} of the "cheap" energy source

$$D\leq q_0^{\sharp}\Rightarrow q_0^{\star}=D\,,\quad q_1^{\star}=0$$

• if the demand D is above the capacity q_0^{\sharp} of the "cheap" energy source,

$$D>q_0^{\sharp}\Rightarrow q_0^{\star}=q_0^{\sharp}\,,\quad q_1^{\star}=D-q_0^{\sharp}$$

• Now, what happens when the demand *D* is no longer deterministic?

If we know the demand beforehand, the optimization problem is deterministic

- We suppose that the demand is a random variable $D:\Omega
 ightarrow\mathbb{R}_+$
- If we solve the problem for each possible value $D(\omega)$ of the random variable D, when $\omega \in \Omega$, we obtain

$$q_0(\omega) = \min\{q_0^{\sharp}, D(\omega)\}, \quad q_1(\omega) = [D(\omega) - q_0^{\sharp}]_+$$

and we face an informational issue

- Indeed, we treat the demand D as if it were observed before making the decisions q₀ and q₁
- When the demand D is not observed, how can we do?

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What happens if we replace the uncertain value D of the demand by its mean D in the deterministic solution?

- If we suppose that the demand D is a random variable $D: \Omega \to \mathbb{R}_+$, with mathematical expectation $\mathbb{E}(D) = \overline{D}$
- and that we propose the "deterministic solution"

$$q_0^{(\overline{D})}=\min\{q_0^\sharp,\overline{D}\}\;,\;\;q_1^{(\overline{D})}=[\overline{D}-q_0^\sharp]_+$$

we cannot assure the inequality



because
$$\sup_{\omega\in\Omega} D(\omega) > \overline{D} = q_0^{(\overline{D})} + q_1^{(\overline{D})}$$

• Are there better solutions among the deterministic ones?

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When the demand D is bounded above, the robust optimization problem has a solution

• In the robust optimization problem, we minimize

 $\min_{q_0,q_1} c_0 q_0 + c_1 q_1$

$$\begin{array}{rll} \text{under the constraints} & \begin{array}{c} 0 & \leq q_0 \leq q_0^{\sharp} \\ 0 & \leq q_1 \\ D(\omega) & \leq q_0 + q_1 \ , \ \forall \omega \in \Omega \end{array}$$

• When
$$D^{\sharp} = \sup_{\omega \in \Omega} D(\omega) < +\infty$$
, the solution is $q_0^{\star} = \min\{q_0^{\sharp}, D^{\sharp}\}, \quad q_1^{\star} = [D^{\sharp} - q_0^{\sharp}]_+$

- Now, the total cost $c_0q_0^* + c_1q_1^*$ is an increasing function of the upper bound D^{\sharp} of the demand
- Is it not too costly to optimize under the worst-case situation?

Where do we stand?

- When the demand D is deterministic, the optimization problem is well posed
- If we know the demand beforehand, the optimization problem is deterministic
- If we replace the uncertain value D of the demand by its mean \overline{D} in the deterministic solution, we remain with a feasability issue
- When the demand *D* is bounded above, the robust optimization problem has a solution, but it is costly

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Where do we stand?

- When the demand D is deterministic, the optimization problem is well posed
- If we know the demand beforehand, the optimization problem is deterministic
- If we replace the uncertain value D of the demand by its mean \overline{D} in the deterministic solution, we remain with a feasability issue
- When the demand *D* is bounded above, the robust optimization problem has a solution, but it is costly

To overcome the above difficulties, we propose to introduce stages



- the decision q_0 is made before observing the demand $D(\omega)$
- the decision $q_1(\omega)$ is made after observing the demand $D(\omega)$

To overcome the above difficulties, we turn to stochastic optimization

• We suppose that the demand D is a random variable, and minimize

 $\min_{q_0,q_1}\mathbb{E}[c_0q_0+c_1q_1]$

under the constraints
$$egin{array}{ccc} 0 & \leq q_0 \leq q_0^{\sharp} \ 0 & \leq q_1 \ D & \leq q_0 + q_1 \ q_1 & ext{depends upon } D \end{array}$$

and we emphasize two issues, new with respect to the deterministic case

- expliciting online information issue: the decision q₁ depends upon the random variable D
- expliciting risk attitudes:

we aggregate the total costs with respect to all possible values by taking the expectation $\mathbb{E}[c_0q_0 + c_1q_1]$

Turning to stochastic optimization forces one to specify online information

• We suppose that the demand D is a random variable, and minimize

 $\min_{q_0,q_1}\mathbb{E}[c_0q_0+c_1q_1]$

$$egin{array}{lll} 0&\leq q_0\leq q_0^{\sharp}\ 0&\leq q_1\ D&\leq q_0+q_1\ q_1\ depends \ upon \end{array}$$

specifying that the decision q₁ depends upon the random variable D, whereas q₀ does not, forces to consider two stages and a so-called non-anticipativity constraint (more on that later)

- first stage: q_0 does not depend upon the random variable D
- second stage: q1 depends upon the random variable D

D

Turning to stochastic optimization forces one to specify risk attitudes

• We suppose that the demand D is a random variable, and minimize

 $\min_{q_0,q_1} \mathbb{E}[c_0 q_0 + c_1 q_1]$

under the constraints
$$egin{array}{ccc} 0 & \leq q_0 \leq q_0^{\sharp} \\ 0 & \leq q_1 \\ D & \leq q_0 + q_1 \\ q_1 & ext{depends upon } D \end{array}$$

• Now that q_1 depends upon the random variable D, it is also a random variable, and so is the total cost $c_0q_0 + c_1q_1$; therefore, we have to aggregate the total costs with respect to all possible values, and we chose to do it by taking the expectation $\mathbb{E}[c_0q_0 + c_1q_1]$

In the uncertain framework, two additional questions must be answered with respect to the deterministic case

Question (expliciting risk attitudes)

How are the uncertainties taken into account in the payoff criterion and in the constraints?

Question (expliciting available online information)

Upon which online information are decisions made?

Outline of the presentation

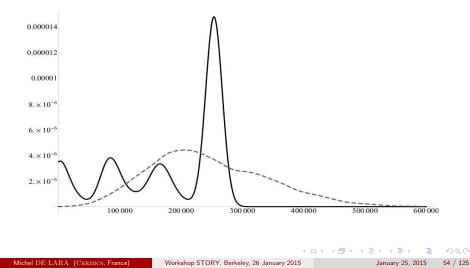
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5 A need for training and research

The output of a stochastic optimization problem is a random variable. How can we rank random variables?



How are the uncertainties taken into account in the payoff criterion and in the constraints?

In a probabilistic setting, where uncertainties are random variables, a classical answer is

• to take the mathematical expectation of the payoff (risk-neutral approach)

E(payoff)

 and to satisfy all (physical) constrainsts almost surely that is, practically, for all possible issues of the uncertainties (robust approach)

 $\mathbb{P}(\text{constrainsts}) = 1$

But there are many other ways to handle risk: robust, worst case, risk measures, in probability, almost surely, by penalization, etc.

Expliciting risk attitudes

A policy and a criterion yield a real-valued payoff

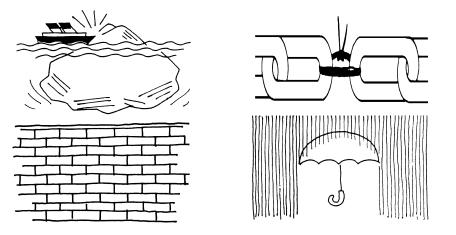
Given an admissible policy $\texttt{Pol} \in \mathcal{U}^{ad}$ and a scenario $w(\cdot) \in \Omega$, we obtain a payoff

 $Payoff(Pol, w(\cdot))$

Policies/Scenarios	$w^{\mathcal{A}}(\cdot)\in\Omega$	$w^B(\cdot)\in \Omega$	
$ extsf{Pol}_1 \in \mathcal{U}^{ extsf{ad}}$	$Payoff(Pol_1, w^A(\cdot))$	$Payoff(Pol_1, w^B(\cdot))$	
$ extsf{Pol}_2 \in \mathcal{U}^{ extsf{ad}}$	$Payoff(Pol_2, w^{A}(\cdot))$	$Payoff(Pol_2, w^B(\cdot))$	

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In the robust or pessimistic approach, Nature is supposed to be malevolent, and the DM aims at protection against all odds



Workshop STORY, Berkeley, 26 January 2015

In the robust or pessimistic approach, Nature is supposed to be malevolent

• In the robust approach, the DM considers the worst payoff



 Nature is supposed to be malevolent, and specifically selects the worst scenario: the DM plays after Nature has played, and maximizes the worst payoff

```
\max_{\text{Pol} \in \mathcal{U}^{ad}} \min_{w(\cdot) \in \Omega} \text{Payoff}(\text{Pol}, w(\cdot))
```

• Robust, pessimistic, worst-case, maximin, minimax (for costs)

Guaranteed energy production

In a dam, the minimal energy production in a given period, corresponding to the worst water inflow scenario

The robust approach can be softened with plausibility weighting

- Let $\Theta: \Omega \to \mathbb{R} \cup \{-\infty\}$ be a a plausibility function.
- The higher, the more plausible: totally implausible scenarios are those for which Θ(w(·)) = −∞
- Nature is malevolent, and specifically selects the worst scenario, but weighs it according to the plausibility function Θ
- The DM plays after Nature has played, and solves

$$\max_{\texttt{Pol} \in \textit{ll}^{\textit{ad}}} \left[\min_{w(\cdot) \in \Omega} \left(\texttt{Payoff}(\texttt{Pol}, w(\cdot)) - \underbrace{\Theta(w(\cdot))}_{\text{plausibility}} \right) \right]$$

In the optimistic approach, Nature is supposed to benevolent

Future. That period of time in which our affairs prosper, our friends are true and our happiness is assured.

Ambrose Bierce

• Instead of maximizing the worst payoff as in a robust approach, the optimistic focuses on the most favorable payoff

$$\underbrace{\max_{w(\cdot)\in\Omega} \mathtt{Payoff}(\mathtt{Pol},w(\cdot))}_{\text{best payoff}}$$

• Nature is supposed to benevolent, and specifically selects the best scenario: the DM plays after Nature has played, and solves

 $\max_{\text{Pol}\in\mathcal{U}^{ad}}\max_{w(\cdot)\in\Omega}\text{Payoff}(\text{Pol},w(\cdot))$

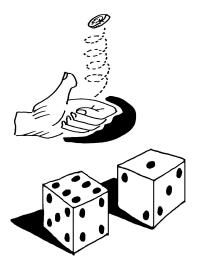
The Hurwicz criterion reflects an intermediate attitude between optimistic and pessimistic approaches

A proportion $\alpha \in [0,1]$ graduates the level of prudence

$$\max_{\text{Pol} \in \mathcal{U}^{sd}} \left\{ \alpha \underbrace{\min_{w(\cdot) \in \Omega} \text{Payoff}(\text{Pol}, w(\cdot))}_{w(\cdot) \in \Omega} + (1 - \alpha) \underbrace{\max_{w(\cdot) \in \Omega} \text{Payoff}(\text{Pol}, w(\cdot))}_{\text{optimistic}} \right\}$$

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In the stochastic or expected approach, Nature is supposed to play stochastically





In the stochastic or expected approach, Nature is supposed to play stochastically

• The expected payoff is

$$\overbrace{\mathbb{E}\Big[\mathsf{Payoff}(\mathsf{Pol},w(\cdot))\Big]}^{\text{mean payoff}} = \sum_{w(\cdot)\in\Omega} \mathbb{P}\{w(\cdot)\}\mathsf{Payoff}(\mathsf{Pol},w(\cdot))$$

 Nature is supposed to play stochastically, according to distribution ℙ: the DM plays after Nature has played, and solves

$$\max_{\texttt{Pol}\in \mathcal{U}^{ad}} \mathbb{E}\bigg[\texttt{Payoff}\big(\texttt{Pol},w(\cdot)\big)\bigg]$$

• The discounted expected utility is the special case

$$\mathbb{E}\left[\sum_{t=t_0}^{+\infty} \delta^{t-t_0} L(x(t), u(t), w(t))\right]$$

The expected utility approach distorts payoffs before taking the expectation

- We consider a utility function L to assess the utility of the payoffs (for instance a CARA exponential utility function)
- The expected utility is

$$\underbrace{\mathbb{E}\left[L\left(\mathsf{Payoff}(\mathsf{Pol}, w(\cdot))\right)\right]}_{\text{expected utility}} = \sum_{w(\cdot)\in\Omega} \mathbb{P}\{w(\cdot)\}L\left(\mathsf{Payoff}(\mathsf{Pol}, w(\cdot))\right)$$

• The expected utility maximizer solves

$$\max_{\texttt{Pol}\in \texttt{U}^{\texttt{ad}}} \mathbb{E}\left[L \Big(\texttt{Payoff} \big(\texttt{Pol}, w(\cdot) \big) \Big) \right]$$

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The ambiguity or multi-prior approach combines robust and expected criterion

- Different probabilities P, termed as beliefs or priors and belonging to a set P of admissible probabilities on Ω
- The multi-prior approach combines robust and expected criterion by taking the worst beliefs in terms of expected payoff

$$\max_{\text{Pol} \in \mathcal{U}^{ad}} \underbrace{\min_{\mathbb{P} \in \mathcal{P}} \mathbb{E}^{\mathbb{P}} \left[\text{Payoff}(\text{Pol}, w(\cdot)) \right]}_{\text{pessimistic over probabilities}}$$

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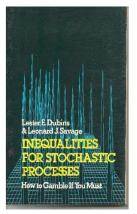
Convex risk measures cover a wide range of risk criteria

- Different probabilities ℙ, termed as beliefs or priors and belonging to a set 𝒫 of admissible probabilities on Ω
- $\bullet\,$ To each probability $\mathbb P$ is attached a plausibility $\Theta(\mathbb P)$

$$\max_{\text{Pol} \in \mathcal{U}^{ad}} \underbrace{\min_{\mathbb{P} \in \mathcal{P}} \mathbb{E}^{\mathbb{P}} \left[\text{Payoff}(\text{Pol}, w(\cdot)) \right]}_{\text{pessimistic over probabilities}} - \underbrace{\Theta(\mathbb{P})}_{\text{polsimistic over probabilities}} \right]$$

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Non convex risk measures can lead to non diversification



How to gamble if you must, L.E. Dubbins and L.J. Savage, 1965 Imagine yourself at a casino with \$1,000. For some reason, you desperately need \$10,000 by morning; anything less is worth nothing for your purpose.

The only thing possible is to gamble away your last cent, if need be, in an attempt to reach the target sum of \$10,000.

- The question is how to play, not whether. What ought you do? How should you play?
 - Diversify, by playing 1 \$ at a time?
 - Play boldly and concentrate, by playing 10,000 \$ only one time?

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• What is your decision criterion?

Savage's minimal regret criterion... "Had I known"



- If the DM knows the future in advance, she solves $\max_{\text{anticipative policies } \overline{Pol}} \operatorname{Payoff}(\overline{Pol}, w(\cdot))$, for each scenario $w(\cdot) \in \Omega$
- The regret attached to a non-anticipative policy Pol ∈ U^{ad} is the loss due to not being visionary
- The best a non-visionary DM can do with respect to regret is minimizing it

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 - The remolding of power systems seen from an optimizer perspective
 - The remolding of power systems
 - Optimization is challenged
 - Moving from deterministic to stochastic dynamic optimization
 - Working out a toy example
 - Expliciting risk attitudes
 - Handling online information
 - Discussing framing and resolution methods

Two snapshots on ongoing research

- Decomposition-coordination optimization methods under uncertainty
- Risk constraints in optimization

5 A need for training and research

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Upon which online information are decisions made?

We navigate between two stumbling blocks: rigidity and wizardry

- On the one hand, it is suboptimal to restrict oneself, as in the deterministic case, to open-loop controls depending only upon time, thereby ignoring the available information at the moment of making a decision
- On the other hand, it is impossible to suppose that we know in advance what will happen for all times:

clairvoyance is impossible as well as look-ahead solutions

The in-between is non-anticipativity constraint

There are two ways to express the non-anticipativity constraint

Denote the uncertainties at time t by w(t), and the control by u(t)

• Functional approach

The control u(t) may be looked after under the form

$$u(t) = \phi_t(\underbrace{w(t_0), \dots, w(t-1)}_{\text{past}})$$

where ϕ_t is a function, called policy, strategy or decision rule

• Algebraic approach

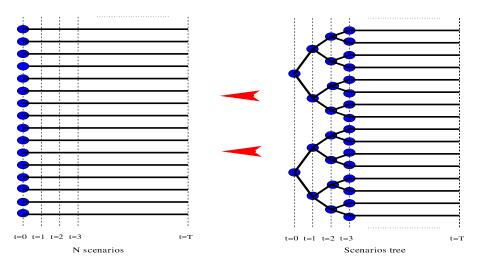
When uncertainties are considered as random variables (measurable mappings), the above formula for u(t) expresses the measurability of the control variable u(t) with respect to the past uncertainties, also written as

$$\underbrace{\sigma(u(t))}_{\sigma\text{-algebra}} \subset \sigma(\underbrace{w(t_0), \ldots, w(t-1)}_{\text{past}})$$

What is a solution at time t?

- In deterministic control, the solution u(t) at time t is a single vector
- In stochastic control, the solution u(t) at time t is a random variable expressed
 - either as $u(t) = \phi_t(w(t_0), \dots, w(t-1))$, where $\phi_t : \mathbb{W}^{t-t_0} \to \mathbb{R}$
 - or as $u(t) : \Omega \to \mathbb{R}$ with measurability constraint $\sigma(u(t)) \subset \sigma(w(t_0), \dots, w(t-1))$ or $u(t) = \mathbb{E}\left(u(t) \mid w(t_0), \dots, w(t-1)\right)$
- Now, as time t goes on, the domain of the function ϕ_t expands, and so do the conditions $\sigma(u(t)) \subset \sigma(w(t_0), \dots, w(t-1))$
- Therefore, for numerical reasons, the information (w(t₀),...,w(t-1)) has to be compressed or approximated

Scenarios can be organized like a comb or like a tree



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There are two classical ways to compress information

State-based functional approach

In the special case of the Markovian framework with $(w(t_0), \ldots, w(T))$ white noise, there is no loss of optimality to look for solutions as

$$u(t) = \psi_t \underbrace{(x(t))}_{\text{state}} \quad \text{where} \quad \underbrace{x(t) \in \mathbb{X}}_{\text{fixed space}}, \quad \underbrace{x(t+1) = F_t(x(t), u(t), w(t))}_{\text{dynamical equation}}$$

Scenario-based measurability approach
 Scenarios are approximated by a finite family (w^s(t₀),..., w^s(T)), s ∈ S

• Either solutions $u^{s}(t)$ are indexed by $s \in S$ with the constraint that

$$(w^{s}(t_{0}),\ldots,w^{s'}(t-1)) = (w^{s'}(t_{0}),\ldots,w^{s'}(t-1)) \Rightarrow u^{s}(t) = u^{s'}(t)$$

 Or — in the case of the scenario tree approach, where the scenarios (w^s(t₀),...,w^s(T)), s ∈ S, are organized in a tree solutions uⁿ(t) are indexed by nodes n on the tree

More on what is a solution at time t State-based approach $u(t) = \psi_t(x(t))$

- The mapping ψ_t can be computed in advance (that is, at initial time t_0) and evaluated at time t on the available online information at that time t
 - either exactly (for example, by dynamic programming)
 - or approximately (for example, among linear decision rules) because the computational burden of finding *any* function is heavy
- The value $u(t) = \psi_t(x(t))$ can be computed at time t
 - either exactly by solving a proper optimization problem, which raises issues of dynamic consistency
 - or approximately

(for example, by assuming that controls from time t on are open-loop)

More on what is a solution at time *t* Scenario-based approach

• An optimal "solution" can be computed scenario by scenario, with the problem that we obtain solutions such that

$$ig(w^s(t_0),\ldots,w^s(t-1)ig)=ig(w^{s'}(t_0),\ldots,w^{s'}(t-1)ig)$$
 and $u^s(t)
eq u^{s'}(t)$

• Optimal solutions can be computed scenario by scenario and then merged (for example, by Progressive Hedging) to be forced to satisfy

 $(w^{s}(t_0),\ldots,w^{s}(t-1))=(w^{s'}(t_0),\ldots,w^{s'}(t-1))\Rightarrow u^{s}(t)=u^{s'}(t)$

- The value u(t) can be computed at time t depending on $(w^{s}(t_{0}), \ldots, w^{s}(t-1))$
 - either exactly by solving a proper optimization problem, which raises issues of dynamic consistency
 - or approximately (for example, by a sequence of two-stages problems)

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5 A need for training and research

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Where do we stand?

- How one frames the non-anticipativity constraint impacts numerical resolution methods
- On a finite scenario space, one obtains large (deterministic) optimization problems either on a tree or on a comb
- Else, one resorts to state-based formulations, with solutions as policies (dynamic programming)

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Optimization approaches to attack complexity

Linear programming

- linear equations and inequalities
- no curse of dimension

Stochastic programming

- no special treatment of time and uncertainties
- no independence assumption
- decisions are indexed by a scenario tree
- what if information is not a node in the tree?

State-based dynamic optimization

- nonlinear equations and inequalities
- curse of dimensionality
- independence assumption on uncertainties
- special treatment of time (dynamic programming equation)
- decisions are indexed by an information state (feedback synthesis)
- an information state summarizes past controls and uncertainties
- decomposition-coordination methods to overcome the curse of dimensionality?

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Summary

- Stochastic optimization highlights risk attitudes tackling
- Stochastic *dynamic* optimization emphasizes the handling of online information
- Many issues are raised, because
 - many ways to represent risk (criterion, constraints)
 - many information structures
 - tremendous numerical obstacles to overcome
- Each method has its numerical wall
 - in dynamic programming, the bottleneck is the dimension of the state (no more than 3)
 - in stochastic programming, the bottleneck is the number of stages (no more than 2)

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- Two snapshots on ongoing research
- 5 A need for training and research

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Outline of the presentation

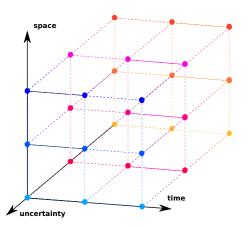
- Long term industry-academy cooperation
 - École des Ponts ParisTech–Cermics–Optimization and Systems
 - Industry partners of the Optimization and Systems Group
 - The remolding of power systems seen from an optimizer perspective
 - The remolding of power systems
 - Optimization is challenged
 - Moving from deterministic to stochastic dynamic optimization
 - Working out a toy example
 - Expliciting risk attitudes
 - Handling online information
 - Discussing framing and resolution methods
- Two snapshots on ongoing research
 - Decomposition-coordination optimization methods under uncertainty
 - Risk constraints in optimization
- 6 A need for training and research

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Decomposition-coordination: divide and conquer

- Spatial decomposition
 - Multiple players with their local information
 - Scales: local / regional / national /supranational
- Temporal decomposition
 - A state is an information summary
 - Time coordination realized through Dynamic Programming, by value functions
 - Hard nonanticipativity constraints
- Scenario decomposition
 - Along each scenario, sub-problems are deterministic (powerful algorithms)
 - Scenario coordination realized through Progressive Hedging, by updating nonanticipativity multipliers
 - Soft nonanticipativity constraints

Coupling constraints: an overview

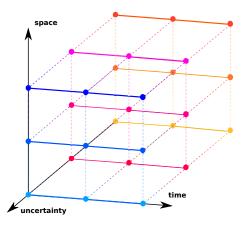


$$\min_{\mathbf{x},\mathbf{u}} \sum_{s=1}^{S} \sum_{i=1}^{N} \sum_{t=0}^{T} \pi_{s} L_{i,t} (\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})$$

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Michel DE LARA (CERMICS, France)

Coupling constraints: time coupling

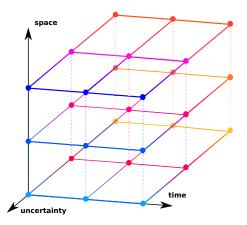


$$\min_{\mathbf{x}, \mathbf{u}} \sum_{s=1}^{S} \sum_{i=1}^{N} \sum_{t=0}^{T} L_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})$$

s.t. $\mathbf{x}_{i,t+1} = f_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})$

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Coupling constraints: scenario coupling

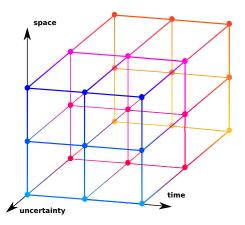


$$\min_{\mathbf{x},\mathbf{u}} \sum_{s=1}^{S} \sum_{i=1}^{N} \sum_{t=0}^{T} L_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})$$
s.t. $\mathbf{x}_{i,t+1} = f_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})$
 $\sigma(\mathbf{u}_{i,t}) \subset \sigma(\mathbf{w}_{0}, \dots, \mathbf{w}_{t})$

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Coupling constraints: space coupling



$$\begin{split} \min_{\mathbf{x},\mathbf{u}} & \sum_{s=1}^{S} \sum_{i=1}^{N} \sum_{t=0}^{T} L_{i,t} (\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t}) \\ \text{s.t.} & \mathbf{x}_{i,t+1} = f_{i,t} (\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t}) \\ & \sigma(\mathbf{u}_{i,t}) \subset \sigma(\mathbf{w}_{0}, \dots, \mathbf{w}_{t}) \\ & \sum_{i=1}^{N} \theta_{i,t} (\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t}) = 0 \end{split}$$

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Decomposition/coordination methods: an overview

Main idea

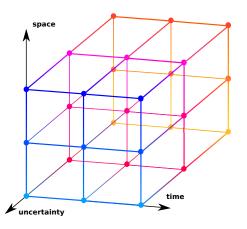
- decompose a large scale problem into smaller subproblems we are able to solve by efficient algorithms
- coordinate the subproblems for the concatenation of their solutions to form the initial problem solution

How to decompose the problem by duality?

- identify the coupling dimensions of the problem: time, uncertainty, space
- Q dualize the coupling constraints by introducing multiplyers
- split the problem into the resulting subproblems and coordinate them by means of the multiplyer

In the case of time decomposition, we can use the time arrow to chain static subproblems by the dynamics equation (without dualizing)

Decomposition/coordination methods: an overview

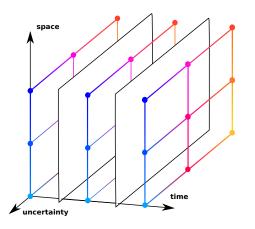


$$\begin{split} \min_{\mathbf{x},\mathbf{u}} & \mathbb{E}\bigg(\sum_{i=1}^{N}\sum_{t=0}^{T}L_{i,t}\big(\mathbf{x}_{i,t},\,\mathbf{u}_{i,t},\,\mathbf{w}_{t}\big)\bigg)\\ \text{s.t.} & \mathbf{x}_{i,t+1} = f_{i,t}\big(\mathbf{x}_{i,t},\,\mathbf{u}_{i,t},\,\mathbf{w}_{t}\big)\\ & \mathbf{u}_{i,t} = \mathbb{E}\big(\mathbf{u}_{i,t} \mid \mathbf{w}_{0},\ldots,\mathbf{w}_{t}\big)\\ & \sum_{i=1}^{N}\theta_{i,t}\big(\mathbf{x}_{i,t},\,\mathbf{u}_{i,t},\,\mathbf{w}_{t}\big) = 0 \end{split}$$

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Decomposition-coordination optimization methods under uncertainty

Decomposition/coordination methods: time coupling



$$\begin{split} \min_{\mathbf{x},\mathbf{u}} & \mathbb{E}\bigg(\sum_{i=1}^{N}\sum_{t=0}^{T}L_{i,t}\big(\mathbf{x}_{i,t},\,\mathbf{u}_{i,t},\,\mathbf{w}_{t}\big)\bigg)\\ \text{s.t.} & \mathbf{x}_{i,t+1} = f_{i,t}\big(\mathbf{x}_{i,t},\,\mathbf{u}_{i,t},\,\mathbf{w}_{t}\big)\\ & \mathbf{u}_{i,t} = \mathbb{E}\big(\mathbf{u}_{i,t} \mid \mathbf{w}_{0},\ldots,\mathbf{w}_{t}\big)\\ & \sum_{i=1}^{N}\theta_{i,t}\big(\mathbf{x}_{i,t},\,\mathbf{u}_{i,t},\,\mathbf{w}_{t}\big) = 0 \end{split}$$

[Stochastic Pontryagin] [Dynamic Programming]

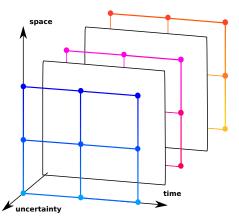
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Workshop STORY, Berkeley, 26 January 2015

January 25, 2015 90 / 125

Decomposition/coordination methods: scenario coupling



$$\min_{\mathbf{x},\mathbf{u}} \mathbb{E}\left(\sum_{i=1}^{N}\sum_{t=0}^{T}L_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})\right)$$

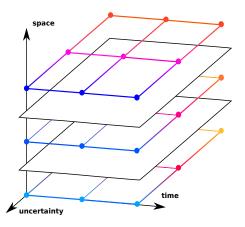
s.t. $\mathbf{x}_{i,t+1} = f_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})$
 $\mathbf{u}_{i,t} = \mathbb{E}(\mathbf{u}_{i,t} \mid \mathbf{w}_{0}, \dots, \mathbf{w}_{t})$
 $\sum_{i=1}^{N}\theta_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t}) = 0$

[Progressive Hedging]

Rockafellar, R.T., Wets R. J-B. Scenario and policy aggregation in optimization under uncertainty, Mathematics of Operations Research, 16, pp. 119-147, 1991

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Decomposition/coordination methods: space coupling



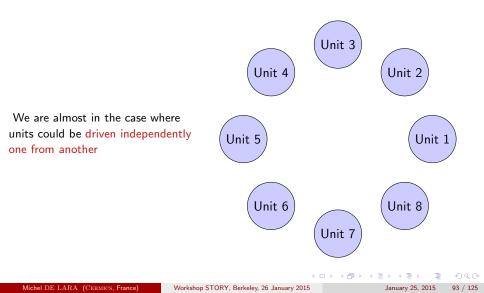
$$\min_{\mathbf{x},\mathbf{u}} \mathbb{E}\left(\sum_{i=1}^{N}\sum_{t=0}^{T}L_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})\right)$$

s.t. $\mathbf{x}_{i,t+1} = f_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t})$
 $\sigma(\mathbf{u}_{i,t}) \subset \sigma(\mathbf{w}_{0}, \dots, \mathbf{w}_{t})$
 $\sum_{i=1}^{N}\theta_{i,t}(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{t}) = 0$

[Our purpose now]

We have a nice decomposed problem but...

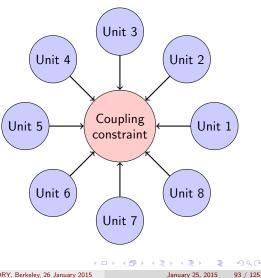
Flower structure



We have a nice decomposed problem but...

Flower structure

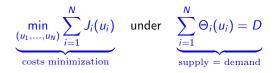
Unfortunately...



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The associated optimization problem can be written as



where

- *u_i* is the decision of each unit *i*
- $J_i(u_i)$ is the cost of making decision u_i for unit *i*
- $\Theta_i(u_i)$ is the production induced by making decision u_i for unit *i*

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Under appropriate duality assumptions, the associated optimization problem can be written without constraints

• For a proper Lagrange multiplier λ

$$\min_{(u_1,\ldots,u_N)}\sum_{i=1}^N J_i(u_i) + \lambda \underbrace{\left(\sum_{i=1}^N \Theta_i(u_i) - D\right)}_{\text{constraint}}$$

• We distribute the coupling constraint to each unit *i*

$$\min_{(u_1,\ldots,u_N)} \big(\sum_{i=1}^N J_i(u_i) + \lambda \Theta_i(u_i)\big) - \lambda D$$

• The problems splits into N optimization problems

$$\min_{u_i} \left(J_i(u_i) + \lambda \Theta_i(u_i) \right), \quad \forall i = 1, \dots, N$$

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Proper prices allow decentralization of the optimum

$$\min_{(u_1,\ldots,u_N)}\sum_{i=1}^N J_i(u_i) \quad \text{under} \quad \sum_{i=1}^N \Theta_i(u_i) = D$$

The simplest decomposition/coordination scheme consists in

- buying the production of each unit at a price $\lambda^{(k)}$ at iteration k
- and letting each unit minimize its modified costs

$$\min_{u_i} J_i(u_i) + \underbrace{\lambda^{(k)}}_{\text{price}} \Theta_i(u_i)$$

• then, updating the price depending on the coupling constraint

$$\lambda^{(k+1)} = \lambda^{(k)} + \rho \Big(\sum_{i=1}^{N} \Theta_i(u_i) - D \Big)$$

(like in the "tâtonnement de Walras" in Economics)

What are the stakes if we extend spatial coupling constraint decomposition to the dynamical and stochastic setting?

• Allowing for time and uncertainties, we classically consider the criterion

$$\min_{\{\mathbf{u}_{i,t}\}_{i\in\{1,N\}}} \mathbb{E}\left(\sum_{i=1}^{N} \left(\sum_{t=0}^{T-1} L_{i,t}(\mathbf{x}_{i,t},\mathbf{u}_{i,t},\mathbf{w}_{i,t}) + K_{i}(\mathbf{x}_{i,T})\right)\right)$$

under the constraints

$$\begin{split} \sum_{i=1}^{N} \Theta_{i,t} \big(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{i,t} \big) - \mathbf{d}_t &= 0, \\ \mathbf{x}_{i,t+1} &= f_{i,t} \big(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{i,t} \big), \end{split} \qquad t \in \llbracket 0, T-1 \rrbracket \end{split}$$

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To avoid finding "magical solutions", only implementable by a wizard knowing the future, we need to specify information constraints

- The optimization problem is not well posed, because we have not specified upon what depends the control **u**_{*i*,*t*} of each unit *i* at each time *t*
- In the causal and perfect memory case,
 we express that the control u_{i,t} depends of all past noises up to time t
 - either by a functional approach

$$\mathbf{u}_{i,t} = \phi_{i,t} \big(\mathbf{w}_{1,0}, \dots, \mathbf{w}_{N,0}, \mathbf{d}_0 \dots \dots \mathbf{w}_{1,t}, \dots, \mathbf{w}_{N,t}, \mathbf{d}_t \big)$$

• or by an algebraic approach

$$\sigma(\mathbf{u}_{i,t}) \subset \sigma(\mathbf{w}_{1,0},\ldots,\mathbf{w}_{N,0},\mathbf{d}_0\ldots\ldots\mathbf{w}_{1,t},\ldots,\mathbf{w}_{N,t},\mathbf{d}_t)$$

Looking after decentralizing prices models

• Going on with the previous scheme, each unit *i* solves

 $\min_{\mathbf{u}_{i,0},\ldots,\mathbf{u}_{i,\tau}} \mathbb{E}\left(\sum_{t=0}^{\tau-1} \left(L_{i,t}(\mathbf{x}_{i,t},\mathbf{u}_{i,t},\mathbf{w}_{i,t}) + \frac{\lambda_{i,t}^{(k)}}{\sum_{\text{price}}} \Theta_{i,t}(\mathbf{x}_{i,t},\mathbf{u}_{i,t},\mathbf{w}_{i,t}) \right) + K_{i}(\mathbf{x}_{i,\tau}) \right)$

$$\mathbf{x}_{i,t+1} = f_{i,t} \big(\mathbf{x}_{i,t}, \mathbf{u}_{i,t}, \mathbf{w}_{i,t} \big), \quad t \in \llbracket 0, T - 1 \rrbracket$$

- The optimal controls $\mathbf{u}_{i,t}^{\star}$ of this problem depend
 - upon the local state **x**_{*i*,*t*}
 - and ... upon all past prices $(\lambda_{i,0}^{(k)}, \ldots, \lambda_{i,t}^{(k)})$!
- Research axis: find an approximate dynamical model for the price process, driven by proper information; for instance, replace $\lambda_{i,t}^{(k)}$ by $\mathbb{E}\left(\lambda_{i,t}^{(k)} \mid \mathbf{y}_t\right)$, where the information variable \mathbf{y}_t is a Markov process (short time memory) \rightarrow "demand response", "adaptive tariffs",

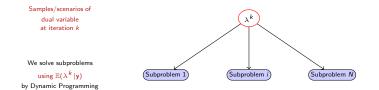
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Samples/scenarios of dual variable at iteration k



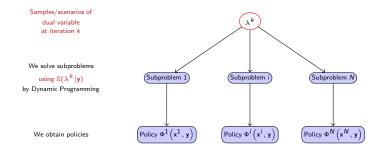
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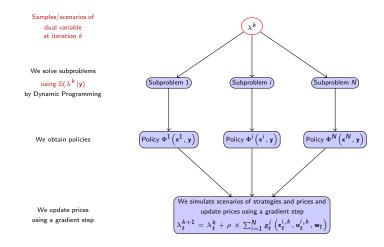


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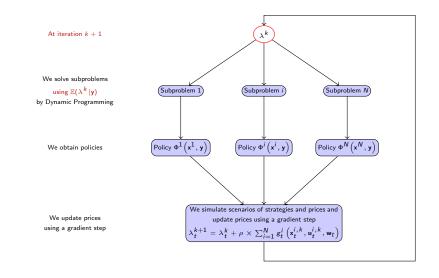


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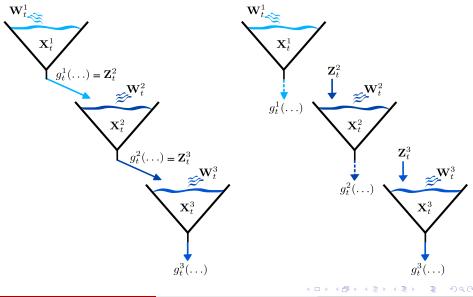


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Extension to interconnected dams



Contribution to dynamic tariffs

- Spatial decomposition of a dynamic stochastic optimization problem
- Lagrange multipliers attached to spatial coupling constraints are stochastic processes (prices)
- By projecting these prices, one expects to identify approximate dynamic models
- Such prices dynamic models are interpreted as dynamic tariffs

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Outline of the presentation

- Long term industry-academy cooperation
 - École des Ponts ParisTech–Cermics–Optimization and Systems
 - Industry partners of the Optimization and Systems Group
 - The remolding of power systems seen from an optimizer perspective
 - The remolding of power systems
 - Optimization is challenged
 - Moving from deterministic to stochastic dynamic optimization
 - Working out a toy example
 - Expliciting risk attitudes
 - Handling online information
 - Discussing framing and resolution methods

Two snapshots on ongoing research

- Decomposition-coordination optimization methods under uncertainty
- Risk constraints in optimization
- 5 A need for training and research

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Tourism issues impose constraints upon traditional economic management of a hydro-electric dam



- Maximizing the revenue from turbinated water
- under a tourism constraint of having enough water in July and August

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We consider a single dam nonlinear dynamical model in the decision-hazard setting

We model the dynamics of the water volume in a dam by



• S(t) volume (stock) of water at the beginning of period [t, t + 1[

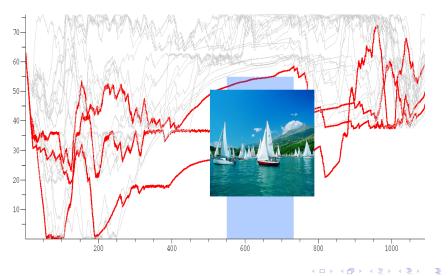
- q(t) turbined outflow volume during [t, t + 1[
 - ${\scriptstyle \bullet }$ decided at the beginning of period [t,t+1[
 - chosen such that $0 \le q(t) \le \min\{S(t), q^{\sharp}\}$
- *a*(*t*) inflow water volume (rain, etc.) during [*t*, *t* + 1[, which materializes at the end *t* + 1 of period [*t*, *t* + 1[
- S^{\sharp} dam capacity

The setting is called decision-hazard because the decision q(t) is made before the hazard a(t)

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Risk constraints in optimization

The red stock trajectories fail to meet the tourism constraint in July and August



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In the risk-neutral economic approach,

an optimal management maximizes the expected payoff

Suppose that

- turbined water q(t) is sold at price p(t), related to the price at which energy can be sold at time t
- a probability P is given on the set Ω = R^{T-t₀} × R^{T-t₀} of water inflows scenarios (a(t₀),..., a(T − 1)) and prices scenarios (p(t₀),..., p(T − 1))
- at the horizon, the final volume S(T) has a value K(S(T)), the "final value of water"
- The traditional (risk-neutral) economic problem is to maximize the intertemporal payoff (without discounting if the horizon is short)

$$\max \mathbb{E}\left[\sum_{t=t_0}^{T-1} \left(\overbrace{p(t) \quad q(t)}^{\text{price turbined}} \underbrace{-\epsilon q(t)^2}_{\text{turbined costs}} \right) + \overbrace{K(S(T))}^{\text{final volume utility}} \right]$$

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We now have a stochastic optimization problem, where the tourism constraint still needs to be dressed in formal clothes

• Traditional cost minimization/payoff maximization

$$\max \mathbb{E}\left[\sum_{t=t_0}^{T-1} \underbrace{p(t)q(t) - \epsilon q(t)^2}_{K(S(T))} + \underbrace{K(S(T))}_{K(S(T))}\right]$$

Tourism constraint

volume $S(t) \geq S^{\flat}$, $\forall t \in \mathcal{T} = \{ \text{ July, August } \}$

• In what sense should we consider this inequality which involves the random variables S(t) for $t \in \mathcal{T}$?

Robust / almost sure / probability constraint

 \bullet Robust constraints: for all the scenarios in a subset $\overline{\Omega} \subset \Omega$

$$S(t) \geq S^{\flat}, \ \forall t \in \mathcal{T}$$

• Almost sure constraints

$$\mathsf{Probability}\,\left\{S(t)\geq S^\flat\;,\;\;\forall t\in\mathcal{T}\right\}=1$$

• Probability constraints, with "confidence" level $p \in [0, 1]$

Probability
$$\left\{S(t) \geq S^{\flat}, \ \forall t \in \mathcal{T}\right\} \geq p$$

• and also by penalization, or in the mean, etc.

• • • • • • • • • • •

Our problem may be clothed as a stochastic optimization problem under a probability constraint

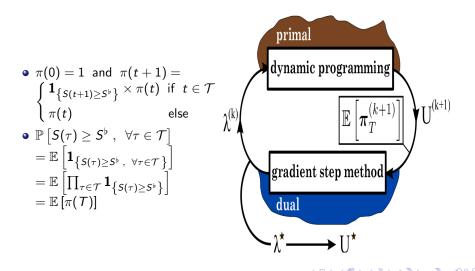
$$P(T) = \sum_{t=t_0}^{T-1} \underbrace{p(t)q(t) - \epsilon q(t)^2}_{t=t_0} + \underbrace{K(S(T))}_{K(S(T))}$$

- The traditional economic problem is $\max \mathbb{E}[P(T)]$
- and a failure tolerance is accepted

Probability
$$\left\{S(t) \geq S^{\flat}, \ \forall t \in \mathcal{T}\right\} \geq 90\%$$

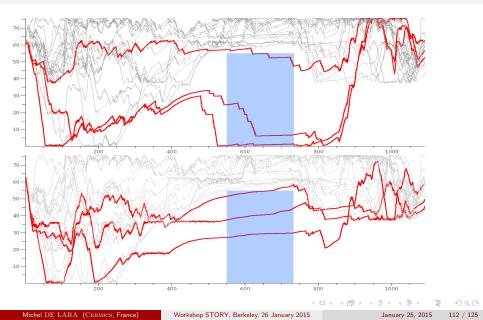
• Details concerning the theoretical and numerical resolution are available on demand ;-)

Details concerning the theoretical and numerical resolution are available on demand ;-)



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90% of the stock trajectories meet the tourism constraint

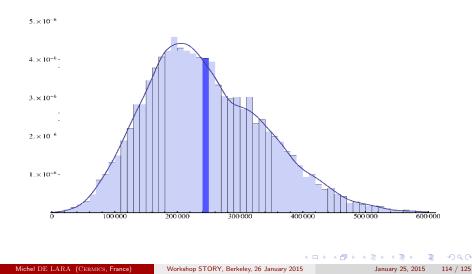


Our resolution approach brings a sensible improvement compared to standard procedures

OPTIMAL POLICIES	OPTIMIZATION		SIMULATION		
	Iterations	Time	Gain	Respect	Well behaviour
Standard	15	10 mn	ref	0,9	no
Convenient	10	160 mn	-3.20%	0,9	yes
Heuristic	10	160 mn	-3.25%	0,9	yes

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However, though the expected payoff is optimal, the payoff effectively realized can be far from it



We propose a stochastic viability formulation to treat symmetrically and to guarantee both environmental and economic objectives

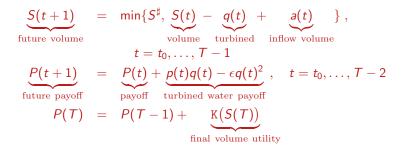
- Given two thresholds to be guaranteed
 - a volume S^{\flat} (measured in cubic hectometers hm^3)
 - a payoff P^b (measured in numeraire \$)
- we look after policies achieving the maximal viability probability

$$\Pi(S^{\flat}, P^{\flat}) = \max \operatorname{Proba} \begin{cases} \text{water inflow scenarios along which} \\ \text{the volumes } S(t) \ge S^{\flat} \\ \text{for all time } t \in \{ \text{July, August} \} \\ \text{and the final payoff } P(T) \ge P^{\flat} \end{cases}$$

 Π(S^b, P^b) is the maximal probability to guarantee to be above the thresholds S^b and P^b

The stochastic viability formulation requires to redefine state and dynamics

- The state is the couple x(t) = (S(t), P(t)) volume/payoff
- The control u(t) = q(t) is the turbined water
- The dynamics is



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In the stochastic viability formulation, we dress objectives as state constraints

• The control constraints are

$$u(t) \in \mathbb{B}(t, x(t)) \iff 0 \le q(t) \le \min\{S(t), q^{\sharp}\}$$

• The state constraints are

$$egin{aligned} \mathsf{x}(t) \in \mathbb{A}(t) & \Longleftrightarrow & \left\{ egin{aligned} S(t) \geq S^{\flat} &, & orall t \in \{ ext{ July, August } \} \ P(T) \geq P^{\flat} & & \end{aligned}
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For each couple of thresholds on payoff and stock, we write a dynamic programming equation

Abstract version

$$V(T,x) = \mathbf{1}_{\mathbb{A}(T)}(x) V(t,x) = \mathbf{1}_{\mathbb{A}(t)}(x) \max_{u \in \mathbb{B}(t,x)} \mathbb{E}_{w(t)} \Big[V\Big(t+1, \operatorname{Dyn}(t,x,u,w(t))\Big) \Big]$$

Specific version

$$V(T, S, P) = \mathbf{1}_{\{P \ge P^{\flat}\}}$$

$$V(T - 1, S, P) = \max_{\substack{0 \le q \le \min\{S, q^{\sharp}\}}} \mathbb{E}_{a(T-1), p(T-1)} \Big[V\Big(t + 1, S - q + a(t), P + K(S)\Big) \Big]$$

$$V(t, S, P) = \max_{\substack{0 \le q \le \min\{S, q^{\sharp}\}\\ t \notin \{ \text{ July, August } \}}} \mathbb{E}_{a(t), p(t)} \Big[V\Big(t + 1, S - q + a(t), P + p(t)q - \epsilon q^{2}\Big) \Big],$$

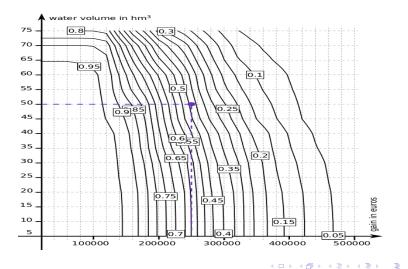
$$V(t, S, P) = \mathbf{1}_{\{S \ge S^{\flat}\}} \max_{\substack{0 \le q \le \min\{S, q^{\sharp}\}\\ t \in \{ \text{ July, August } \}}} \mathbb{E}_{a(t), p(t)} \Big[V\Big(t + 1, S - q + a(t), P + p(t)q - \epsilon q^{2}\Big) \Big],$$

$$t \in \{ \text{ July, August } \}$$

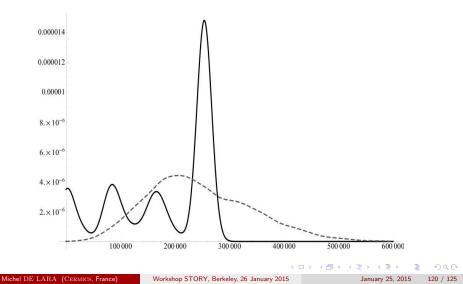
Michel DE LARA (CERMICS, France)

Risk constraints in optimization

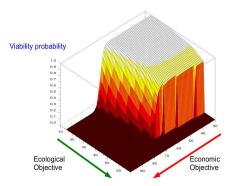
We plot iso-values for the maximal viability probability as a function of guaranteed thresholds S^{\flat} and P^{\flat}



The probability distribution of the random gain reflects the viability objectives



Contribution to quantitative sustainable management



- Conceptual framework for quantitative sustainable management
- Managing ecological and economic conflicting objectives
- Displaying tradeoffs between ecology and economy sustainability thresholds and risk

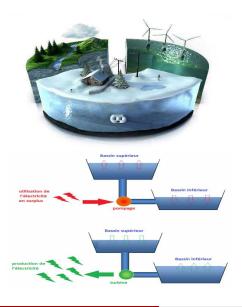
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Outline of the presentation

- Long term industry-academy cooperation
- 2 The remolding of power systems seen from an optimizer perspective
- 3 Moving from deterministic to stochastic dynamic optimization
- 4) Two snapshots on ongoing research
- 5 A need for training and research

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Trends are favorable to statistics and optimization



- More telecom technology
 → more data
- More data, more unpredicability
 → more statistics
- More unpredicability
 - $\hookrightarrow \mathsf{more}\ \mathsf{storage}$
 - $\hookrightarrow \mathsf{more} \ \mathsf{dynamic} \ \mathsf{optimization}$
- More unpredicability
 → more stochastic dynamic optimization

Image: A match a ma

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A context of increasing complexity





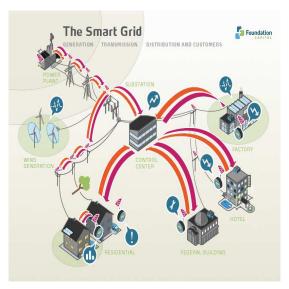
Demand Response

- Multiple energy resources: photovoltaic, solar heating, heatpumps, wind, hydraulic power, combined heat and power
- Spatially distributed energy resources (onshore and offshore windpower, solarfarms), producers, consumers
- Strongly variable production: wind, solar
- Intermittent demand: electrical vehicles
- Two-ways flows in the electrical network

Image: A match a ma

• Environmental and risk constraints (CO2, nuclear risk, land use)

Challenges ahead for stochastic optimization



- large scale stochastic optimization
- various risk constraints
- decentralized and private information
- game theory, stochastic equilibrium, market design...

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