

Control Theory and Viability Methods for the Sustainable Management of Natural Resources

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WANRM, CARM, Brisbane, 3 October 2017

October 2, 2017

We highlight management issues at the interface between nature and society



To make a long story short . . .

We claim that mathematical control theory is an insightful framework to deal with natural resources management issues

- Problems.** Many natural resources management problems can be grasped within **mathematical control theory**
- ▶ climate change mitigation, management of energies
 - ▶ fisheries management, epidemics control
- Methods.** Theory provides **concepts, tools** and **methods**
- ▶ viability kernel, viable controls
 - ▶ dynamic programming, monotonicity
- Answers.** **Practical answers** are obtained
- ▶ ecosystem viable yields, precautionary rules
 - ▶ tradeoffs display between economic and ecological sustainability thresholds and risk

I travel with colleagues along this journey

- ▶ C. Béné, L. Doyen, and D. Gabay. *A viability analysis for a bio-economic model*. **Ecological Economics**, 36: 385–396, 2001.
- ▶ M. De Lara, L. Doyen, T. Guilbaud, M.-J. Rochet. *Is a management framework based on spawning-stock biomass indicators sustainable? A viability approach..* In **ICES Journal of Marine Science**, 64(4):761–767, 2007.
- ▶ M. De Lara, L. Doyen, T. Guilbaud, M.-J. Rochet. *Monotonicity properties for the viable control of discrete time systems* **Systems and Control Letters** Volume 56, Number 4, 296–302, 2006.
- ▶ V. Martinet and L. Doyen. *Sustainable management of an exhaustible resource: a viable control approach*. **Resource and Energy Economics**, 29(1):p.17–39, 2007.
- ▶ V. Martinet, L. Doyen, and O. Thébaud. *Defining viable recovery paths toward sustainable fisheries*. **Ecological Economics**, 64(2):411–422, 2007.
- ▶ L. Doyen, M. De Lara, J. Ferraris, and D. Pelletier. *Sustainability of exploited marine ecosystems through protected areas: a viability model and a coral reef case study*. **Ecological Modelling**, 208(2-4):353–366, November 2007.
- ▶ M. De Lara and V. Martinet. *Multi-criteria dynamic decision under uncertainty: a stochastic viability analysis and an application to sustainable fishery management*. **Mathematical Biosciences**, Volume 217, Issue 2, 118–124, February 2009.
- ▶ M. De Lara, P. Gajardo, H. Ramírez C. *Viable harvest of monotone bioeconomic models*. **Systems and Control Letters**, 2010 Volume 60, 192–197, 2011.
- ▶ L. Doyen, M. De Lara. *Stochastic viability and dynamic programming*. **Systems and Control Letters**, Volume 59, Number 10, 629–634, 2010.
- ▶ Michel De Lara, Eladio Ocaña Anaya, Ricardo Oliveros–Ramos, Jorge Tam. *Ecosystem Viable Yields*. **Environmental Modeling & Assessment**, Volume 17, Issue 6, 565–575, 2012.
- ▶ Michel De Lara, Vincent Martinet, Luc Doyen. *Satisficing Versus Optimality: Criteria for Sustainability*. **Bulletin of Mathematical Biology**, Volume 77, Issue 2, 281–297, February 2015.
- ▶ Esther Regnier, Michel De Lara. *Robust Viable Analysis of a Harvested Ecosystem Model*. **Environmental Modeling & Assessment**, 2015.
- ▶ Vincent Martinet, Julio Peña-Torres, Michel De Lara, Hector Ramirez Cabrera. *Risk and Sustainability: Assessing Fishery Management Strategies*. **Environmental and Resource Economics**, March 2015

Outline of the presentation

Natural resources management issues and viability

- Examples of decision models

- Discrete-time viability

- Are the ICES fishing quotas recommendations “sustainable”?

- Ecosystem viable yields (anchovy-hake application)

Risk management, robust and stochastic viability

- Uncertainty variables are new input variables

- Robust viability

- Robust viability analysis of anchovy-hake Peruvian fisheries

- Stochastic viability

- Stochastic viability analysis of bycatches in a nephrops-hake fishery

- Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management

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Robust viability

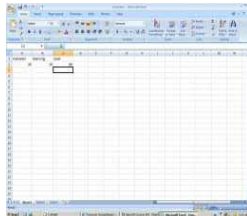
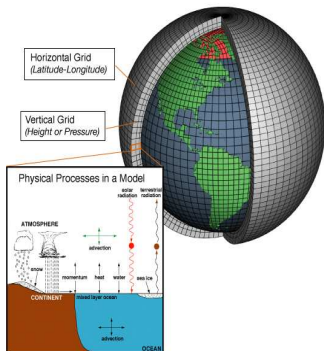
Robust viability analysis of anchovy-hake Peruvian fisheries

Stochastic viability

Stochastic viability analysis of bycatches in a nephrops-hake fishery

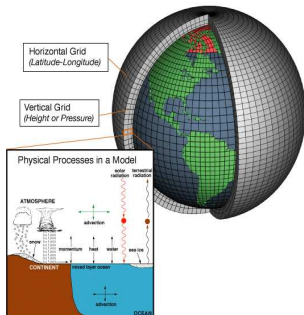
Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management



First, we start by laying out
a far-reaching distinction between
knowledge/assessment models
versus
decision models
(for control/optimization problems)

We distinguish two polar classes of models:
knowledge models *versus* decision models



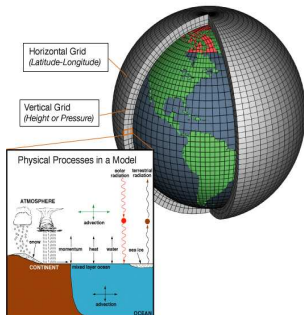
Knowledge models:

1/1 000 000 → 1/1 000 → 1/1

maps

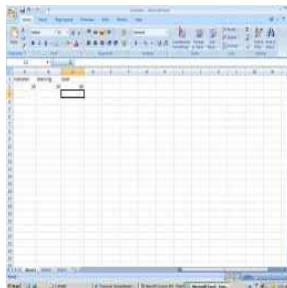
Office of Oceanic and
Atmospheric Research (OAR)
climate model

We distinguish two polar classes of models: knowledge models *versus* decision models



Knowledge models:
1/1 000 000 → 1/1 000 → 1/1
maps

Office of Oceanic and
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climate model



Action/decision models:
economic models are **fables**
designed to provide **insight**

William Nordhaus
economic-climate model

This talk is *not* about crafting dynamical models

- ▶ Elaborating a dynamical model is a delicate venture
 - ▶ Peter Yodzis, *Predator-Prey Theory and Management of Multispecies Fisheries*, Ecological Applications 4:51–58, 1994

In population modelling the functional forms of models are at least as important as are parameter values in expressing the underlying biology and in determining the outcome. (...) For instance, May et al. (1979) assumed, without comment, a particular form of predator-prey interaction; and this particular form was carried over, again without comment, by Flaaten. It turns out that this "invisible" but powerful assumption is responsible in large part for the conclusion reached by Flaaten (1988). (...) Flaaten's work is controversial because of his conclusion that "sea mammals should be heavily depleted to increase the surplus production of fish resources for man" (Flaaten 1988:114).
- ▶ Our starting point will be a mathematical dynamical model that captures how sequences of decisions affect a “piece of reality”
- ▶ Then, we will use such a model **to frame a decision problem**

Second, we present a series of
natural resources management problems
formalized by means of
decision model + viability/optimization problem

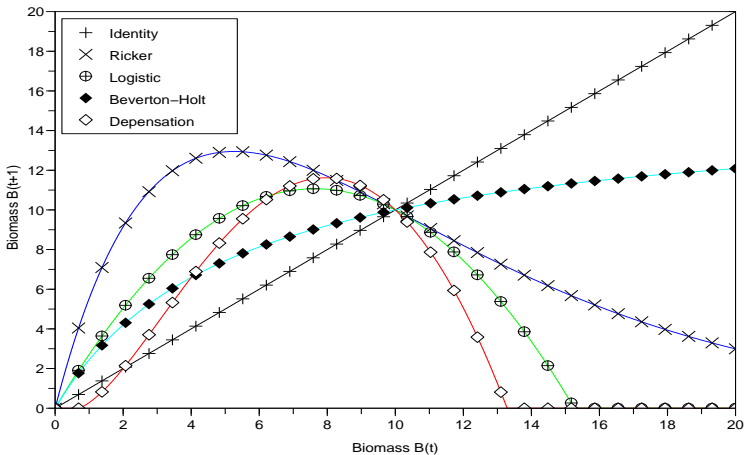
Viable management of an animal population



$$B(t+1) = \overbrace{\text{Biol}}^{\text{dynamic}} \left(\underbrace{B(t)}_{\text{biomass}} - \underbrace{h(t)}_{\text{catches}} \right)$$

- ▶ $B(t)$ biomass
- ▶ $h(t)$ catch with $0 \leq h(t) \leq B(t)$
- ▶ Biol natural resource growth function
(linear, logistic, etc.)

Biomass dynamics



Distinct population dynamics Bio1 for $r = 1.9$, $K = 10$, $B^b = 2$

We define an ecological window by lower and upper bounds for the biomass



State constraints

$$B^b \leq B(t) \leq B^\# , \quad t = t_0, \dots, T$$

- ▶ B^b minimum viable population
- ▶ $B^\#$ maximal safety value
(pest control, invasive species)

Epidemics control

Endemic channels form the core of a decision rule for dengue outbreak prevention

The epidemiological surveillance system should be able to differentiate between transient and seasonal increases in disease incidence and increases observed at the beginning of a dengue outbreak. One such approach is to track the occurrence of current (probable) cases and compare them with the average number of cases by week (or month) of the preceding 5–7 years, with confidence intervals set at two standard deviations above and below the average ($\pm 2 SD$). This is sometimes referred to as the “endemic channel”. If the number of cases reported exceeds 2 SDs above the “endemic channel” in weekly or monthly reporting, an outbreak alert is triggered.

Dengue. Guidelines for Diagnosis, Treatment, Prevention and Control. A joint publication of the World Health Organization (WHO) and the Special Programme for Research and Training in Tropical Diseases (TDR), 2009

We consider an epidemiological model with vector control

- ▶ Basic variables and parameters are
 - ▶ time $t = t_0, t_0 + 1, \dots, T - 1, T$, measured in days
 - ▶ M_t , the abundance of infected mosquitos (Aedes Aegypti adultos)
 - ▶ H_t , the abundance of infected humans
 - ▶ $\Delta\mu_t^M$, the additional mortality rate of mosquitos, a control variable
 - ▶ $\bar{M}, \bar{H}, f^H, f^M, \mu^M$ and μ^H , parameters
- ▶ The controlled dynamics of an epidemic outbreak is

$$\begin{aligned}M_{t+1} &= f^H H_t (\bar{M} - M_t) - (\mu^M + \Delta\mu_t^M) M_t \\H_{t+1} &= f^M M_t (\bar{H} - H_t) - \mu^H H_t\end{aligned}$$

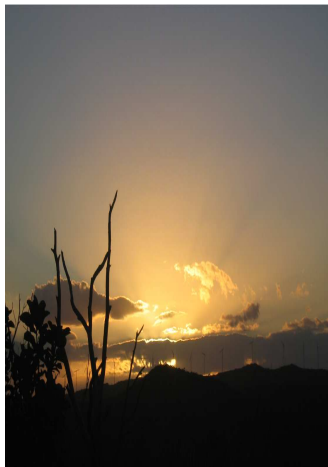
- ▶ The objective is to maintain infected humans at a low level

$$H_t \leq H^\#, \quad \forall t = t_0, \dots, T$$

with limited resources $0 \leq \Delta\mu_t^M \leq \Delta\mu^\#, \quad \forall t = t_0, \dots, T - 1$

Climate change mitigation

Let us scout a very stylized model of the climate-economy system



We lay out a dynamical model with

- ▶ two **state** variables

environmental: atmospheric CO_2
concentration level $M(t)$

economic: gross world product
gwp $Q(t)$

- ▶ one **decision** variable,
the emission **abatement rate** $a(t)$

A carbon cycle model “à la Nordhaus” is an example of *decision model*

- ▶ Time index t in years
- ▶ Economic production $Q(t)$ (gwp)

$$Q(t+1) = \overbrace{(1+g)}^{\text{economic growth}} Q(t)$$

- ▶ CO_2 concentration $M(t)$

$$M(t+1) = M(t) \underbrace{-\delta(M(t) - M_{-\infty})}_{\text{natural sinks}} + \alpha \overbrace{\text{Emiss}(Q(t))}_{\text{emissions}} \underbrace{(1 - a(t))}_{\text{abatement}}$$

- ▶ Decision $a(t) \in [0, 1]$ is the abatement rate of CO_2 emissions

Data

- ▶ $M(t)$ CO_2 atmospheric concentration, measured in ppm, parts per million
(379 ppm in 2005)
- ▶ $M_{-\infty}$ pre-industrial atmospheric concentration
(about 280 ppm)
- ▶ $\text{Emiss}(Q(t))$ “business as usual” CO_2 emissions
(about 7.2 GtC per year between 2000 and 2005)
- ▶ $0 \leq a(t) \leq 1$ abatement rate reduction of CO_2 emissions
- ▶ α conversion factor from emissions to concentration
($\alpha \approx 0.471 \text{ ppm} \cdot \text{GtC}^{-1}$ sums up highly complex physical mechanisms)
- ▶ δ natural rate of removal of atmospheric CO_2 to unspecified sinks
($\delta \approx 0.01 \text{ year}^{-1}$)

A concentration target is pursued to avoid danger



United Nations Framework Convention on Climate Change

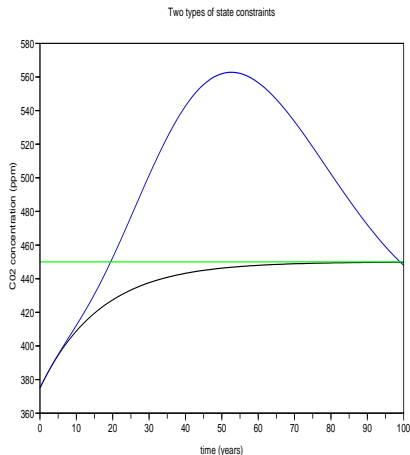
“to achieve, (...), stabilization of greenhouse gas concentrations in the atmosphere at a level that would prevent dangerous anthropogenic interference with the climate system”

Limitation of concentrations of CO_2

- ▶ below a tolerable threshold $M^\#$
(say 350 ppm, 450 ppm)
- ▶ at a specified date $T > 0$
(say year 2050 or 2100)

$$\underbrace{M(T)}_{\text{concentration at horizon}} \leq \underbrace{M^\#}_{\text{threshold}}$$

Constraints capture different requirements



- ▶ The **concentration** has to remain below a tolerable level **at the horizon T** :

$$M(T) \leq M^\#$$

- ▶ More demanding: **from the initial time t_0 up to the horizon T**

$$M(t) \leq M^\#$$

$$t = t_0, \dots, T$$

Constraints may be environmental, physical, economic

- ▶ The **concentration** has to remain below a tolerable level from initial time t_0 up to the horizon T

$$M(t) \leq M^\sharp, \quad t = t_0, \dots, T$$

- ▶ Abatements are expressed as fractions

$$0 \leq a(t) \leq 1, \quad t = t_0, \dots, T - 1$$

- ▶ As with “cap and trade”, setting a **ceiling on CO_2 price** amounts to cap abatement costs

$$\underbrace{\text{Cost}(a(t), Q(t))}_{\text{costs}} \leq c^\sharp (100 \text{ euros} / \text{tonne CO}_2), \quad t = t_0, \dots, T - 1$$

Mixing dynamics, optimization and constraints yields a cost-effectiveness problem

- ▶ Minimize abatement costs

$$\min_{a(t_0), \dots, a(T-1)} \sum_{t=t_0}^{T-1} \left(\frac{1}{1+r_e} \right)^{t-t_0} \underbrace{\text{Cost}(a(t), Q(t))}_{\text{abatement costs}}$$

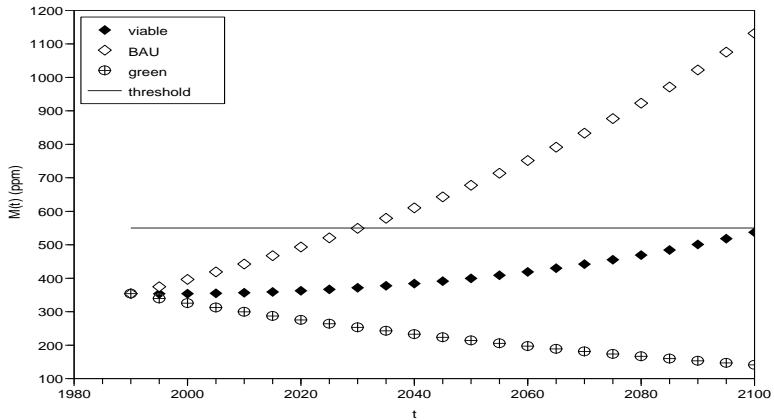
- ▶ under the gwp-co₂ dynamics

$$\begin{cases} M(t+1) &= M(t) - \delta(M(t) - M_{-\infty}) + \alpha \text{Emiss}(Q(t))(1 - a(t)) \\ Q(t+1) &= (1+g)Q(t) \end{cases}$$

- ▶ and under target constraint

$$\underbrace{M(T) \leq M^\#}_{\text{CO}_2 \text{ concentration}}$$

Concentration CO2



Fishery management

Populations can be described by abundances at ages



Jack Mackrel abundances (Chilean data)
are measured in **thousand of individuals**

13651022 thousand of age < 1 (recruits)

7495888 thousand of age $\in [1, 2[$

6804151

4191318

4582943

2500338

1139182

523261

269328

166390

95606

thousand of age ≥ 11

We now line up the ingredients of a harvested population age-class dynamical model



- ▶ **Time** $t \in \mathbb{N}$ measured in years
- ▶ **Abundances** at age
 $N = (N_a)_{a=1, \dots, A} \in \mathbb{X} = \mathbb{R}_+^A$
- ▶ $a \in \{1, \dots, A\}$ **age class index**
 - ▶ $A = 3$ for anchovy
 - ▶ $A = 8$ for hake
 - ▶ $A = 40$ for bacalao
- ▶ **Control** variable $\lambda \in \mathbb{U} = \mathbb{R}_+$
is **fishing effort**

One year older every year...

Except for the recruits ($a = 1$) and the last age class ($a = A$),

$$N_a(t+1) = e^{\underbrace{M_{a-1}}_{\text{natural mortality}} + \underbrace{\lambda(t)F_{a-1}}_{\text{fishing mortality}}} N_{a-1}(t), \quad a = 2, \dots, A-1$$

where

- ▶ M_a stands for the **natural mortality-at-age a**
- ▶ F_a is the harvesting mortality rate of individuals of age a , also called **exploitation pattern-at-age a** , related to the mesh size for instance
- ▶ the control variable $\lambda(t)$ is the fishing effort, or the **exploitation pattern multiplier**



The last age-class may comprise a plus-group

- ▶ N_A is the abundance of individuals of age **above** $A - 1$ (and not equal, like for other classes)
- ▶ To account for this specificity, one considers the dynamics

$$N_A(t+1) = N_{A-1}(t) \exp(- (M_{A-1} + \lambda(t)F_{A-1})) \\ + \underbrace{\pi}_{0 \text{ or } 1} N_A(t) \exp(- (M_A + \lambda(t)F_A))$$

- ▶ The parameter $\pi \in \{0, 1\}$ is related to the existence of a so-called **plus-group**
 - ▶ if we neglect the survivors older than age A , then $\pi = 0$ (an example is anchovy)
 - ▶ if we consider the survivors older than age A , then $\pi = 1$, and the last age class is a plus group (an example is hake)

The stock-recruitment function mathematically turns spawning stock biomass into future recruits abundance

- ▶ The **spawning stock biomass** is

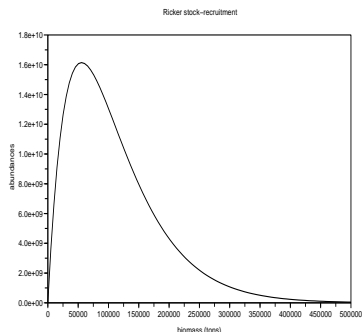
$$\text{SSB}(N) = \sum_{a=1}^A \underbrace{\gamma_a}_{\text{proportion}} \underbrace{\mu_a}_{\text{mass}} \underbrace{N_a}_{\text{abundance}}$$

- ▶ γ_a proportion of matures-at-age a
- ▶ μ_a weight-at-age a
- ▶ The **stock-recruitment relationship** S/R turns biomass into abundance

$$\underbrace{N_1(t+1)}_{\text{future recruits}} = \text{S/R} \left(\underbrace{\text{SSB}(N(t))}_{\text{spawning biomass}} \right)$$

Here are traditional examples of stock-recruitment functions

Recruitment involves complex biological and environmental processes that fluctuate in time, and are difficult to integrate into a population model



- ▶ constant: $S/R(B) = R$
- ▶ linear: $S/R(B) = rB$
- ▶ Beverton-Holt:
$$S/R(B) = \frac{B}{\alpha + \beta B}$$
- ▶ Ricker: $S/R(B) = \alpha B e^{-\beta B}$

And here are the state vector and the control

- ▶ The **state** vector $N(t)$ is forged with abundances at age

$$N(t) = \begin{pmatrix} N_1(t) \\ N_2(t) \\ \vdots \\ N_{A-1}(t) \\ N_A(t) \end{pmatrix} \in \mathbb{R}_+^A$$

- ▶ The scalar **control** $\lambda(t)$ is the fishing effort multiplier

A harvested population age-class model is an A -dimensional controlled dynamical system

$$N_1(t+1) = S/R \left(\overbrace{\text{SSB}(N(t))}^{\text{spawning biomass}} \right) \quad \text{recruitment}$$

$$N_2(t+1) = e^{-(M_1 + \lambda(t)F_1)} N_1(t)$$

$$N_a(t+1) = e^{\overbrace{-(M_{a-1} + \lambda(t)F_{a-1})}^{\text{mortality}}} N_{a-1}(t), \quad a = 2, \dots, A-1$$

natural
fishing

$$N_{A-1}(t+1) = e^{-(M_{A-2} + \lambda(t)F_{A-2})} N_{A-2}(t)$$

$$N_A(t+1) = e^{-(M_{A-1} + \lambda(t)F_{A-1})} N_{A-1}(t) + \underbrace{\pi e^{-(M_A + \lambda(t)F_A)}}_{\text{plus group}} N_A(t)$$

The ices precautionary approach uses indicators and reference points to tackle ecological objectives

International Council for the Exploration of the Sea precautionary approach

- ▶ keeping (or restoring) **spawning stock biomass SSB** indicator **above a threshold** reference point B_{lim}
- ▶ restricting fishing effort to have **mean fishing mortality F** indicator **below a threshold** reference point F_{lim}

Definition	Notation	Anchovy	Hake
F limit RP	F_{lim}	/	0.35
SSB limit RP (t)	B_{lim}	21 000	100 000

Spawning biomass and fishing mortality are outputs of the harvested population age-class model

- ▶ Spawning stock biomass

$$\text{SSB}(N) = \sum_{a=1}^A \underbrace{\gamma_a}_{\text{proportion}} \underbrace{\mu_a}_{\text{mass}} \underbrace{N_a}_{\text{abundance}}$$

with reference point $\text{SSB}(N) \geq B_{\text{lim}}$

- ▶ Mean fishing mortality over age range from a_r to A_r

$$F(\lambda) = \frac{\lambda}{A_r - a_r + 1} \sum_{a=a_r}^{a=A_r} F_a$$

with reference point $F(\lambda) \leq F_{\text{lim}}$

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Robust viability

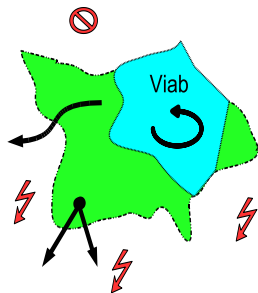
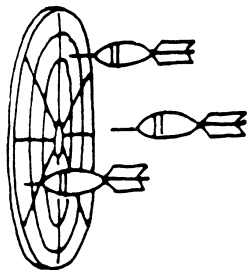
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A control system connects input and output variables



Input variables

Control wood logs
Uncertainty wood humidity,
metal
conductivity

Output variables

soup quality,
water vapor,
temperature
(internal state)

Discrete-time nonlinear state-control systems are special input-output systems

A specific output is distinguished, and is labeled **state**,
when the system may be written as

$$x(t+1) = F(t, x(t), u(t)), \quad t \in \mathbb{T} = \{t_0, t_0 + 1, \dots, T - 1\}$$

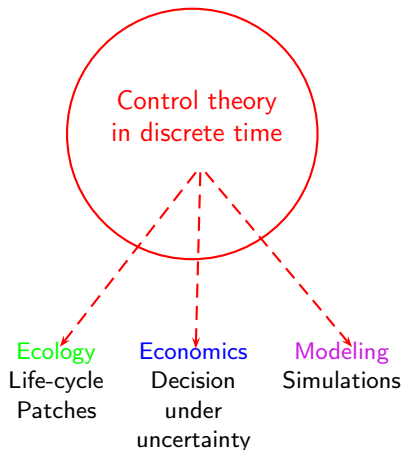
- ▶ the **time** $t \in \bar{\mathbb{T}} = \{t_0, t_0 + 1, \dots, T - 1, T\} \subset \mathbb{N}$ is discrete with **initial time** t_0 and **horizon** T ($T < +\infty$ or $T = +\infty$)
(the time period $[t, t + 1[$ may be a year, a month, etc.)
- ▶ the **state variable** $x(t)$ belongs to the *state space* $\mathbb{X} = \mathbb{R}^{n_x}$
(stocks, biomasses, abundances, capital)
- ▶ the **control variable** $u(t)$ is an element of the *control space* $\mathbb{U} = \mathbb{R}^{n_u}$
(inflows, outflows, catches, harvesting effort, investment)
- ▶ the **dynamics** F maps $\mathbb{T} \times \mathbb{X} \times \mathbb{U}$ into \mathbb{X}
(storage, age-class model, population dynamics, economic model)



A historical snapshot on the distinction between states and controls

The Maximum Principle of optimal control: A history of ingenious ideas and missed opportunities, by Hans Josef Pesch and Michael Plail, Control and Cybernetics, vol. 38 (2009) No. 4A

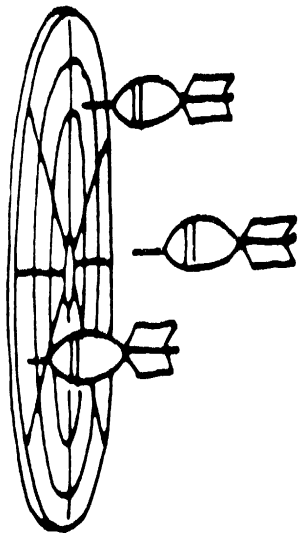
- ▶ Lawrence M. Graves (1932, 1933) distinguished the state variables and the degrees of freedom by different letters
- ▶ Buried in RAND reports (1949, 1950), Magnus R. Hestenes has definitely introduced different notations for the state and the control variables
- ▶ RAND (Research ANd Development) corporation: Magnus R. Hestenes, Rufus P. Isaacs, Richard E. Bellman
- ▶ Later, Rudolf E. Kálmán as well introduced the concept of state and control variables
- ▶ The letter *u* stands for the **Russian word for control: *upravlenie***
- ▶ Russian school: Pontryagin, Gamkrelidze, Boltyanskii

We dress natural resources management issues in the formal clothes of control theory in discrete time



- ▶ Problems are framed as
 - ▶ find **controls/decisions** driving a dynamical system
 - ▶ to achieve various **goals**
- ▶ Three main ingredients are
 - ▶ controlled dynamics 
 - ▶ constraints 
 - ▶ criterion to optimize

We mathematically express the objectives pursued as control and state constraints



- ▶ For a state-control system, we cloth **objectives as constraints**
- ▶ and we distinguish **control constraints** (rather easy) **state constraints** (rather difficult)
- ▶ Viability theory deals with state constraints

Constraints may be explicit on the control variable

and are rather easily handled by reducing the decision set

Examples of control constraints

- ▶ Irreversibility constraints, physical bounds

$$0 \leq a(t) \leq 1, \quad 0 \leq h(t) \leq B(t)$$

- ▶ Tolerable costs $c(a(t), Q(t)) \leq c^\#$



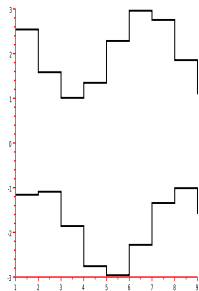
Control constraints / admissible decisions

$$\underbrace{u(t)}_{\text{control}} \in \underbrace{\mathbb{B}(t, x(t))}_{\text{admissible set}}, \quad t = t_0, \dots, T-1$$

Easy because control variables $u(t)$ are precisely those variables whose values the decision-maker can fix at any time within given bounds

Meeting constraints bearing on the state variable is delicate

due to the dynamics pipeline between controls and state



State constraints / admissible states

$$\underbrace{x(t)}_{\text{state}} \in \underbrace{\mathbb{A}(t)}_{\text{admissible set}}, \quad t = t_0, \dots, T$$

Examples (“tipping points”)

- ▶ CO_2 concentration $M(t) \leq M^\#$
- ▶ biomass $B^b \leq B(t) \leq B^\#$

State constraints are mathematically difficult because of “inertia”

$$x(t) = \underbrace{\text{function}}_{\text{iterated dynamics}} \left(\underbrace{u(t-1), \dots, u(t_0)}_{\text{past controls}}, x(t_0) \right)$$

Target and asymptotic state constraints are special cases

- ▶ **Final state** achieves some **target**

$$\underbrace{x(T)}_{\text{final state}} \in \underbrace{\mathbb{A}(T)}_{\text{target set}}$$

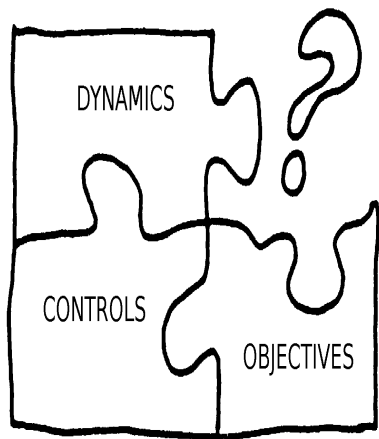
Example: CO₂ concentration

- ▶ **State converges** toward a **target**

$$\underbrace{\lim_{t \rightarrow +\infty} x(t)}_{\text{asymptotic state}} \in \underbrace{\mathbb{A}(\infty)}_{\text{target set}}$$

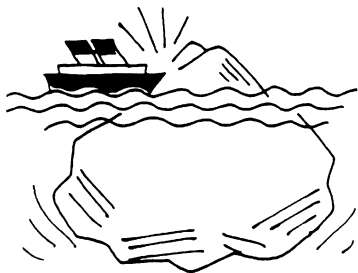
Example: in mathematical epidemiology, convergence towards an endemic state

Can we solve the compatibility puzzle between dynamics and objectives by means of appropriate controls?

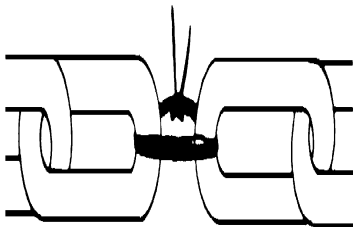
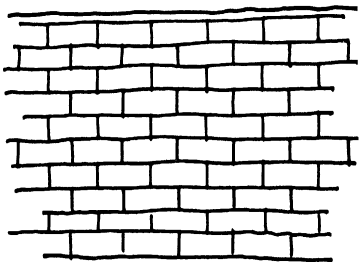


- ▶ **Given a dynamics** that mathematically embodies the causal impact of controls on the state
- ▶ **Imposing objectives** bearing on output variables (states, controls)
- ▶ Is it possible to **find a control path** that achieves the objectives for all times?

Crisis occurs when constraints are trespassed at least once



- ▶ An initial state is **not viable** if, whatever the sequence of controls, a crisis occurs
- ▶ **There exists a time** when one of the state or control constraints is **violated**

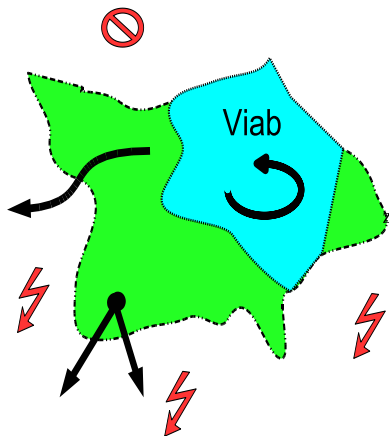


The compatibility puzzle can be solved when the initial viability kernel $\text{Viab}(t_0)$ is not empty

Viable initial states form the **viability kernel** (Jean-Pierre Aubin)

$$\text{Viab}(t) = \left\{ \begin{array}{l} \text{initial} \\ \text{states} \\ x \in \mathbb{X} \end{array} \left| \begin{array}{l} \text{there exist a control path } u(\cdot) = \\ (u(t), u(t+1), \dots, u(T-1)) \\ \text{and a state path } x(\cdot) = \\ (x(t), x(t+1), \dots, x(T)) \\ \text{starting from } x(t) = x \text{ at time } t \\ \text{satisfying for any time } s \in \{t, \dots, T-1\} \\ x(s+1) = F(s, x(s), u(s)) \quad \text{dynamics} \\ u(s) \in \mathbb{B}(s, x(s)) \quad \text{control constraints} \\ x(s) \in \mathbb{A}(s) \quad \text{state constraints} \\ \text{and } x(T) \in \mathbb{A}(T) \quad \text{target constraints} \end{array} \right. \right\}$$

The viability kernel is included in the state constraint set



- ▶ The largest set is the **state constraint set \mathbb{A}**
- ▶ It includes the smaller blue **viability kernel $\text{Viab}(t_0)$**
- ▶ The **green set** measures the incompatibility between dynamics and constraints: good start, but inevitable crisis!

The viability program aims at turning
a priori constraints, with state constraints,
into a posteriori constraints, without state constraints

- ▶ **A priori** constraints, **with state constraints**

$$\left\{ \begin{array}{l} x(t_0) \in \mathbb{X} \\ x(t+1) = F(t, x(t), u(t)) \\ u(t) \in \mathbb{B}(t, x(t)) \quad \text{control constraints} \\ x(t) \in \mathbb{A}(t) \quad \text{state constraints} \end{array} \right.$$

- ▶ are turned into **a posteriori** constraints, **without state constraints**
except for the initial state

$$\left\{ \begin{array}{l} x(t_0) \in \mathbb{Viab}(t_0) \quad \text{initial state constraint} \\ x(t+1) = F(t, x(t), u(t)) \\ u(t) \in \mathbb{B}^{\text{viab}}(t, x(t)) \quad \text{control constraints} \end{array} \right.$$

The viability kernels satisfy a backward dynamic programming equation

Proposition

Assume that $T < +\infty$. The viability kernels $\mathbb{V}iab(t)$ satisfy a backward induction, where t runs from $T - 1$ down to t_0 :

$$\mathbb{V}iab(T) = \mathbb{A}(T)$$

$$\mathbb{V}iab(t) = \left\{ \begin{array}{l} \text{admissible states } x \in \mathbb{A}(t) \mid \\ \text{there exists an admissible control } u \in \mathbb{B}(t, x) \\ \text{such that the future state } F(t, x, u) \\ \text{belongs to the next viability kernel } \mathbb{V}iab(t + 1) \end{array} \right\}$$

DRAWBACK

The dynamic programming equation yields viable controls

- ▶ The following **viable regulation set**

$$\mathbb{B}^{\text{viab}}(t, x) = \{u \in \mathbb{B}(t, x) \mid F(t, x, u) \in \text{Viab}(t+1)\}$$

is not empty if and only if $x \in \text{Viab}(t)$

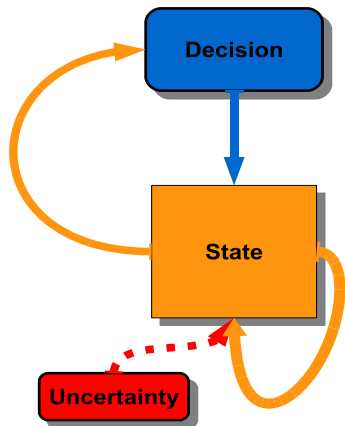
$$\mathbb{B}^{\text{viab}}(t, x) \neq \emptyset \iff x \in \text{Viab}(t)$$

- ▶ Any $u \in \mathbb{B}^{\text{viab}}(t, x)$ is said to be a **viable control**
- ▶ A **viable policy** is a mapping $\text{Pol} : \mathbb{T} \times \mathbb{X} \rightarrow \mathbb{U}$ such that

$$\text{Pol}(t, x) \in \mathbb{B}^{\text{viab}}(t, x)$$

for all $(t, x) \in \mathbb{T} \times \mathbb{X}$

“Policies” are closed-loop controls



- ▶ Deterministic control theory appeals to **open-loop** control, \oplus that is, a time-dependent sequence (**planning**, scheduling)

$$u : \underbrace{t \in \mathbb{T}}_{\text{time}} \mapsto \underbrace{u(t) \in \mathbb{U}}_{\text{control}}$$

- ▶ Another notion of solution is a **decision rule**, $\oplus \times \odot$ a **policy**, that is, a mapping

$$\text{Pol} : \underbrace{(t, x) \in \mathbb{T} \times \mathbb{X}}_{\text{(time, state)}} \mapsto u = \underbrace{\text{Pol}(t, x) \in \mathbb{U}}_{\text{control}}$$

which “closes the loop” between **time t –state x** and **control u** (and is especially relevant in presence of uncertainties)

Monotonicity assumptions on dynamics and constraints can help identify viable decision rules

Monotonicity assumptions

- ▶ **Dynamics F is monotonous:**
 - ▶ the more abundant today, the more tomorrow
 - ▶ the more harvested today, the less abundance tomorrow (monospecific models and technical interactions)
- ▶ **Constraints/objectives are monotonous functions**

Results

- ▶ **Lower and upper approximations** of the viability kernel
- ▶ **Precautionary viable** decision rules

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Are the ICES fishing quotas recommendations "sustainable"?

Ecosystem viable yields (anchovy-hake application)

Risk management, robust and stochastic viability

Uncertainty variables are new input variables

Robust viability

Robust viability analysis of anchovy-hake Peruvian fisheries

Stochastic viability

Stochastic viability analysis of bycatches in a nephrops-hake fishery

Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management



Is the ICES precautionary approach sustainable?

- ▶ The **precautionary approach (PA)** may be sketched as follows
 - ▶ the condition $SSB(N) \geq B_{lim}$ is checked
 - ▶ if valid, the following usual advice is given

$$\underbrace{\lambda_{UA}}_{\text{effort}} \underbrace{(N)}_{\text{abundance}} = \max\{\lambda \in \mathbb{R}_+ \mid \underbrace{SSB(F(N, \lambda))}_{\text{next year spawning biomass}} \geq B_{lim} \text{ and } \underbrace{F(\lambda)}_{\text{fishing mortality}} \leq F_{lim}\}$$

- ▶ Is it possible to apply the ICES precautionary rule every year?
- ▶ If so, can we **remain within precautionary bounds** as follows?

$$SSB(N(t)) \geq B_{lim} \text{ and } F(\lambda(t)) \leq F_{lim}, \quad \forall t = t_0, t_0 + 1, \dots$$

The ices precautionary rule is sustainable or not, depending on the stock-recruitment model

- ▶ Bay of Biscay anchovy

S/R Relationship	Constant	Constant	Constant (2002)	Constant (2004)	Linear	Ricker
Condition	$R_{\text{mean}} \geq R$	$R_{\text{gm}} \geq R$	$R_{\text{min}} \geq R$	$R_{\text{min}} \geq R$	$\gamma_1 \mu_1 r \geq 1$	
Left hand side	$14\,016 \times 10^6$	$7\,109 \times 10^6$	$3\,964 \times 10^6$	696×10^6	0.84	0
Right hand side	$1\,312 \times 10^6$	$1\,312 \times 10^6$	$1\,312 \times 10^6$	$1\,312 \times 10^6$	1	21\,000
Sustainable	yes	yes	yes	no	no	no

- ▶ For species with **late maturation**, like hake, **ices precautionary approach is never sustainable!**

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Robust viability

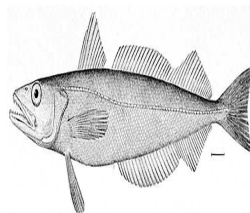
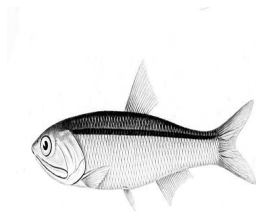
Robust viability analysis of anchovy-hake Peruvian fisheries

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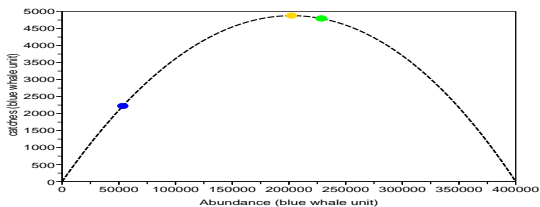
Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management

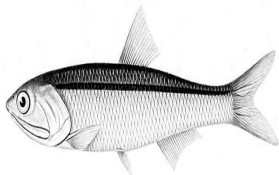
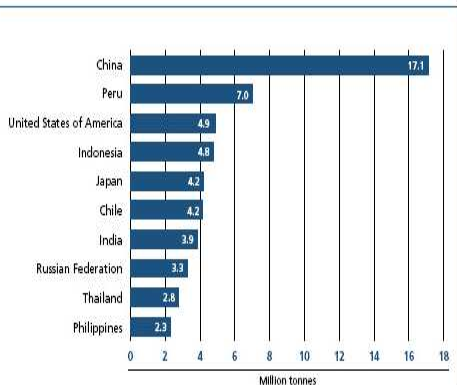


Despite calls to an “ecosystem approach”, stocks management remains monospecific

- ▶ The World Summit on Sustainable Development (Johannesburg, 2002) encouraged the application of the “ecosystem approach” by 2010
- ▶ but... following the Summit, the signatory States undertook to restore and exploit their stocks at maximum sustainable yield (MSY)
- ▶ The MSY is a concept which relies upon a monospecific dynamic model $\dot{B} = f(B) - qEB$ where B is biomass, and E fishing effort



Perú is World 2nd for marine and inland capture fisheries



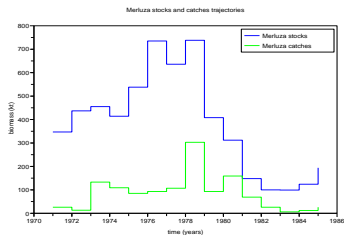
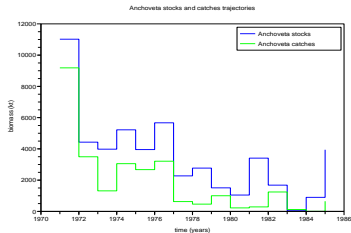
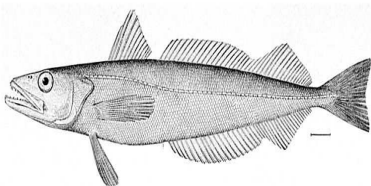
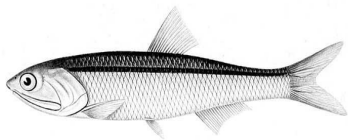
The northern Humboldt current system off Perú covers

less than 0.1% of the world ocean

but presently sustains

about 10% of the world fish catch

We were lucky enough that IMARPE entrusted us yearly data of anchoveta and merluza stock and catches from 1971 to 1985



We consider two species targeted by two fleets in a biomass ecosystem dynamic

We embody stocks and fishing interactions in a two-dimensional dynamical model

$$\begin{aligned} \underbrace{A(t+1)}_{\text{future biomass}} &= A(t) \underbrace{\mathcal{R}_A(A(t), H(t))}_{\text{growth factor}} \underbrace{(1 - E_A(t))}_{\substack{\text{effort} \\ \text{control}}} \\ H(t+1) &= H(t) \mathcal{R}_H(A(t), H(t)) \underbrace{(1 - E_H(t))}_{\substack{\text{effort} \\ \text{control}}} \end{aligned}$$

- ▶ State vector $(A(t), H(t))$ represents **biomasses**
- ▶ Control vector $(E_A(t), E_H(t))$ is **fishing effort** of each species
- ▶ **Catches** are $E_A(t)\mathcal{R}_A(A(t), H(t))A(t)$ and $E_H(t)\mathcal{R}_H(A(t), H(t))H(t)$ (measured in biomass)

Our objectives are twofold: conservation and production

The **viability kernel** is the set of **initial species biomasses** $(A(t_0), H(t_0))$ from which **appropriate effort controls** $(E_A(t), E_H(t))$, $t = t_0, t_0 + 1, \dots$ produce a **trajectory** of biomasses $(A(t), H(t))$, $t = t_0, t_0 + 1, \dots$ such that the following goals are satisfied

- ▶ **preservation** (minimal biomass thresholds)

$$A \text{ stocks: } A(t) \geq S_A^b$$

$$H \text{ stocks: } H(t) \geq S_H^b$$

- ▶ **economic/social** requirements (minimal catch thresholds)

$$A \text{ catches: } E_A(t) \mathcal{R}_A(A(t), H(t)) A(t) \geq C_A^b$$

$$H \text{ catches: } E_H(t) \mathcal{R}_H(A(t), H(t)) H(t) \geq C_H^b$$

We provide an explicit expression for the viability kernel under rather weak assumptions

Proposition

If the *thresholds* S_A^b, S_H^b and C_A^b, C_H^b meet the inequalities

$$\underbrace{S_A^b \mathcal{R}_A(S_A^b, S_H^b) - S_A^b}_{\text{surplus}} \geq C_A^b \quad \text{and} \quad \underbrace{S_H^b \mathcal{R}_H(S_A^b, S_H^b) - S_H^b}_{\text{surplus}} \geq C_H^b$$

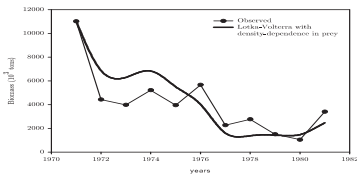
the *viability kernel* is given by

$$\left\{ (A, H) \mid A \geq S_A^b, H \geq S_H^b, A \mathcal{R}_A(A, H) - S_A^b \geq C_A^b, H \mathcal{R}_H(A, H) - S_H^b \geq C_H^b \right\}$$

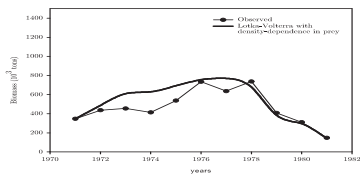
We Taylor a Lotka-Volterra *decision model* to hake-anchovy Peruvian fisheries scarce data

Hake-anchovy Peruvian fisheries data between 1971 and 1981, in thousands of tonnes (10^3 tons)

- ▶ anchoveta_stocks= [11019 4432 3982 5220 3954 5667 2272 2770 1506 1044 3407]
- ▶ merluza_stocks= [347 437 455 414 538 735 636 738 408 312 148]
- ▶ anchoveta_captures= [9184 3493 1313 3053 2673 3211 626 464 1000 223]
- ▶ merluza_captures= [26 13 133 109 85 93 107 303 93 159 69]



(a) Anchovy



(b) Hake

Figure: Comparison of observed and simulated biomasses of anchovy and hake using a Lotka-Volterra model with density-dependence in the prey. Model parameters are $R = 2.25$, $L = 0.945$, $\kappa = 67\,113 \times 10^3$ t ($K = 37\,285 \times 10^3$ t), $\alpha = 1.22 \times 10^{-6} t^{-1}$, $\beta = 4.845 \times 10^{-8} t^{-1}$.

Here is the Lotka-Volterra *decision model*

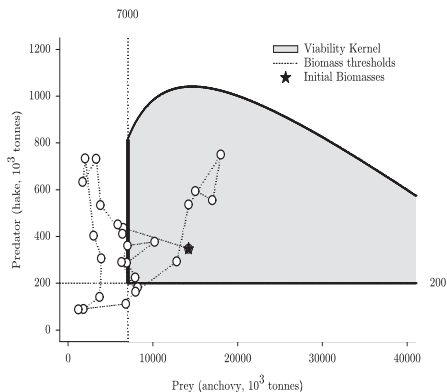
- ▶ A is the prey biomass (**anchovy**)
- ▶ H is the predator biomass (**hake**)
- ▶ The discrete-time Lotka-Volterra system is

$$\begin{aligned} A(t+1) &= A(t) \overbrace{\left(R - \frac{R}{\kappa} A(t) - \alpha H(t) \right)}^{\mathcal{R}_A(A(t), H(t))} (1 - E_A(t)) \\ H(t+1) &= H(t) \underbrace{\left(L + \beta A(t) \right)}_{\mathcal{R}_H(A(t), H(t))} (1 - E_H(t)), \end{aligned}$$

- ▶ The associated **deterministic viability kernel** is $\mathbb{V}(t_0) =$

$$\left\{ (A, H) \mid A \geq S_A^b, \frac{1}{\alpha} \left[R - \frac{R}{\kappa} A - \frac{S_A^b + C_A^b}{A} \right] \geq H \geq \max \left\{ \frac{S_H^b + C_H^b}{L + \beta A}, S_H^b \right\} \right\}$$

For given biomasses and catches thresholds,
we display the associated viability kernel



► Minimal biomasses thresholds

- $S_A^b = 7\,000\text{ kt}$ (anchovy)
- $S_H^b = 200\text{ kt}$ (hake)

► Minimal catches thresholds

- $C_A^b = 2\,000\text{ kt}$ (anchovy)
- $C_H^b = 5\text{ kt}$ (hake)

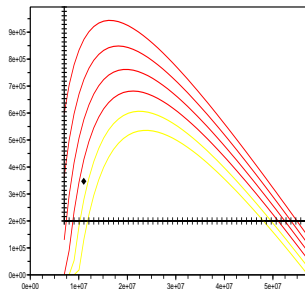
First acid test: plotting years of observed biomasses

- The range of values for viable states fits with measured biomasses
- Theoretically, a viable management with guaranteed biomasses and catches would have been possible since the initial state \star is viable

Let us make a pause on our way towards ecosystem viable yields

- ▶ Let us turn back on what we have covered so far
 - ▶ taking in consideration both ecological and economic objectives
 - ▶ we have identified the viable states starting from which both objectives can be guaranteed as time flies
- ▶ And let us change the perspective
 - ▶ by first guaranteeing the ecological objectives
 - ▶ and then identifying compatible captures that can be guaranteed
 - ▶ when starting from a given initial state

We use the viability kernel the other way round,
to design ecosystem viable yields



1. Considering that first are given minimal biomass conservation thresholds $S_A^b \geq 0$, $S_H^b \geq 0$
2. for initial biomasses $A_0 \geq S_A^b$ and $H_0 \geq S_H^b$, the following catch levels, if positive, can be sustainably maintained

$$C_A^{b,*}(A_0, H_0) = \min \{ S_A^b \mathcal{R}_A(S_A^b, S_H^b) - S_A^b; A_0 \mathcal{R}_A(A_0, H_0) - S_A^b \}$$

$$C_H^{b,*}(A_0, H_0) = \min \{ S_H^b \mathcal{R}_H(S_A^b, S_H^b) - S_H^b; H_0 \mathcal{R}_H(A_0, H_0) - S_H^b \}$$

And now, the second acid test... We compare theoretical ecosystem viable yields to Perú official quotas

	Viable yields (kt)		Perú official quotas (kt)	
	Model 1	Model 2	2006	2007
Anchovy	5 152	5 399		

And now, the second acid test. . . We compare theoretical ecosystem viable yields to Perú official quotas

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	Viable yields (kt)		Perú official quotas (kt)	
	Model 1	Model 2	2006	2007
Anchovy	5 152	5 399	4 250	5 300
Hake	49	56,8	55	35

- ▶ Quotas are maximal bounds on catches
- ▶ Ecosystem viable yields (EVY) are minimal guaranteed yields
- ▶ EVY are obtained by “puzzling” viable effort rules:
one can harvest more than the predator EVY to let the prey increase
- ▶ *Instituto del Mar del Perú* showed interest for this transparent method

Where have we gone till now? And what comes next

- ▶ We have laid out examples of natural resources management problems where objectives are framed as constraints, using the apparatus of mathematical control theory
- ▶ We have provided solutions derived from viability theory methods
- ▶ And now, how do we move from deterministic dynamics and constraints to the uncertainty situation?

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Natural resources management issues and viability

- Examples of decision models

- Discrete-time viability

- Are the ICES fishing quotas recommendations “sustainable”?

- Ecosystem viable yields (anchovy-hake application)

Risk management, robust and stochastic viability

- Uncertainty variables are new input variables

- Robust viability

- Robust viability analysis of anchovy-hake Peruvian fisheries

- Stochastic viability

- Stochastic viability analysis of bycatches in a nephrops-hake fishery

- Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management

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Contribution to quantitative sustainable management

A control system connects input and output variables



Input variables

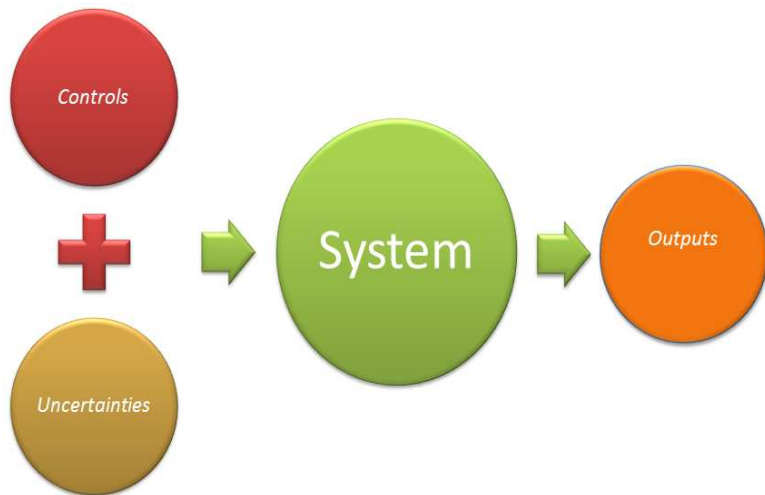
Control wood logs

Uncertainty wood humidity,
metal
conductivity

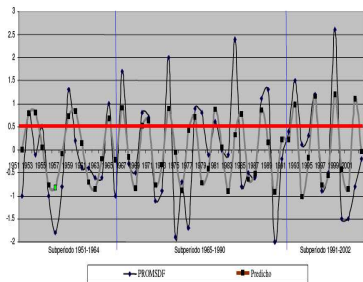
Output variables

soup quality,
water vapor,
temperature
(internal state)

Uncertainty variables are new input variables



Uncertainty is pervasive in natural resources management



- ▶ Environmental uncertainties (*El Niño*)
- ▶ Habitats changes, mortality, natality
- ▶ Scientific uncertainties (structure of trophic networks, ecosystem services)

We plug uncertain variables into the carbon cycle model “à la Nordhaus”

- ▶ Economic production $Q(t)$

$$Q(t+1) = \left(1 + \overbrace{g(w_e(t))}^{\text{economic growth}} \right) Q(t)$$

- ▶ CO_2 concentration $M(t)$

$$M(t+1) = M(t) - \delta(M(t) - M_{-\infty}) + \underbrace{\alpha(w_p(t))}_{\text{physics}} \overbrace{\text{Emiss}(Q(t), w_z(t))}^{\text{technologies}} (1 - a(t))$$

- ▶ **Vector of uncertainties** $w(t) = (w_e(t), w_p(t), w_z(t))$ on
 - ▶ economic growth
 - ▶ technologies
 - ▶ climate dynamics

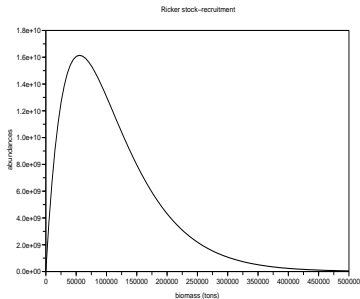
Uncertainties transpire in epidemiological models

- ▶ Basic variables and parameters are
 - ▶ time $t = t_0, t_0 + 1, \dots, T - 1, T$, measured in days
 - ▶ M_t , the **abundance of infected mosquitos** (*Aedes Aegypti* adultos)
 - ▶ H_t , the **abundance of infected humans**
 - ▶ $\Delta\mu_t^M$, the **additional mortality rate of mosquitos**, a **control variable**
 - ▶ $\bar{M}, \bar{H}, f^H, f^M, \mu^M$ and μ^H , parameters
- ▶ The controlled dynamics of an epidemic outbreak is

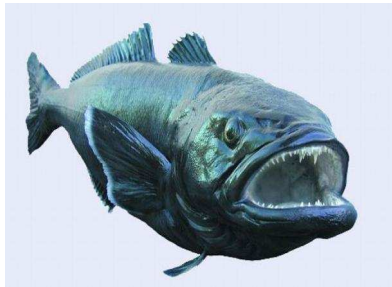
$$\begin{aligned}M_{t+1} &= f^H H_t (\bar{M} - M_t) - (\mu^M + \Delta\mu_t^M) M_t \\H_{t+1} &= f^M M_t (\bar{H} - H_t) - \mu^H H_t\end{aligned}$$

- ▶ Scientific literature provides **bounds** for
 - ▶ disease transmission rates f^H and f^M
 - ▶ mortality rate of mosquitos μ^M

Uncertainties about in population models



- ▶ Stock-recruitment relationship condenses, in one function, complex mechanisms of birth, dispersion, predation, habitats, physical conditions
- ▶ Natural mortality (diseases, predation) between age-classes is poorly known



We plug uncertain variables into the harvested age-class model

$$N_1(t+1) = S/R \left(\text{SSB}(N(t)), \underbrace{w(t)}_{\text{birth mortality, etc.}} \right) \quad \text{recruitment}$$

$$N_2(t+1) = e^{-(M_1 + \lambda(t)F_1)} N_1(t)$$

$$\vdots = \vdots$$

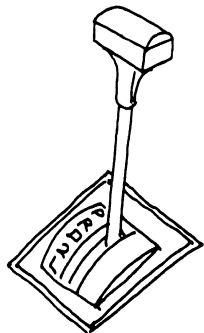
$$N_a(t+1) = e^{-(\overbrace{M_{a-1}}^{\text{mortality}} + \lambda(t)F_{a-1})} N_{a-1}(t), \quad a = 2, \dots, A-1$$

$$N_A(t+1) = e^{-(M_{A-1} + \lambda(t)F_{A-1})} N_{A-1}(t) + \pi e^{-(M_A + \lambda(t)F_A)} N_A(t)$$

Input control variables are in the hands of the decision-maker at successive time periods

Control variables $u(t) \in \mathbb{U}$

The decision-maker can **choose** the values of **control variables** $u(t)$ at any time within given bounds

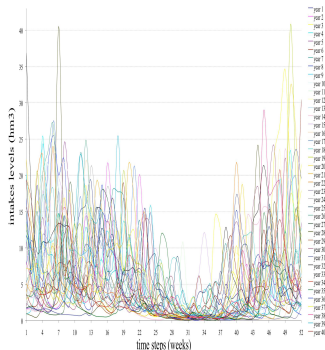


- ▶ at successive time periods
 - ▶ annual catches
 - ▶ years, months:
starting of energy units like nuclear plants
 - ▶ weeks, days, intra-day:
starting of hydropower units
- ▶ within given bounds
 - ▶ fishing quotas
 - ▶ turbined capacity

Input uncertain variables are out of the control of the decision-maker

Uncertain variables $w(t) \in \mathbb{W}$ are variables

- ▶ that take **more than one single value** (else they are deterministic)
- ▶ and **over which the decision-maker (DM) has no control whatsoever**



- ▶ **Stationary parameters:**
unitary cost of CO₂ emissions
- ▶ **Trends or seasonal effects:**
energy consumption pathway, mean temperatures, mean prices
- ▶ **Stochastic processes:**
rain inputs in a dam, energy demand, prices
- ▶ **Else (set membership):**
costs of climate change damage,
water inflows in a dam

Let us fix notations and vocabulary

Uncertainty variables are new input variables in a discrete-time nonlinear state-control system

A specific output is distinguished, and is labeled “state”
(more on this later), when the system may be written

$$x(t+1) = F(t, x(t), u(t), w(t)), \quad t \in \mathbb{T} = \{t_0, t_0 + 1, \dots, T - 1\}$$

- ▶ the **time** $t \in \overline{\mathbb{T}} = \{t_0, t_0 + 1, \dots, T - 1, T\} \subset \mathbb{N}$ is discrete with **initial time** t_0 and **horizon** T ($T < +\infty$ or $T = +\infty$)
(the time period $[t, t + 1[$ may be a year, a month, etc.)
- ▶ the **state variable** $x(t)$ belongs to the *state space* $\mathbb{X} = \mathbb{R}^{n_x}$
(stocks, biomasses, abundances, capital)
- ▶ the **control variable** $u(t)$ is an element of the *control space* $\mathbb{U} = \mathbb{R}^{n_u}$
(inflows, outflows, catches, harvesting effort, investment)
- ▶ the **uncertainty** $w(t) \in \mathbb{W} = \mathbb{R}^{n_w}$
(recruitment or mortality uncertainties, climate fluctuations)
- ▶ the **dynamics** F maps $\mathbb{T} \times \mathbb{X} \times \mathbb{U}$ into \mathbb{X}
(storage, age-class model, population dynamics, economic model)

What have we covered so far?

Uncertainty variables are new input variables

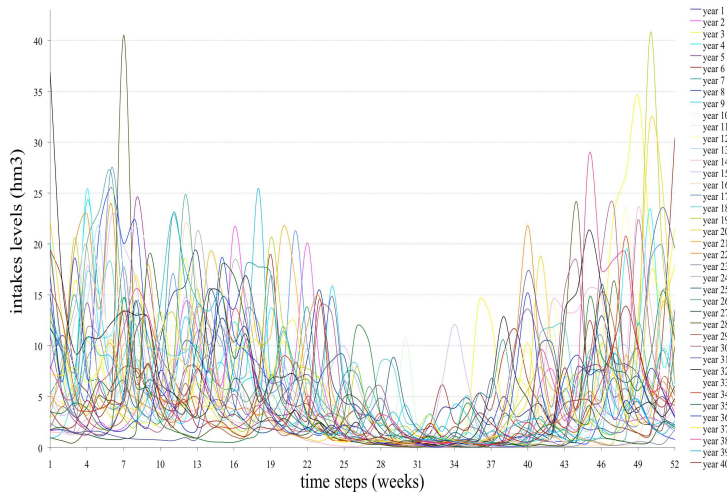
$$x(t+1) = F(t, x(t), u(t), \underbrace{w(t)}_{\text{uncertainty}})$$

- ▶ The future state $x(t+1)$ is no longer predictable
- ▶ because of the uncertain term $w(t)$,
- ▶ but the current state $x(t)$ carries information relevant for decision-making,
- ▶ and we shed light on the notion of policy

Summary

- ▶ Control variables are defined rather unambiguously:
the DM can select their values at any time within given sets
- ▶ The **distinction between input and output variables** is **relative to a system**: for two interconnected dams, the water release from the upper to the lower dam can be “seen” as an input to the lower dam or as a control variable for the two-dams system
- ▶ In various examples of natural resources management, we have seen so-called uncertain variables
- ▶ **Uncertain variables** are variables
 - ▶ which take **more than one single value** (else they are deterministic)
 - ▶ and **over which the decision-makers have no control whatsoever**
- ▶ Uncertain and control variables combine in a dynamical model

Water inflows historical scenarios

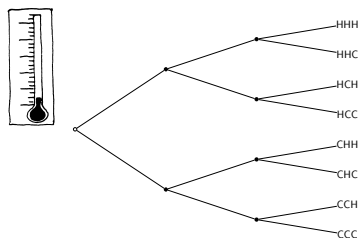


We call scenario a temporal sequence of uncertainties

Scenarios are special cases of “states of Nature”

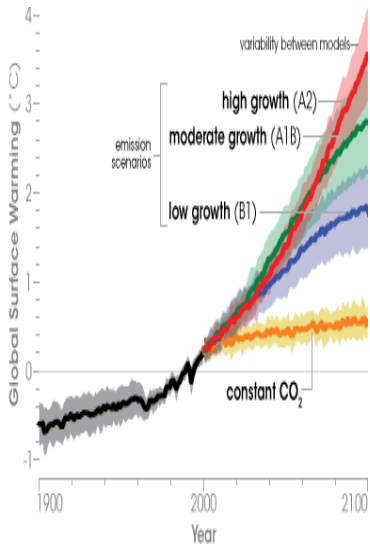
A **scenario** (pathway, chronicle) is a sequence of uncertainties

$$w(\cdot) = (w(t_0), w(t_0 + 1), \dots, w(T - 1)) \in \mathbb{S} = \mathbb{W}^{T-t_0}$$



El tiempo se bifurca perpetuamente hacia innumerables futuros
(Jorge Luis Borges, *El jardín de senderos que se bifurcan*)

Beware! Scenario holds a different meaning in other scientific communities



- ▶ In practice, what modelers call a “**scenario**” is a mixture of
 - ▶ a sequence of uncertain variables (also called a **pathway**, a **chronicle**)
 - ▶ a **policy** Po1
 - ▶ and even a **static or dynamical model**
- ▶ In what follows
scenario = pathway = chronicle

A scenario is said to be viable for a given policy if the state and control trajectories satisfy the constraints

Viable scenario under given policy

A scenario $w(\cdot) \in \mathbb{S}$ is said to be viable under policy $\text{Pol} : \mathbb{T} \times \mathbb{X} \rightarrow \mathbb{U}$ if the trajectories $x(\cdot)$ and $u(\cdot)$ generated by the dynamics

$$x(t+1) = F(t, x(t), u(t), w(t)), \quad t = t_0, \dots, T-1$$

with the policy

$$u(t) = \text{Pol}(t, x(t))$$

satisfy the state and control constraints

$$\underbrace{u(t) \in \mathbb{B}(t, x(t))}_{\text{control constraints}} \quad \text{and} \quad \underbrace{x(t) \in \mathbb{A}(t)}_{\text{state constraints}}, \quad \forall t = t_0, \dots, T$$

The set of viable scenarios is denoted by $\mathbb{S}_{\text{Pol}, t_0, x_0}$

We look after policies that make the corresponding set of viable scenarios “large”

Set of viable scenarios

$$\mathbb{S}_{\text{Po1}, t_0, x_0} = \{w(\cdot) \in \mathbb{S} \mid \begin{array}{l} \text{the state constraints} \\ x(t) \in \mathbb{A}(t) \\ \text{and the control constraints} \\ u(t) \in \mathbb{B}(t, x(t)) \\ \text{are satisfied for all times } t = t_0, \dots, T \} \end{array}$$

- ▶ The larger set $\mathbb{S}_{\text{Po1}, t_0, x_0}$ of viable scenarios, the better, because the policy Po1 is able to maintain the system within constraints for a large “number” of scenarios
- ▶ But “large” in what sense? Robust? Probabilistic?

Outline of the presentation

Natural resources management issues and viability

Examples of decision models

Discrete-time viability

Are the ICES fishing quotas recommendations “sustainable”?

Ecosystem viable yields (anchovy-hake application)

Risk management, robust and stochastic viability

Uncertainty variables are new input variables

Robust viability

Robust viability analysis of anchovy-hake Peruvian fisheries

Stochastic viability

Stochastic viability analysis of bycatches in a nephrops-hake fishery

Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management

Robust viability dissects how to channel the system inside constraints *whatever the scenarios*

Let $\overline{\mathbb{S}} \subset \mathbb{S}$ be a subset of the set \mathbb{S} of scenarios

The robust viability problem

Identify the initial states $x_0 \in \mathbb{X}$ for which there exists at least one **viable robust policy** $\text{Pol} : \mathbb{T} \times \mathbb{X} \rightarrow \mathbb{U}$ such that **for all scenarios** $w(\cdot) \in \overline{\mathbb{S}}$

- ▶ the state trajectories given by the state solution map $x(t) = X_F[t_0, x_0, \text{Pol}, w(\cdot)](t)$ satisfy the following **state constraints**

$$x(t) \in \mathbb{A}(t) \text{ for } t = t_0, \dots, T$$

- ▶ and the **control constraints** $u(t) = \text{Pol}(t, x(t)) \in \mathbb{B}(t, x(t))$ are satisfied for $t = t_0, \dots, T - 1$

The robust viability kernel is the set of initial states for which the robust viability problem can be solved

Robust viability kernel

$$\text{Viab}_1(t_0) = \left\{ x_0 \in \mathbb{X} \left| \begin{array}{l} \text{there exists a policy } \text{Pol} \in \mathcal{U} \\ \text{such that for all scenario } w(\cdot) \in \overline{\mathbb{S}} \\ \text{the state constraints } x(t) \in \mathbb{A}(t) \\ \text{and the control constraints} \\ u(t) = \text{Pol}(t, x(t)) \in \mathbb{B}(t, x(t)) \\ \text{are satisfied for all times } t = t_0, \dots, T \end{array} \right. \right\}$$

where the state $x(t) = X_F[t_0, x_0, \text{Pol}, w(\cdot)](t)$
is given by the state solution map

The robust viability kernel and viable scenarios are related

$$x_0 \in \underbrace{\text{Viab}_1(t_0)}_{\text{robust viability kernel}} \iff \left\{ \begin{array}{l} \text{there exists a policy } \text{Pol} \in \mathcal{U}, \\ \bar{\mathcal{S}} \subset \underbrace{\mathcal{S}_{\text{Pol}, t_0, x_0}}_{\text{viable scenarios}} \end{array} \right.$$

Robust viability kernels and robust viable policies can be defined for all times

Robust viability kernel at time t

The **robust viability kernel at time t** is the subset of states

$$\text{Viab}_1(t) = \left\{ x \in \mathbb{X} \left| \begin{array}{l} \text{there exists } \text{Po1} \in \mathcal{U}^{ad} \text{ such that} \\ \text{for all scenario } w(\cdot) \in \overline{\mathbb{S}} \\ x(s) \in \mathbb{A}(s) \text{ for } s = t, \dots, T \end{array} \right. \right\}$$

where $x(s) = X_F[t, x, \text{Po1}, w(\cdot)](s)$ is given by the state solution map
The final viability kernel is the whole target set: $\text{Viab}_1(T) = \mathbb{A}(T)$

Viable robust policies

$$\mathcal{U}_1^{\text{viab}}(t, x) = \left\{ \text{Po1} \in \mathcal{U}^{ad} \left| \begin{array}{l} \text{for all scenario } w(\cdot) \in \overline{\mathbb{S}} \\ X_F[t, x, \text{Po1}, w(\cdot)](s) \in \mathbb{A}(s) \\ \text{for } s = t, \dots, T \end{array} \right. \right\}$$

The viability program aims at turning state constraints into control constraints

- ▶ **A priori** constraints, **with state constraints**

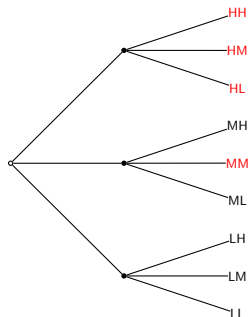
$$\begin{cases} x(t_0) \in \mathbb{X} \\ x(t+1) = F(t, x(t), u(t), w(t)) \\ u(t) \in \mathbb{B}(t, x(t)) \quad \text{control constraints} \\ x(t) \in \mathbb{A}(t) \quad \text{state constraints} \end{cases}$$

- ▶ are turned into **a posteriori** constraints, **without state constraints** except for the initial state

$$\begin{cases} x(t_0) \in \text{Viab}_1(t_0) \quad \text{initial state constraint} \\ x(t+1) = F(t, x(t), u(t), w(t)) \\ u(t) \in \mathbb{B}_1^{\text{viab}}(t, x(t)) \subset \mathbb{B}(t, x(t)) \quad \text{control constraints} \end{cases}$$

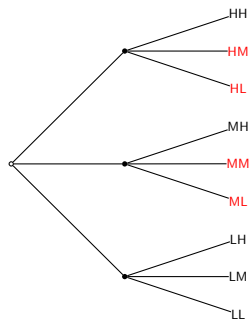
- ▶ **ex ante** state constraints \rightarrow **ex post** control constraints

Product scenarios subsets embody time independence



There is **no** time independence because the range of values of $w(t+1)$ depends on the value of $w(t)$:

- $w(t) = H \Rightarrow w(t+1) \in \{M, L\}$
- $w(t) = M \Rightarrow w(t+1) \in \{M\}$



There is time independence because

$$\bar{\mathcal{S}} = \{H, M\} \times \{M, L\} \subset \mathcal{S}$$

is a product set

A priori information on the scenarios may be set membership

The product case

- ▶ Uncertain variables may be restricted to subsets, period by period

$$w(t) \in \overline{W}(t) \subset W$$

so that some scenarios are selected and the rest are excluded

$$w(\cdot) \in \overline{S} = \overline{W}(t_0) \times \cdots \times \overline{W}(T-1) \subset S = W^{T-t_0}$$

Bounded water inflows in a dam

If only an upper bound on water inflows is known,
we represent off-line information by

$$0 \leq a(t) \leq a^\#$$

The robust dynamic programming equation is a backward equation relating the robust viability kernels

Robust dynamic programming equation

If the scenarios vary within a rectangle $\bar{S} = \bar{W}(t_0) \times \cdots \times \bar{W}(T-1)$ (corresponding to independence in the stochastic setting), the robust viability kernels satisfy the following backward induction, where t runs from $T-1$ down to t_0

$$\text{Viab}_1(T) = \mathbb{A}(T)$$

$$\text{Viab}_1(t) = \left\{ x \in \mathbb{A}(t) \left| \begin{array}{l} \text{there exists an admissible control } u \in \mathbb{B}(t, x) \\ \text{such that for all scenarios } w \in \bar{W}(t) \\ \text{one has that } F(t, x, u, w) \in \text{Viab}_1(t+1) \end{array} \right. \right\}$$

DRAWBACK

The robust dynamic programming equation yields the robust viable controls

Robust viable controls

For any time t and state x , **robust viable controls** are

$$\mathbb{B}_1^{\text{viab}}(t, x) = \{u \in \mathbb{B}(t, x) \mid \forall w \in \overline{\mathbb{W}}(t), F(t, x, u, w) \in \text{Viab}_1(t+1)\}$$

Proposition

Viable robust policies are those $\text{Pol} \in \mathcal{U}$ such that

$$\text{Pol}(t, x) \in \mathbb{B}_1^{\text{viab}}(t, x), \quad \forall t \in \mathbb{T}, \forall x \in \text{Viab}_1(t)$$

The viability program is achieved

- ▶ Robust viable controls exist at time t if and only if the state x belongs to the robust viability kernel at time t :

$$\mathbb{B}_1^{\text{viab}}(t, x) \neq \emptyset \iff x \in \text{Viab}_1(t)$$

- ▶ A **solution to the viability problem** is
 - ▶ an initial state x_0
 - ▶ and a policy Pol

such that

$$x_0 \in \text{Viab}_1(t_0)$$

$$\text{Pol}(t, x) \in \mathbb{B}_1^{\text{viab}}(t, x), \quad \forall t \in \mathbb{T}, \forall x \in \text{Viab}_1(t)$$

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Uncertainty variables are new input variables

Robust viability

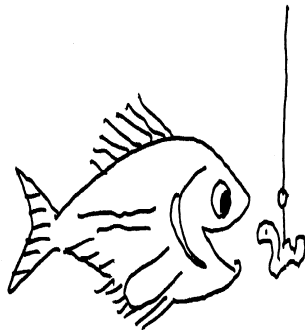
Robust viability analysis of anchovy-hake Peruvian fisheries

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Dam management under environmental/tourism constraint

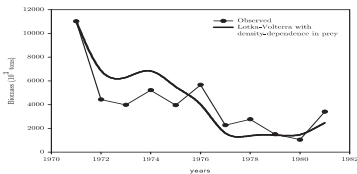
Contribution to quantitative sustainable management



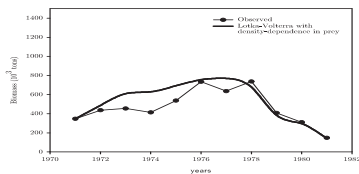
We tailored a Lotka-Volterra *decision model* to hake-anchovy Peruvian fisheries scarce data

Hake-anchovy Peruvian fisheries data between 1971 and 1981, in thousands of tonnes (10^3 tons)

- ▶ anchoveta_stocks= [11019 4432 3982 5220 3954 5667 2272 2770 1506 1044 3407]
- ▶ merluza_stocks= [347 437 455 414 538 735 636 738 408 312 148]
- ▶ anchoveta_captures= [9184 3493 1313 3053 2673 3211 626 464 1000 223]
- ▶ merluza_captures= [26 13 133 109 85 93 107 303 93 159 69]



(a) Anchovy



(b) Hake

Figure: Comparison of observed and simulated biomasses of anchovy and hake using a Lotka-Volterra model with density-dependence in the prey. Model parameters are $R = 2.25$, $L = 0.945$, $\kappa = 67\,113 \times 10^3$ t ($K = 37\,285 \times 10^3$ t), $\alpha = 1.22 \times 10^{-6} t^{-1}$, $\beta = 4.845 \times 10^{-8} t^{-1}$.

Now, we add an uncertain term, $w_A(t)$ and $w_H(t)$, to the growth rate of each population

- ▶ **Uncertainties** $w_A(t)$ and $w_H(t)$ are discrepancies between the Lotka-Volterra model and the data
- ▶ State vector $(A(t), H(t))$ represents **biomasses**
- ▶ Control vector $(E_A(t), E_H(t))$ is **fishing effort** of each species
- ▶ The discrete-time Lotka-Volterra system with uncertainty is

$$\begin{aligned} A(t+1) &= A(t) \underbrace{\left(w_A(t) + R - \frac{R}{\kappa} A(t) - \alpha H(t) \right)}_{\mathcal{R}_A(A(t), H(t), w_A(t))} (1 - E_A(t)) \\ H(t+1) &= H(t) \underbrace{\left(w_H(t) + L + \beta A(t) \right)}_{\mathcal{R}_H(A(t), H(t), w_H(t))} (1 - E_H(t)) \end{aligned}$$

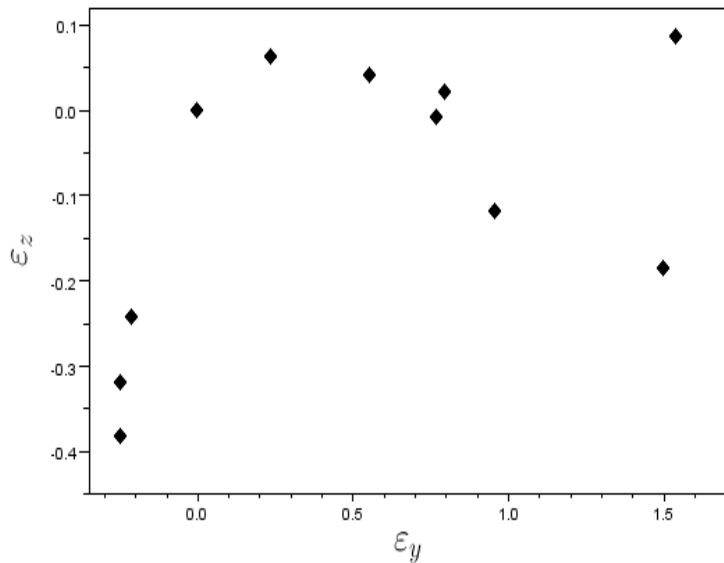
In practice, we consider stationary uncertainty sets forged from empirical data

- ▶ $(\bar{A}(t), \bar{H}(t))_{t=t_0, \dots, T}$ and $(\bar{E}_A(t), \bar{E}_H(t))_{t=t_0, \dots, T-1}$ denote the empirical biomass and effort trajectories between 1971 and 1981, in thousands of tonnes (10^3 tons)
 - ▶ anchoveta_stocks= [11019 4432 3982 5220 3954 5667 2272 2770 1506 1044 3407]
 - ▶ merluza_stocks= [347 437 455 414 538 735 636 738 408 312 148]
 - ▶ anchoveta_captures= [9184 3493 1313 3053 2673 3211 626 464 1000 223]
 - ▶ merluza_captures= [26 13 133 109 85 93 107 303 93 159 69]
- ▶ We define $\bar{w}_A(t)$ and $\bar{w}_H(t)$ such that

$$\begin{cases} \bar{A}(t+1) &= \bar{A}(t)(\bar{w}_A(t) + R - \frac{R}{\kappa}\bar{A}(t) - \alpha\bar{H}(t))(1 - \bar{E}_A(t)) \\ \bar{H}(t+1) &= \bar{H}(t)(\bar{w}_H(t) + L + \beta\bar{A}(t))(1 - \bar{E}_H(t)) \end{cases}$$

Empirical distribution of the uncertainties

$(\bar{w}_A(t), \bar{w}_H(t))_{t=t_0, \dots, T-1}$



We consider two species targeted by two fleets in a biomass ecosystem dynamics *with uncertainties*

We embody **uncertainties**, stocks and fishing interactions in a two-dimensional dynamical model

$$\begin{aligned} \underbrace{A(t+1)}_{\text{future biomass}} &= A(t) \underbrace{\mathcal{R}_A(A(t), H(t), w_A(t))}_{\text{growth factor}} (1 - \underbrace{E_A(t)}_{\text{effort control}}) \\ &\quad \underbrace{w_A(t)}_{\text{uncertainty}} \\ H(t+1) &= H(t) \mathcal{R}_H(A(t), H(t), \underbrace{w_H(t)}_{\text{uncertainty}}) (1 - \underbrace{E_H(t)}_{\text{effort control}}) \end{aligned}$$

- ▶ **Uncertainties** $w_A(t)$ and $w_H(t)$ are discrepancies
- ▶ State vector $(A(t), H(t))$ represents **biomasses**
- ▶ Control vector $(E_A(t), E_H(t))$ is **fishing effort** of each species
- ▶ **Catches** are $E_A(t)\mathcal{R}_A(A(t), H(t), w_A(t))A(t)$ and $E_H(t)\mathcal{R}_H(A(t), H(t), w_H(t))H(t)$ (measured in biomass)

Our objectives are twofold: conservation and production

The **robust viability kernel** is the set of **initial species biomasses** $(A(t_0), H(t_0))$ from which at least one appropriate **policy** produces biomasses and effort **trajectories** such that the following goals are satisfied

for all the scenarios $(w_A(t), w_H(t))$, $t = t_0, t_0 + 1, \dots, T$

- ▶ **preservation** (minimal biomass thresholds)

$$A \text{ stocks: } A(t) \geq S_A^b$$

$$H \text{ stocks: } H(t) \geq S_H^b$$

- ▶ **economic/social** requirements (minimal catch thresholds)

$$A \text{ catches: } E_A(t) \mathcal{R}_A(A(t), H(t), w_A(t)) A(t) \geq C_A^b$$

$$H \text{ catches: } E_H(t) \mathcal{R}_H(A(t), H(t), w_H(t)) H(t) \geq C_H^b$$

We make a heroic assumption about the set of scenarios

- ▶ An uncertainty **scenario** is a time sequence of uncertainty couples

$$(w_A(\cdot), w_H(\cdot)) = \left((w_A(t_0), w_H(t_0)), \dots, (w_A(T-1), w_H(T-1)) \right)$$

- ▶ We assume that, at each time t ,
the uncertainties $(w_A(t), w_H(t))$ can take any value in a
two-dimensional set

$$(w_A(t), w_H(t)) \in \overline{W}(t) \subset \mathbb{R}^2$$

- ▶ Therefore, from one time t to the next $t + 1$,
uncertainties can be drastically different,
since $(w_A(t), w_H(t))$ is not related to $(w_A(t + 1), w_H(t + 1))$
- ▶ Such an independence assumption is materialized by the property
that a scenario can take any value in a product set

$$(w_A(\cdot), w_H(\cdot)) \in \prod_{t=t_0}^{T-1} \overline{W}(t)$$

In practice, we consider stationary uncertainty sets forged from empirical data

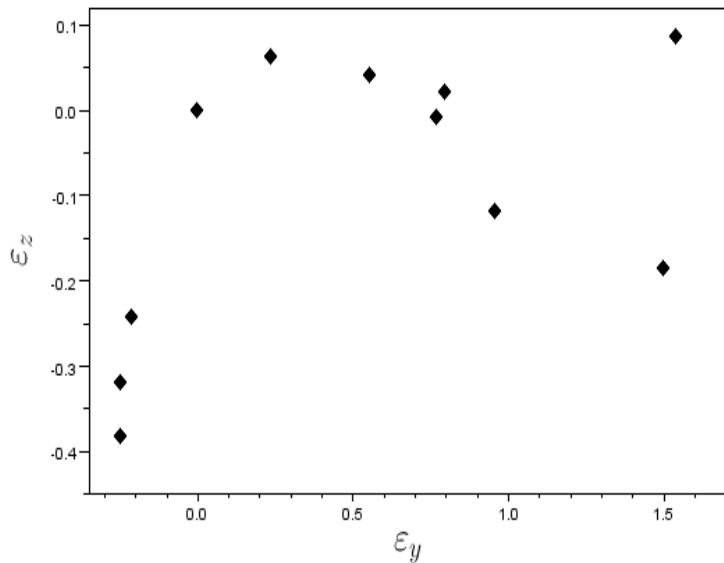
- ▶ In practice, we consider **stationary uncertainty sets**

$$\overline{\mathbb{W}}(t) = \overline{\mathbb{W}}$$

- ▶ Therefore, our heroic assumption about the set of scenarios is:
**any of the possible uncertainty of any year
can materialize any *other* year**

Empirical distribution of the uncertainties

$$(\overline{w}_A(t), \overline{w}_H(t))_{t=t_0, \dots, T-1}$$



We first consider the empirical uncertainty set

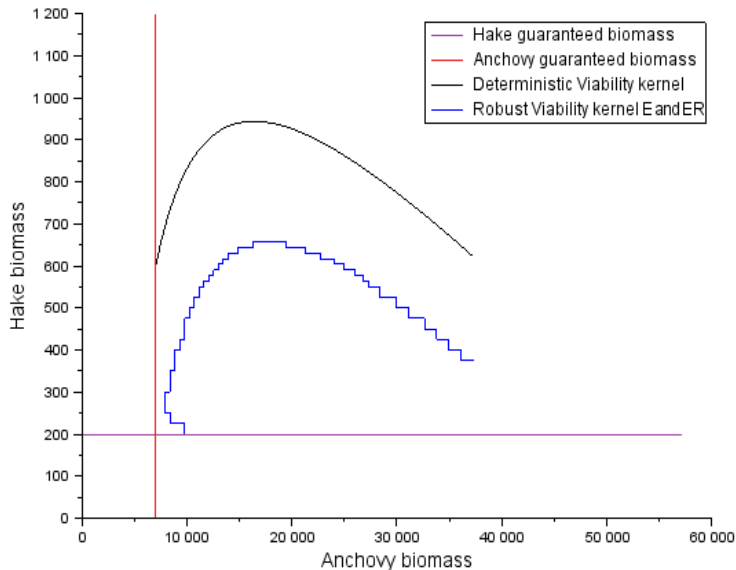
- ▶ The **empirical uncertainties set** is

$$\overline{\mathbb{W}}^E = \underbrace{\{(\overline{w}_A(t), \overline{w}_H(t)) \mid t = t_0, \dots, T-1\}}_{\text{empirical discrepancies}} \cup \underbrace{\{(0, 0)\}}_{\text{deterministic case}}$$

- ▶ Since $\{(0, 0)\} \subset \overline{\mathbb{W}}^E$,
the corresponding robust and deterministic viability kernels satisfy

$$\text{Viab}_1^E(t_0) \subset \text{Viab}(t_0)$$

The robust viability kernel is noticeably smaller than the deterministic one

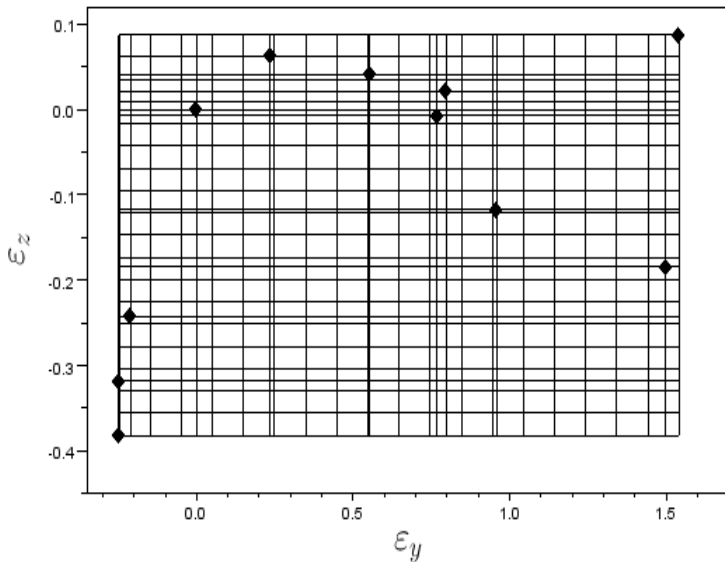


Algorithm for the robust viability kernel and the robust viable controls

```
initialization  $V(T, A, H) = \mathbf{1}_{A \geq S_A^b} \mathbf{1}_{H \geq S_H^b}$ ;  
for times  $t = T, T - 1, \dots, t_0$  do  
  forall biomasses  $(A, H)$  do  
    forall efforts  $(C_A, C_H)$  do  
      forall uncertainties  $(w_A, w_H)$  do  
         $V(t + 1, F(t, A, H, C_A, C_H, w_A, w_H))$   
       $\inf_{w_A, w_H} V(t + 1, F(t, A, H, C_A, C_H, w_A, w_H))$   
     $\max_{(C_A, C_H)} \inf_{(w_A, w_H)} V(t + 1, F(t, A, H, C_A, C_H, w_A, w_H))$   
   $V(t, A, H) = \mathbf{1}_{A \geq S_A^b} \mathbf{1}_{H \geq S_H^b} V(t + 1, F(t, A, H, C_A, C_H, w_A, w_H))$  ;  
   $\mathbb{B}_1^{\text{viab}}(t, A, H) =$   
   $\operatorname{argmax}_{(C_A, C_H)} \inf_{(w_A, w_H)} V(t + 1, F(t, A, H, C_A, C_H, w_A, w_H))$ 
```

Second, we consider a refined uncertainty set

Figure: Uncertainty sets \overline{W}^E (diamonds) and \overline{W}^{ER} (grid)



Here is the refinement of the empirical uncertainty set

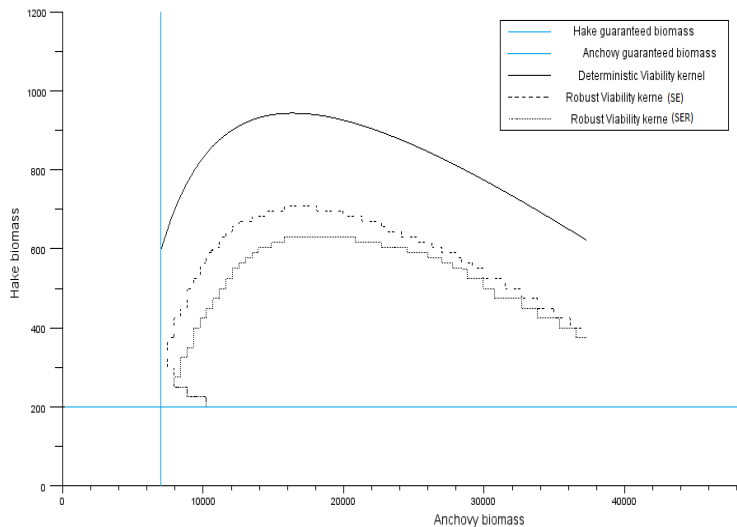
- ▶ The **empirical uncertainties set** is

$$\overline{\mathbb{W}}^E = \underbrace{\{(\overline{w}_A(t), \overline{w}_H(t)) \mid t = t_0, \dots, T-1\}}_{\text{empirical discrepancies}} \cup \underbrace{\{(0, 0)\}}_{\text{deterministic case}}$$

- ▶ The **refined empirical uncertainties set** $\overline{\mathbb{W}}^{ER}$ is made of 900 uncertainty couples delineated by a 30×30 grid over the rectangle $[\overline{w}_A^{min}, \overline{w}_A^{max}] \times [\overline{w}_H^{min}, \overline{w}_H^{max}]$, including all the uncertainty couples in $\overline{\mathbb{W}}^E$
- ▶ Since $\{(0, 0)\} \subset \overline{\mathbb{W}}^E \subset \overline{\mathbb{W}}^{ER}$, the corresponding robust and deterministic viability kernels satisfy

$$\text{Viab}_1^{ER}(t_0) \subset \text{Viab}_1^E(t_0) \subset \text{Viab}(t_0)$$

The robust viability kernels are noticeably smaller than the deterministic one



Now, we focus on worst-case uncertainties

- ▶ Numerical simulations led us to consider the three following uncertainty sets
 - ▶ low growth factor for both species /
low growth factor for prey and high growth factor for predator

$$\overline{W}^M = \{(\overline{W}_A^{\min}, \overline{W}_H^{\min}), (\overline{W}_A^{\min}, \overline{W}_H^{\max})\}$$

- ▶ half

$$\overline{W}^L = \{(\frac{\overline{W}_A^{\min}}{2}, \frac{\overline{W}_H^{\min}}{2}), (\frac{\overline{W}_A^{\min}}{2}, \frac{\overline{W}_H^{\max}}{2})\}$$

- ▶ 10% increase

$$\overline{W}^H = 1.1 \times \overline{W}^M$$

- ▶ Since $\{(0, 0)\} \subset \overline{W}^L \subset \overline{W}^M \subset \overline{W}^H$,
the corresponding robust and deterministic viability kernels satisfy

$$\text{Viab}_1^H(t_0) \subset \text{Viab}_1^M(t_0) \subset \text{Viab}_1^L(t_0) \subset \text{Viab}(t_0)$$

Figure: Uncertainty sets \overline{W}^L (crosses), \overline{W}^M (diamonds) and \overline{W}^H (triangles)

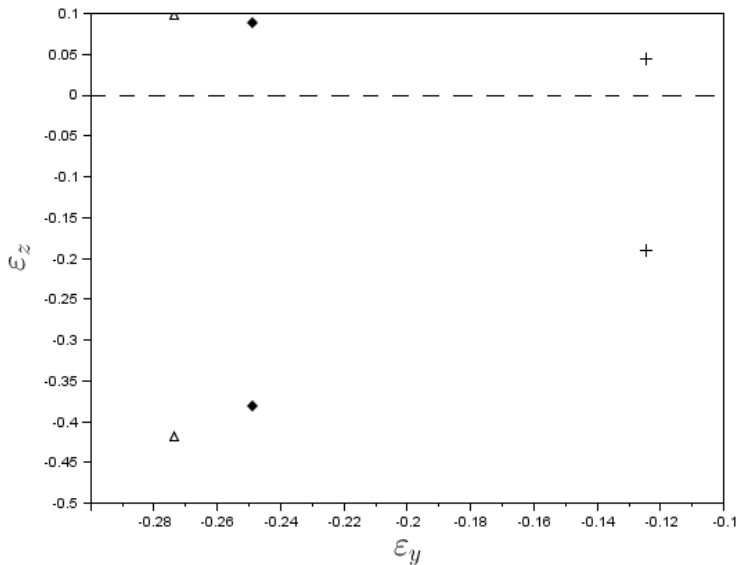
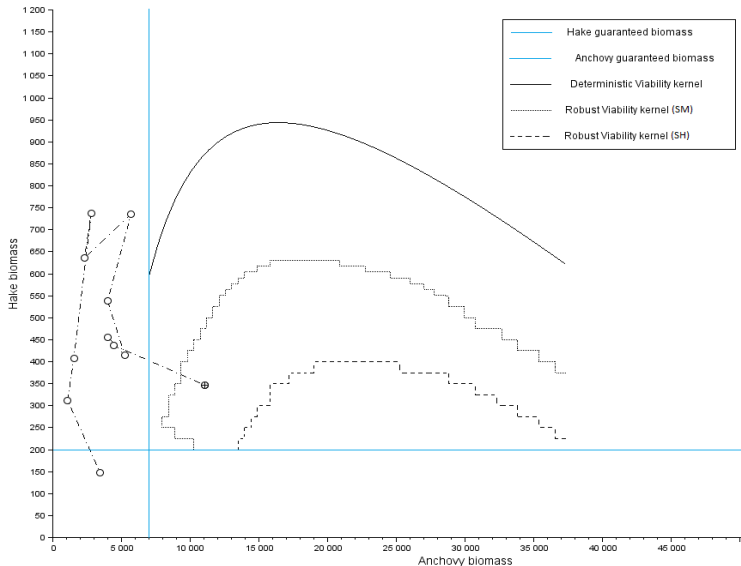


Figure: Robust viability kernels $\text{Viab}_1^L(t_0)$, $\text{Viab}_1^M(t_0)$ and $\text{Viab}_1^H(t_0)$ and the deterministic viability kernel



Summary

- ▶ We introduce uncertainties in the growth rates of interacting populations
- ▶ When populations start from a robust viable state, the fisheries can be managed so that both preservation and conservation objectives are met, *whatever the scenarios of uncertainties*
- ▶ To compute robust viable states, we make the strong assumption that, from one year t to the next $t + 1$, uncertainties can be drastically different (independence)
- ▶ With this assumption, we compute the robust viability kernel by dynamic programming, for different sets of uncertainties
- ▶ We observe that the robust viability kernels are noticeably smaller than the deterministic ones
- ▶ We also identify uncertainties and **scenarios that really matter** for a **precautionary approach**: low growth for both species
alternance of low growth of anchovy/high growth of hake

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Ecosystem viable yields (anchovy-hake application)

Risk management, robust and stochastic viability

Uncertainty variables are new input variables

Robust viability

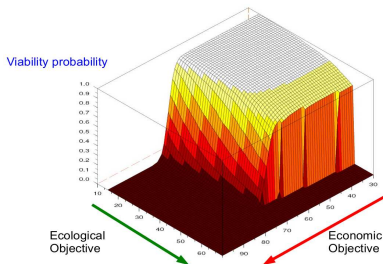
Robust viability analysis of anchovy-hake Peruvian fisheries

Stochastic viability

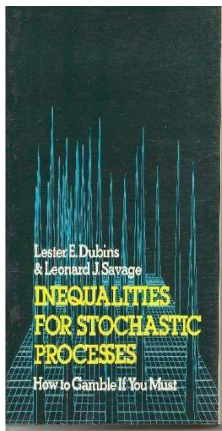
Stochastic viability analysis of bycatches in a nephrops-hake fishery

Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management



Maximizing the probability of success may be an objective



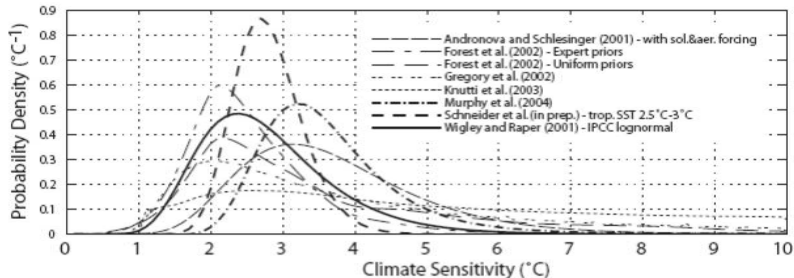
How to gamble if you must,
L.E. Dubbins and L.J.
Savage, 1965

Imagine yourself at a casino with \$1,000. For some reason, you desperately need \$10,000 by morning; anything less is worth nothing for your purpose.

The only thing possible is to gamble away your last cent, if need be, in an attempt to reach the target sum of \$10,000.

- ▶ The question is **how to play**, not whether. What ought you do? How should you play?
 - ▶ Diversify, by playing 1 \$ at a time?
 - ▶ Play boldly and concentrate, by playing 1,000 \$ only one time?
- ▶ What is your **decision criterion**?

We suppose that the set \mathbb{S} of scenarios is equipped with a probability \mathbb{P} (though this is a delicate issue!)



In practice, one often assumes that the components $(w(t_0), \dots, w(T-1))$ form an **independent and identically distributed** sequence of random variables, or form a **Markov chain**, or a **time series**

We extend viability kernels to
stochastic viability kernels

Stochastic viability kernels

In stochastic viability, state constraints are to be met along time with a given confidence level $\beta \in [0, 1]$

$$\mathbb{P}\left(w(\cdot) \in \mathbb{S} \mid x(t) \in \mathbb{A}(t) \text{ for } t = t_0, \dots, T\right) \geq \beta$$

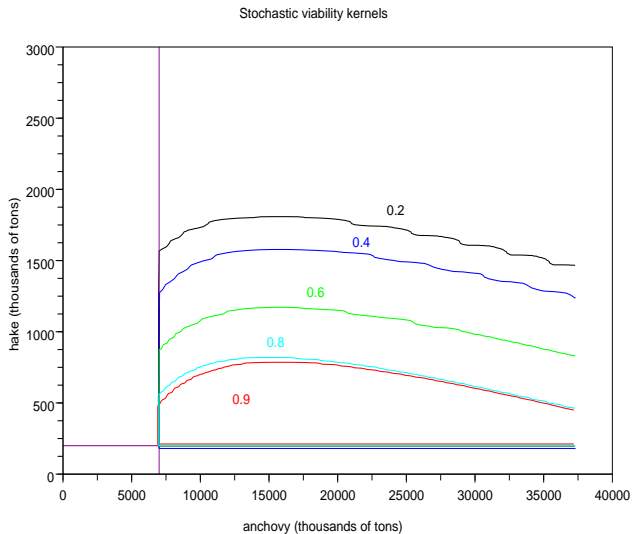
Stochastic viability kernels

The **stochastic viability kernel** at confidence level $\beta \in [0, 1]$ is

$$\text{Viab}_\beta(t_0) = \left\{ x_0 \in \mathbb{X} \mid \begin{array}{l} \text{there exists a policy } \text{Pol} \in \mathcal{U}^{ad} \text{ such that} \\ \mathbb{P}\left(w(\cdot) \in \mathbb{S} \mid x(t) \in \mathbb{A}(t) \text{ for } t = t_0, \dots, T\right) \geq \beta \end{array} \right\}$$

where the state $x(t) = X_F[t_0, x_0, \text{Pol}, w(\cdot)](t)$
is the outcome of the state solution map

Stochastic viability kernels $\mathbb{V}iab_{\beta}(t_0)$ for a hake-anchovy fisheries model



Stochastic viability kernels
can be obtained by
dynamic programming

The viability probability is the probability of satisfying constraints under a policy

Viability probability

The **viability probability** associated with the initial time t_0 , the initial state x_0 and the **policy Pol** is the probability $\mathbb{P}[\mathbb{S}_{\text{Pol}, t_0, x_0}]$ of the set $\mathbb{S}_{\text{Pol}, t_0, x_0}$ of viable scenarios

$$\mathbb{P}[\mathbb{S}_{\text{Pol}, t_0, x_0}] = \text{Proba} \left\{ w(\cdot) \in \mathbb{S} \mid \begin{array}{l} \text{the state constraints} \\ X_F[t_0, x_0, \text{Pol}, w(\cdot)](t) \in \mathbb{A}(t) \\ \text{and the control constraints} \\ U_F[t_0, x_0, \text{Pol}, w(\cdot)] \in \mathbb{B}(t, x(t)) \\ \text{are satisfied for all times } t = t_0, \dots, T \end{array} \right\}$$

The maximal viability probability is the upper bound for the probability of satisfying constraints

Maximal viability probability and optimal viable policy

The maximal viability probability is

$$\max_{\text{Po1}} \mathbb{P} [S_{\text{Po1}, t_0, x_0}]$$

An optimal viable policy Po1^* satisfies

$$\mathbb{P} [S_{\text{Po1}^*, t_0, x_0}] \geq \mathbb{P} [S_{\text{Po1}, t_0, x_0}]$$

In a sense, any optimal viable policy makes the set of viable scenarios the “largest” possible

Let us introduce the stochastic viability Bellman function

Suppose that the **primitive random variables** $(w(t_0), w(t_0 + 1), \dots, w(T - 2), w(T - 1))$ are **independent** under the probability \mathbb{P}

Bellman function / stochastic viability value function

Define the **probability-to-go** as

$$V(t, x) = \max_{\text{Pol}} \mathbb{P} \left(\overbrace{w(\cdot) \in \mathbb{S} \mid \text{Pol}(s, x(s)) \in \mathbb{B}(s, x(s))}^{\text{control constraints}} \text{ and } \overbrace{x(s) \in \mathbb{A}(s)}^{\text{state constraints}} \text{ for } s \geq t \right)$$

where $x(s + 1) = F(s, x(s), \text{Pol}(s, x(s)), w(s))$ and $x(t) = x$

- ▶ The function $V(t, x)$ is called **stochastic viability value function** or **Bellman function**
- ▶ The original problem is $V(t_0, x_0)$

The dynamic programming equation is a backward equation satisfied by the stochastic viability value function

Proposition

If the *primitive random variables*

$(w(t_0), w(t_0 + 1), \dots, w(T - 2), w(T - 1))$ are *independent* under the probability \mathbb{P} , the stochastic viability value function $V(t, x)$ satisfies the following backward induction, where t runs from $T - 1$ down to t_0

$$V(T, x) = \mathbf{1}_{\mathbb{A}(T)}(x)$$

$$V(t, x) = \mathbf{1}_{\mathbb{A}(t)}(x) \max_{u \in \mathbb{B}(t, x)} \mathbb{E}_{w(t)} \left[V(t + 1, F(t, x, u, w(t))) \right]$$

Algorithm for the Bellman functions and the stochastic viable controls

```
initialization  $V(T, x) = \mathbf{1}_{\mathbb{A}(T)}(x)$ ;  
for  $t = T, T - 1, \dots, t_0$  do  
  forall  $x \in \mathbb{X}$  do  
    forall  $u \in \mathbb{B}(t, x)$  do  
       $\mathbb{E}_{w(t)} \left[ V(t + 1, F(t, x, u, w(t))) \right]$   
     $\max_{u \in \mathbb{B}(t, x)} \mathbb{E}_{w(t)} \left[ V(t + 1, F(t, x, u, w(t))) \right]$   
   $V(t, x) = \mathbf{1}_{\mathbb{A}(t)}(x) \max_{u \in \mathbb{B}(t, x)} \mathbb{E}_{w(t)} \left[ V(t + 1, F(t, x, u, w(t))) \right]$ 
```

The stochastic viable dynamic programming equation yields stochastic viable policies

For any time t and state x , let us assume that the set

$$\mathbb{B}^{\text{viab}}(t, x) = \operatorname{argmax}_{u \in \mathbb{B}(t, x)} \left(\mathbf{1}_{A(t)}(x) \mathbb{E}_{w(t)} \left[V(t+1, F(t, x, u, w(t))) \right] \right)$$

of **viable controls** is not empty

Proposition

Then, any (measurable) policy Pol such that $\text{Pol}^*(t, x) \in \mathbb{B}^{\text{viab}}(t, x)$ is an optimal viable policy which achieves the **maximal viability probability**

$$V(t_0, x_0) = \max_{\text{Pol}} \mathbb{P}[\mathbb{S}_{\text{Pol}, t_0, x_0}]$$

The dynamic programming equation yields the viability kernels

The viability kernel at confidence level β turns out to coincide with the section of level β of the stochastic value function:

$$V(t_0, x_0) \geq \beta \iff x_0 \in \text{Viab}_\beta(t_0)$$

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The image shows two posters from the Peruvian Ministry of Production (PRODUCE) regarding fishing regulations. The left poster is titled "Tallas Mínimas de Captura de Peces" (Minimum Catch Lengths of Fish) and lists various fish species with their corresponding minimum catch lengths. The right poster is titled "Longitudes Mínimas de Malla" (Minimum Mesh Lengths) and illustrates the correct and incorrect ways to use fishing nets, emphasizing the importance of respecting minimum mesh sizes to ensure sustainable fishing.

Tallas Mínimas de Captura de Peces
establecidas por el Ministerio de la Producción

¡RECORDAR!
RESPECTAR EL TALLADO DE LA PESCA ARTESANAL TAMBIÉN DEPENDE DE TI Y TU COMUNIDAD.

Respetar las TALLAS MÍNIMAS DE CAPTURA para poder disfrutar de la pesca artesanal.

ESPECIE	TALLA MÍNIMA (cm)
Merluza	25
Merluza común	25
Merluza negra	25
Merluza blanca	25
Merluza amarilla	25
Merluza roja	25
Merluza azul	25
Merluza verde	25
Merluza morada	25
Merluza gris	25
Merluza blanca	25
Merluza amarilla	25
Merluza roja	25
Merluza azul	25
Merluza verde	25
Merluza morada	25
Merluza gris	25
Merluza blanca	25
Merluza amarilla	25
Merluza roja	25
Merluza azul	25
Merluza verde	25
Merluza morada	25
Merluza gris	25

LONGITUD
→ Marquilla ←
→ Total ←

RECORDAR SI RESPETAS LAS TALLAS MÍNIMAS ESTABLECIDAS DE MALLAS MÍNIMAS Y CUMPLES CON LAS VEDAS, TENDRÁS BUENA PESCA.

¡NO OLVIDES SACAR TU PERMISO DE PESCA, ES FÁCIL Y GRATUITO!

¡NO OLVIDES SACAR TU PERMISO DE PESCA, ES FÁCIL Y GRATUITO!

Longitudes Mínimas de Malla
establecidas por el Ministerio de la Producción

¡RECORDAR!
RESPECTAR EL TALLADO DE LA PESCA ARTESANAL TAMBIÉN DEPENDE DE TI Y TU COMUNIDAD.

Respetar las TALLAS MÍNIMAS DE MALLA para poder disfrutar de la pesca artesanal.

SI
...RESPECTAS EL TALLADO...
...BUENA PESCA...

NO
...RESPECTAS EL TALLADO...
...BUENA PESCA...

RECORDAR SI RESPETAS LAS TALLAS MÍNIMAS ESTABLECIDAS DE MALLAS MÍNIMAS Y CUMPLES CON LAS VEDAS, TENDRÁS BUENA PESCA.

¡NO OLVIDES SACAR TU PERMISO DE PESCA, ES FÁCIL Y GRATUITO!

RECORDAR SI RESPETAS LAS TALLAS MÍNIMAS ESTABLECIDAS DE MALLAS MÍNIMAS Y CUMPLES CON LAS VEDAS, TENDRÁS BUENA PESCA.

¡NO OLVIDES SACAR TU PERMISO DE PESCA, ES FÁCIL Y GRATUITO!

We set up a dynamical age-class model
of hake and nephrops in technical interaction

$$N_1^h(t+1) = w^h(t) \text{ uncertain hake recruitment}$$

$$N_1^n(t+1) = w^n(t) \text{ uncertain nephrops recruitment}$$

$$N_a^h(t+1) = N_{a-1}^h(t) \left(1 - M_{a-1}^h - \overbrace{u(t)F_{a-1}^{nh}}^{\text{hake bycatch}} - F_{a-1}^{hh} \right)$$

$$N_a^n(t+1) = N_{a-1}^n(t) \left(1 - M_{a-1}^n - \overbrace{u(t)F_{a-1}^{nn}}^{\text{nephrops fishing mortality}} \right)$$

$$N_A^h(t+1) = N_{A-1}^h(t) (1 - M_{A-1}^h - u(t)F_{A-1}^{nh} - F_{A-1}^{hh})$$

$$+ N_A^h(t) (1 - M_A^h - u(t)F_A^{nh} - F_A^{hh})$$

$$N_A^n(t+1) = N_{A-1}^n(t) (1 - M_{A-1}^n - u(t)F_{A-1}^{nn})$$

$$+ N_A^n(t) (1 - M_A^n - u(t)F_A^{nn})$$

The relative effort of the nephrops fleet has to be controlled to ensure both nephrops fleet profitability and hake preservation

- ▶ **Economic objective:** nephrops fishery is economically viable if the **gross return** is greater than a threshold

$$\underbrace{P(N^n(t), u(t))}_{\text{payoff}} \geq P^b$$

- ▶ **Ecological objective:** fishery is ecologically viable if its impact by **bycatch** on the hake biology is compatible with **sufficient recruitment of mature hakes**

$$\underbrace{N_4^h(t)}_{\text{fourth age-class}} \geq (N_4^h)^b$$

An optimal viable policy can be calculated thanks to monotonicity properties

- ▶ Due to **monotonicity properties**
 - ▶ of the dynamics, increasing in the state variable and decreasing in the control
 - ▶ of the constraints, increasing in the state variable and decreasing in the control
- ▶ we can prove that

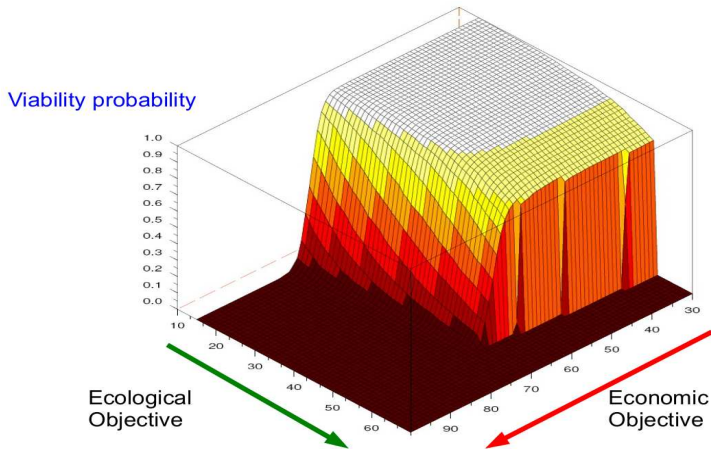
$$Pol^*(t, N) = \inf\{u \in [0, u^\#] \mid P(N^n, u) \geq P^b\}$$

is an **optimal viable policy**

Numerical evaluation of the maximal viability probability as a function of the guaranteed thresholds P^b and $(N_4^h)^b$

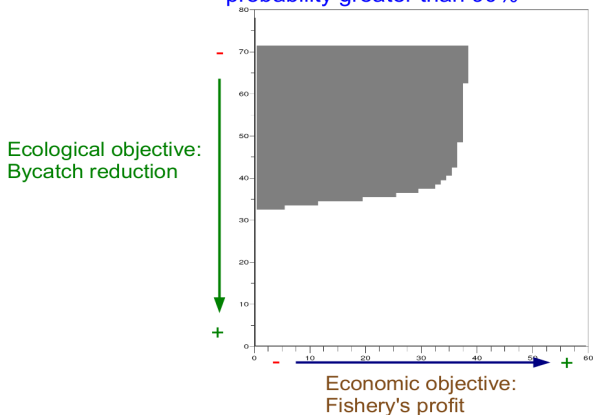
- ▶ We fix the horizon (10 years)
- ▶ We select a 18-dimensional initial state (hake and nephrops abundances at all age-classes)
- ▶ A top loop runs over the thresholds P^b and $(N_4^h)^b$
- ▶ We launch S Monte-Carlo simulations ($S = 10,000$)
- ▶ For each recruitment scenario, we simulate hake and nephrops abundances with the dynamics driven by the optimal policy (that depends on the threshold P^b)
- ▶ For each recruitment scenario, we evaluate the minimum over time of the abundance of the hake fourth age-class and check whether it exceeds $(N_4^h)^b$ or not
- ▶ We increment the viability frequency by $1/S$ or by 0 accordingly

We draw the maximal viability probability as a function of the guaranteed thresholds P^b and $(N_4^h)^b$



We draw the iso-values for the maximal viability probability as a function of guaranteed thresholds P^b and $(N_4^h)^b$

Sustainability objectives achievable with a probability greater than 90%



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- Uncertainty variables are new input variables

- Robust viability

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- Stochastic viability

- Stochastic viability analysis of bycatches in a nephrops-hake fishery

- Dam management under environmental/tourism constraint**

Contribution to quantitative sustainable management



Tourism issues impose constraints upon traditional economic management of a hydro-electric dam



- ▶ Maximizing the revenue from turbinated water
- ▶ under a tourism constraint of having enough water in July and August

We consider a single dam nonlinear dynamical model in the decision-hazard setting

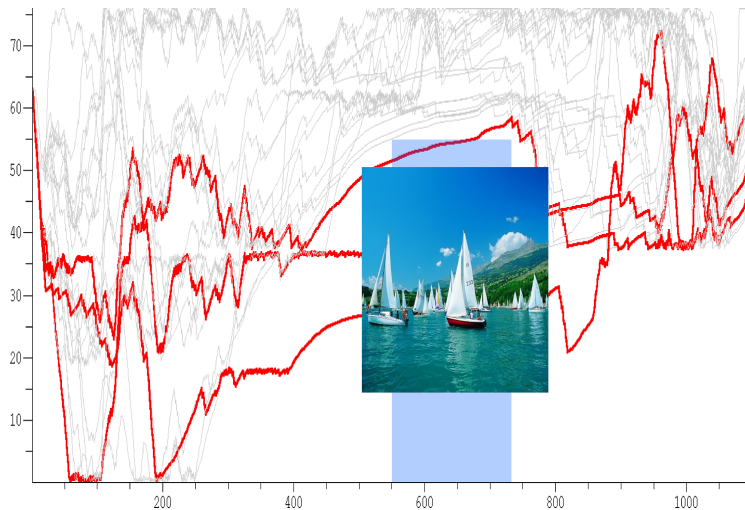
We model the dynamics of the water volume in a dam by

$$\underbrace{S(t+1)}_{\text{future volume}} = \min\{S^\#, \underbrace{S(t)}_{\text{volume}} - \underbrace{q(t)}_{\text{turbined}} + \underbrace{a(t)}_{\text{inflow volume}}\}$$

- ▶ $S(t)$ **volume** (stock) of water at the beginning of period $[t, t + 1[$
- ▶ $q(t)$ **turbined outflow volume** during $[t, t + 1[$
 - ▶ decided at the beginning of period $[t, t + 1[$
 - ▶ chosen such that $0 \leq q(t) \leq \min\{S(t), q^\#\}$
- ▶ $a(t)$ **inflow water volume** (rain, etc.) during $[t, t + 1[$, which materializes at the end $t + 1$ of period $[t, t + 1[$
- ▶ $S^\#$ **dam capacity**

The setting is called **decision-hazard** because the **decision** $q(t)$ is made **before** the **hazard** $a(t)$

The red stock trajectories fail to meet the tourism constraint in July and August



In the risk-neutral economic approach,
an optimal management maximizes the expected payoff

- ▶ Suppose that
 - ▶ **turbined water** $q(t)$ is sold at price $p(t)$,
related to the price at which energy can be sold at time t
 - ▶ a **probability** \mathbb{P} is given on the set $\mathbb{S} = \mathbb{R}^{T-t_0} \times \mathbb{R}^{T-t_0}$
of **water inflows scenarios** $(a(t_0), \dots, a(T-1))$
and **prices scenarios** $(p(t_0), \dots, p(T-1))$
 - ▶ at the horizon, **the final volume** $S(T)$ has a value $K(S(T))$,
the “final value of water”
- ▶ The traditional (risk-neutral) economic problem is to maximize the intertemporal payoff (without discounting if the horizon is short)

$$\max \mathbb{E} \left[\sum_{t=t_0}^{T-1} \left(\underbrace{p(t)}_{\text{price}} \underbrace{q(t)}_{\text{turbined}} - \underbrace{\epsilon q(t)^2}_{\text{turbined costs}} \right) + \underbrace{K(S(T))}_{\text{final volume utility}} \right]$$

We now have a stochastic optimization problem, where the tourism constraint still needs to be dressed in formal clothes

- ▶ Traditional cost minimization/payoff maximization

$$\max \mathbb{E} \left[\sum_{t=t_0}^{T-1} \overbrace{p(t)q(t) - \epsilon q(t)^2}^{\text{turbined water payoff}} + \overbrace{K(S(T))}^{\text{final volume utility}} \right]$$

- ▶ Tourism constraint

$$\text{volume } S(t) \geq S^b, \quad \forall t \in \mathcal{T} = \{ \text{July, August} \}$$

- ▶ In what sense should we consider this inequality which involves the random variables $S(t)$ for $t \in \mathcal{T}$?

Robust / almost sure / probability constraint

- ▶ **Robust** constraints: for all the scenarios in a subset $\bar{\mathcal{S}} \subset \mathcal{S}$

$$S(t) \geq S^b, \quad \forall t \in \mathcal{T}$$

- ▶ **Almost sure** constraints

$$\text{Probability} \left\{ S(t) \geq S^b, \quad \forall t \in \mathcal{T} \right\} = 1$$

- ▶ **Probability** constraints, with “confidence” level $p \in [0, 1]$

$$\text{Probability} \left\{ S(t) \geq S^b, \quad \forall t \in \mathcal{T} \right\} \geq p$$

- ▶ and also by penalization, or in the mean, etc.

Our problem may be clothed as a stochastic optimization problem under a probability constraint

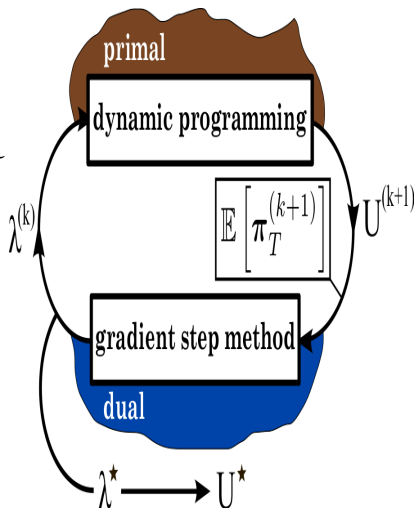
$$P(T) = \sum_{t=t_0}^{T-1} \overbrace{p(t)q(t) - \epsilon q(t)^2}^{\text{turbined water payoff}} + \overbrace{K(S(T))}^{\text{final volume utility}}$$

- ▶ The traditional economic problem is $\max \mathbb{E}[P(T)]$
- ▶ and a failure tolerance is accepted

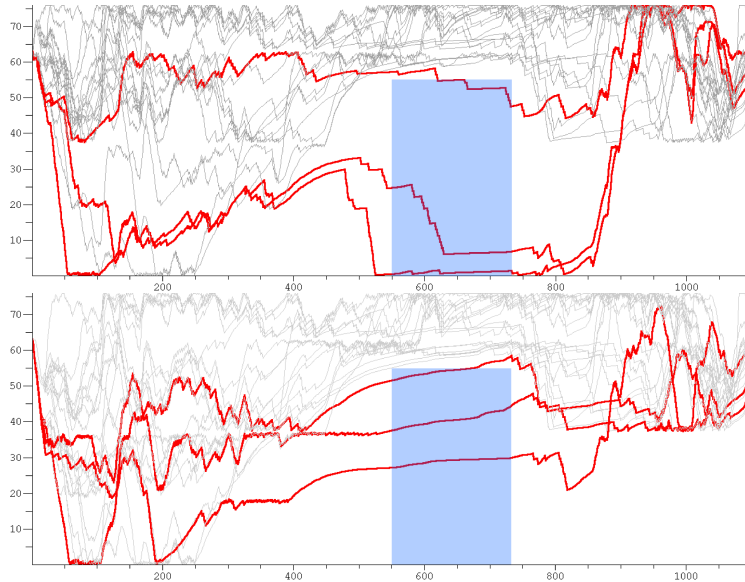
$$\text{Probability} \left\{ S(t) \geq S^b, \forall t \in \mathcal{T} \right\} \geq 90\%$$

Details concerning the theoretical and numerical resolution are available on demand

- ▶ $\pi(0) = 1$ and $\pi(t+1) = \begin{cases} \mathbf{1}_{\{S(t+1) \geq S^b\}} \times \pi(t) & \text{if } t \in \mathcal{T} \\ \pi(t) & \text{else} \end{cases}$
- ▶ $\mathbb{P}[S(\tau) \geq S^b, \forall \tau \in \mathcal{T}]$
 $= \mathbb{E}[\mathbf{1}_{\{S(\tau) \geq S^b, \forall \tau \in \mathcal{T}\}}]$
 $= \mathbb{E}[\prod_{\tau \in \mathcal{T}} \mathbf{1}_{\{S(\tau) \geq S^b\}}]$
 $= \mathbb{E}[\pi(T)]$



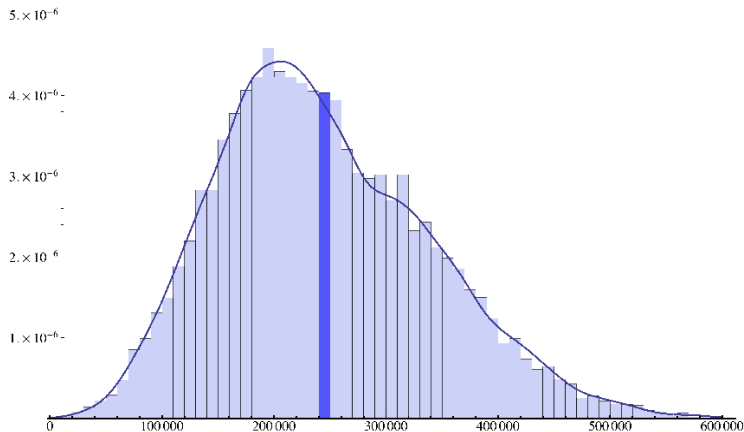
90% of the stock trajectories meet the tourism constraint



Our resolution approach brings a sensible improvement compared to standard procedures

OPTIMAL POLICIES	OPTIMIZATION		SIMULATION		
	Iterations	Time	Gain	Respect	Well behaviour
Standard	15	10 mn	ref	0,9	no
Convenient	10	160 mn	-3.20%	0,9	yes
Heuristic	10	160 mn	-3.25%	0,9	yes

However, though the expected payoff is optimal, the payoff effectively realized can be far from it



We propose a stochastic viability formulation to treat symmetrically and to guarantee both environmental and economic objectives

- ▶ Given two thresholds to be guaranteed
 - ▶ a volume S^b (measured in cubic hectometers hm^3)
 - ▶ a payoff P^b (measured in numeraire \$)
- ▶ we look after policies achieving the **maximal viability probability**

$$\Pi(S^b, P^b) = \max \text{Proba} \left\{ \begin{array}{l} \text{water inflow scenarios along which} \\ \text{the volumes } S(t) \geq S^b \\ \text{for all time } t \in \{ \text{July, August} \} \\ \text{and the final payoff } P(T) \geq P^b \end{array} \right\}$$

- ▶ $\Pi(S^b, P^b)$ is the **maximal probability** to guarantee to be above the thresholds S^b and P^b

The stochastic viability formulation requires to redefine state and dynamics

- ▶ The state is the couple $x(t) = (S(t), P(t))$ volume/payoff
- ▶ The control $u(t) = q(t)$ is the turbined water
- ▶ The dynamics is

$$\underbrace{S(t+1)}_{\text{future volume}} = \min\{S^\sharp, \underbrace{S(t)}_{\text{volume}} - \underbrace{q(t)}_{\text{turbined}} + \underbrace{a(t)}_{\text{inflow volume}}\},$$
$$t = t_0, \dots, T-1$$

$$\underbrace{P(t+1)}_{\text{future payoff}} = \underbrace{P(t)}_{\text{payoff}} + \underbrace{p(t)q(t) - \epsilon q(t)^2}_{\text{turbined water payoff}}, \quad t = t_0, \dots, T-2$$

$$P(T) = P(T-1) + \underbrace{K(S(T))}_{\text{final volume utility}}$$

In the stochastic viability formulation,
we dress objectives as state constraints

- ▶ The control constraints are

$$u(t) \in \mathbb{B}(t, x(t)) \iff 0 \leq q(t) \leq \min\{S(t), q^\#\}$$

- ▶ The state constraints are

$$x(t) \in \mathbb{A}(t) \iff \begin{cases} S(t) \geq S^b \\ P(T) \geq P^b \end{cases}, \quad \forall t \in \{\text{July, August}\}$$

For each couple of thresholds on payoff and stock, we write a dynamic programming equation

► Abstract version

$$\begin{aligned} V(T, x) &= \mathbf{1}_{\mathbb{A}(T)}(x) \\ V(t, x) &= \mathbf{1}_{\mathbb{A}(t)}(x) \max_{u \in \mathbb{B}(t, x)} \mathbb{E}_{w(t)} \left[V \left(t + 1, F(t, x, u, w(t)) \right) \right] \end{aligned}$$

► Specific version

$$V(T, S, P) = \mathbf{1}_{\{P \geq p^b\}}$$

$$V(T-1, S, P) = \max_{0 \leq q \leq \min\{S, q^\#\}} \mathbb{E}_{a(T-1), p(T-1)} \left[V \left(t + 1, S - q + a(t), P + K(S) \right) \right]$$

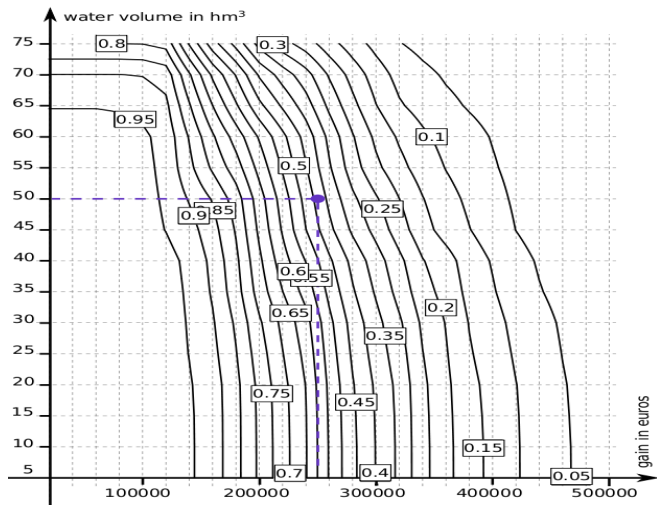
$$V(t, S, P) = \max_{0 \leq q \leq \min\{S, q^\#\}} \mathbb{E}_{a(t), p(t)} \left[V \left(t + 1, S - q + a(t), P + p(t)q - \epsilon q^2 \right) \right],$$

$t \notin \{ \text{July, August} \}$

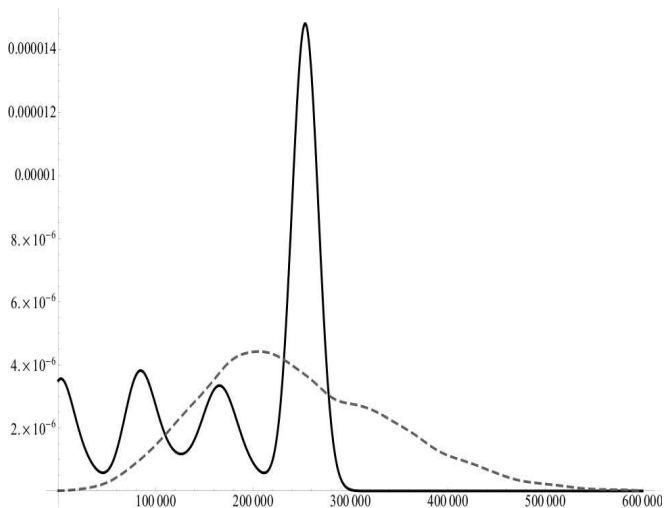
$$V(t, S, P) = \mathbf{1}_{\{S \geq s^b\}} \max_{0 \leq q \leq \min\{S, q^\#\}} \mathbb{E}_{a(t), p(t)} \left[V \left(t + 1, S - q + a(t), P + p(t)q - \epsilon q^2 \right) \right]$$

$t \in \{ \text{July, August} \}$

We plot iso-values for the maximal viability probability as a function of guaranteed thresholds S^b and P^b



The probability distribution of the random gain reflects the viability objectives



Outline of the presentation

Natural resources management issues and viability

- Examples of decision models

- Discrete-time viability

- Are the ICES fishing quotas recommendations “sustainable”?

- Ecosystem viable yields (anchovy-hake application)

Risk management, robust and stochastic viability

- Uncertainty variables are new input variables

- Robust viability

- Robust viability analysis of anchovy-hake Peruvian fisheries

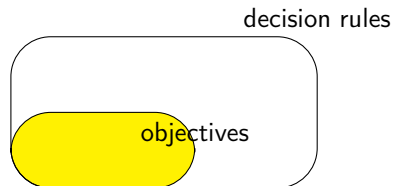
- Stochastic viability

- Stochastic viability analysis of bycatches in a nephrops-hake fishery

- Dam management under environmental/tourism constraint

Contribution to quantitative sustainable management

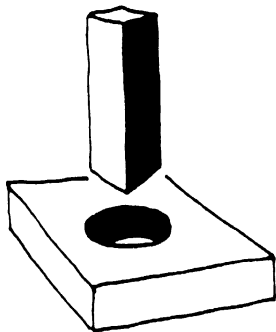
In the resource managers literature, the distinction between objectives and decision rules is often blurred



In practice, we observe that resource managers generally

- ▶ design decision rules
- ▶ which directly incorporate objectives
- ▶ with confusion between objectives and decision rules

Mismatch can be avoided by highlighting the distinction between objectives and decision rules



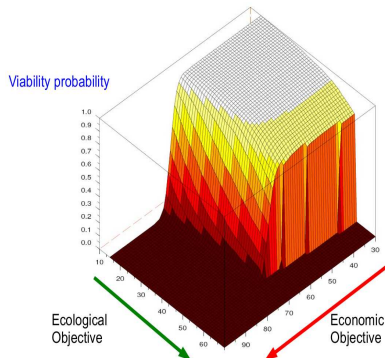
- ▶ **Control theory** makes a **clear distinction** between **objectives** and **decision rules**

objectives \Rightarrow **adapted decision rules**

- ▶ More specifically, **viability theory** puts emphasis on **consistency between dynamics and objectives**

objectives + dynamics \Rightarrow **decision rules**

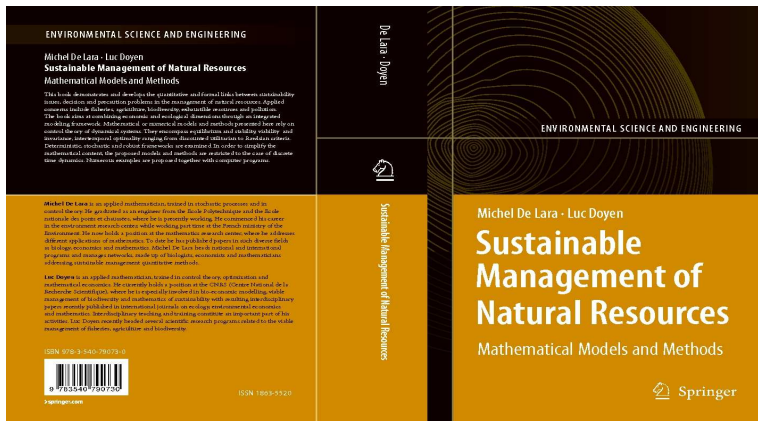
At the end of the day, where do we stand?



- ▶ **Conceptual framework** for **quantitative** sustainable management
- ▶ Managing ecological and economic **conflicting objectives**
- ▶ **Ecosystem viable yields** as a contribution to the “ecosystem approach”
- ▶ Displaying **tradeoffs** between **ecology and economy** sustainability thresholds and **risk**

“Nul n'est mieux servi que par soi-même”
“Self-promotion, nobody will do it for you” ;-)

M. De Lara, L. Doyen, **Sustainable Management of Natural Resources. Mathematical Models and Methods**, Springer, 2008.



THANK YOU!

