Multilevel Markov Chain Monte Carlo Methods with Applications in Subsurface Flow

Robert Scheichl*

* Department of Mathematical Sciences, University of Bath (R.Scheichl@maths.bath.ac.uk, http://www.maths.bath.ac.uk/ masrs/)

ABSTRACT

We address the prohibitively large cost of Markov chain Monte Carlo for large-scale PDE applications with high dimensional parameter spaces. We propose a new multilevel Metropolis-Hastings algorithm, and give an abstract theorem on its cost. For a typical model problem in subsurface flow, we then provide a detailed analysis of the assumptions in the theorem and show gains of at least one order in the ε -cost over standard Metropolis-Hastings both theoretically and numerically.