

# Design of Sustainable Quotas for an Hake–Anchovy Peruvian Ecosystem Model

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Ricardo OLIVEROS–RAMOS <sup>3</sup> and Jorge TAM <sup>3</sup>

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# Anchoveta/Anchovy and Merluza/Hake

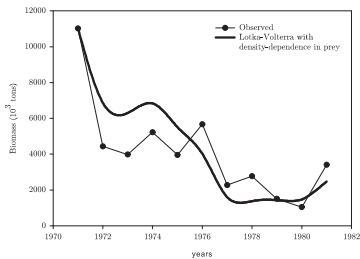


# 11 years of data from 1971 to 1981

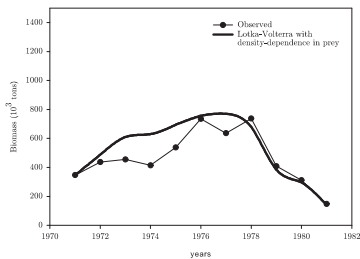
In thousands of tonnes ( $10^3$  tons)

- anchoveta\_stocks=  
[4058 3116 3461 2649 4517 1232 3727 1812 1826 8793 3418]
- merluza\_stocks=  
[347 437 455 414 538 735 636 738 408 312 148]
- anchoveta\_captures=  
[5797 1600 2540 3191 2299 1323 353 1154 177 202 1209]
- merluza\_captures=  
[27 13 133 109 85 93 107 303 93 159 69]

# Hake–anchovy Peruvian fisheries between 1971 and 1981



(c) Anchovy



(d) Hake

**Figure:** Comparison of observed and simulated biomasses of anchovy and hake using a Lotka–Volterra model with density-dependence in the prey. Model parameters are  $R = 2.24$ ,  $L = 0.98$ ,  $\kappa = 64\,672 \times 10^3 \text{ t}$  ( $K = 35\,800 \times 10^3 \text{ t}$ ),  $\alpha = 1.230 \times 10^{-6} \text{ t}^{-1}$ ,  $\beta = 4.326 \times 10^{-8} \text{ t}^{-1}$ .

# Conservation and catch thresholds

The following **annual objectives**

|                 | Anchovy (prey, $y$ ) | Hake (predator, $z$ ) |
|-----------------|----------------------|-----------------------|
| minimal biomass | 7 000 kt             | 200 kt                |
| minimal catch   | 2 000 kt             | 5 kt                  |

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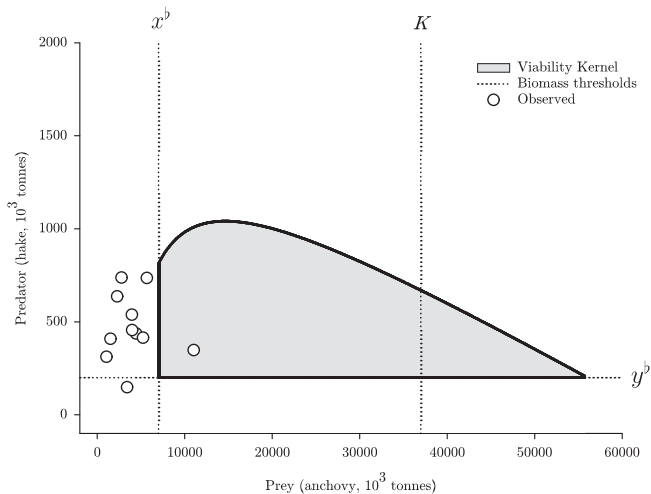
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# Lotka–Volterra model with density–dependence

$$\begin{cases} y(t+1) = y(t) \underbrace{\left( R - \frac{R}{k}y(t) - \alpha z(t) - v(t) \right)}_{R_y}, \\ z(t+1) = z(t) \underbrace{\left( L + \beta y(t) - w(t) \right)}_{R_z}, \end{cases}$$

- state vector  $(y, z)$  represents **biomasses**,
  - $y$  prey biomass: **anchovy**
  - $z$  predator biomass: **hake**
- control vector  $(v, w)$  is **fishing effort** of each species,
- **catches** are  $vy$  and  $wz$  (measured in biomass),
- $R_y$  and  $R_z$  are **annual growth factors**.

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The **viability kernel** is the set of **initial states**  $(y(t_0), z(t_0))$  from which **can emerge a trajectory**  $(y(t), z(t))$ ,  $t = t_0, t_0 + 1, \dots$  driven by **appropriate controls**  $(v(t), w(t))$ ,  $t = t_0, t_0 + 1, \dots$  such that the following goals are satisfied

- **preservation** (minimal biomass thresholds)

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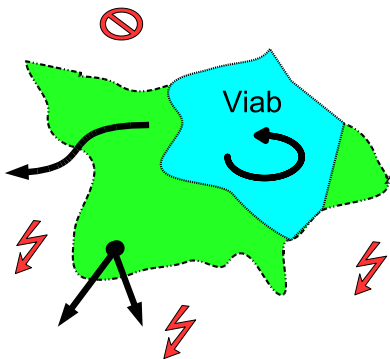
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**Figure:** The state constraint set is the large set. It includes the smaller viability kernel.

# Explicit expression for the viability kernel

## Proposition

- If the *growth factors* are *decreasing in the fishing effort*
- and if the *thresholds*  $S_y^b, S_z^b, C_y^b, C_z^b$  are such that the following *growth factors are greater than one*

$$R_y(S_y^b, S_z^b, \frac{C_y^b}{S_y^b}) \geq 1 \text{ and } R_z(S_y^b, S_z^b, \frac{C_z^b}{S_z^b}) \geq 1,$$

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# Adjusting catches to prominent conservation thresholds

- 1 Considering that first are given **minimal biomass conservation thresholds**  $S_y^b \geq 0$ ,  $S_z^b \geq 0$
- 2 and defining

$$\begin{cases} C_y^{b,*} & := S_y^b \max\{v \geq 0 \mid R_y(S_y^b, S_z^b, v) \geq 1\} \\ C_z^{b,*} & := S_z^b \max\{w \geq 0 \mid R_z(S_y^b, S_z^b, w) \geq 1\} \end{cases}$$

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$$C_y^b = \min \left\{ C_y^{b,*}, y(R - Ry/\kappa - \alpha z) - S_y^b \right\} \quad \text{and} \quad C_z^b = C_z^{b,*} .$$

- 4 These **sustainable quotas**  $C_y^b$  and  $C_z^b$  are not defined species by species, but depend on the whole ecosystem dynamics and on all conservation thresholds  $S_y^b \geq 0$ ,  $S_z^b \geq 0$ .

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# Hake–anchovy Peruvian fishery: Peru official quotas and sustainable quotas given by the viability approach

|         | Sustainable quotas (kt) |         | Peru official quotas (kt) |       |
|---------|-------------------------|---------|---------------------------|-------|
|         | Model 1                 | Model 2 | 2006                      | 2007  |
| Anchovy | 5 152                   | 5 399   | 4 250                     | 5 300 |
| Hake    | 49                      | 56,8    | 55                        | 35    |

# Hake–anchovy Peruvian fishery: Peru official quotas and sustainable quotas given by the viability approach

|         | Sustainable quotas (kt) |         | Peru official quotas (kt) |       |
|---------|-------------------------|---------|---------------------------|-------|
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