A mathematical approach to viable management of fisheries and biodiversity through protected areas: the Abore reef reserve case

> M. De Lara: ENPC, Cermics L. Doyen: CNRS - MNHN J. Ferraris: IRD, UR CoReUs D. Pelletier: IFREMER, EMH

A mathematical approach toviable management offisheries and biodiversitythrough protected areas: the Abore reef reserve case – p. 1

To begin with...

A quite honest talk

on

the multiple difficulties of a multidisciplinary work with multiple contributors, multiple species, multiple objectives!

or

a MISSION IMPOSSIBLE from

A mathematical approach toviable management offisheries and biodiversitythrough protected areas: the Abore reef reserve case - p. 2

to...

```
cor_max=0.8;
// maximum covering = 80 %
cor_min=0.05;
// minimal covering = 5 %
```

// R_c tested from 1.001 to 1.01 by dichotomy
R_c=1.002;
K_c = cor_max * R_c / (R_c -1);

```
function Xp=logistic(t,X)
Xp= X .* (R_c * (1 - X/K_c) );
// on force les Densités à être positives
endfunction
```

```
time=0:(9*365);
```

Scientific context

Appel à propositions de recherche biodiversité et changement global Institut français de la biodiversité Ministère de l'Ecologie et du Développement durable

Accepted project (2004): Modèles pour une gestion durable de la biodiversité sous incertitude et dynamique globales

Problem statement

- Protected area: a relevant tool for sustainable management of renewable resource?
- What is a **protected area** (**PA**) effect?
 - on *stocks*?
 - on *catches*?
- Which **sustainable management** through PA?
 - Size
 - Placement

Modelling requirements

• The context:

- *Population dynamics*: nonlinearity, complexity, age-structured, spatial
- *Decision* : size and location of the PA
- Uncertainties: catches, stocks, processes, etc.
- The issues:
 - Multi-criteria
 - *Ecology:* conservation
 - *Economy:* fishing income
 - *Intergenerational equity*: both short and long term horizon

PLAN

- 1. The Abore reef reserve, New Caledonia
- 2. A dynamic state model
- 3. The difficulties of parameter estimation from data
- 4. Measuring the reserve effect by stochastic viability
- 5. Simulations (skipped because not yet discussed with biologists)
- 6. Discussion

Some facts and figures

Assessment of the Impact of Removing Marine Reserve Status on Demersal and Benthic Fish Communities : a Comprehensive Approach

J. Ferraris (1), D. Pelletier (2), M. Kulbicki (1),
C. Chauvet (3)
(1) Unité de Recherche CoRéUs, IRD, Nouméa, Nouvelle-Calédonie
(2) Laboratoire MAERHA, IFREMER, Nantes, France
(3) Laboratoire LERVEM, Université, Nouméa,

Nouvelle-Calédonie

The Noumea lagoon, New Caledonia

The Noumea lagoon, located in South-Western New Caledonia, South Pacific (Figure 1) is a large coral reef ecosystem where several marine reserves were established in the 1980's in view of protecting the coral reef ecosystem from damage due to fishing and other human activities.

The Abore reef reserve

The Abore Reef reserve is located on a 25 km long barrier reef representing an area of ca. 15 000 ha.

Fishing was banned from the whole reef from 1990 to 1993, and allowed again on 2/3 of the reef from August 1993 for a fishing experiment in the perspective of adaptive management.

This opening was monitored by the Natural Resource Department of the South Province and by LERVEM (New Caledonia University)

Expected reserve effects

The main effects expected from the establishment of reserves are

- *increased abundances and biomasses* of spawning stocks and recruitment inside the protected area and in surrounding areas through spillover
- *rebuilding of ecosystems* through *protection of habitat* from fishing gears

A strong fishing pressure

In the Pacific islands, the reef and lagoon subsistence fisheries represent about 80 % of total coastal catch. Right after the reserve opening in August 1993:

- the number of boats and fish yield during the 2 weeks after the opening reached the levels previously observed for a whole year;
- monitoring of fishing effort and catch rates showed that, in the open area, *benefits from the* 1990-1993 closure were dissipated within a few weeks.

Fishing experiment

The whole reef was finally closed to fishing from August 1995.

In 1995, 2/3 of the reef had been closed for 3 years (1990-1993) and fished for 2 years (1993-1995), while the remaining had been permanently closed during the 5 years (1990-1995).

The area open to fishing from August 1993 is the impact area (area B in Figure 2), while the reference area has been permanently closed (area A in Figure 2).

Survey / Before After Control Impact design

A survey was conducted in July 1993 and July 1995, respectively right before the opening and before the final closure.

A scientific evaluation of how reserve is likely to affect fish community, e.g. increased densities, larger fish, modified interspecific relationships.

A glimpse at complexity and uncertainty

The experimental design rests on a stratification of the reef into three morphological zones : reef flat, inner slope and lagoon (Figure 2), delineated on aerial photographs.

The structure and functioning of communities are often poorly known, in particular because coral reef ecosystems exhibit a very high diversity of fish species, generally linked with live coral cover.

For demersal and benthic species, spatial distributions of populations mostly depend on habitat preferences.

A glimpse at biodiversity: species richness

A total of **374 species** were identified during the survey. As a consequence of the high diversity of the reef community, the number of species observed at a given transect often exceeded 100, most species being encountered only at a few stations.

The criteria used for partitioning the fish community into species groups were *mobility, taxonomy and feeding habits.*

Four groups of species defined for mobility

• *territorial species* living in a very restricted range (usually less than 10 m²);

- *sedentary species* with a restricted range between ten and a few hundred square meters;
- *weakly mobile species* not restricted to a specific range(up to several thousands m²);

• *highly mobile species* usually foraging over very large areas; they are not restricted to a given reef over a short period of time.

These categories form a continuum, and some species were difficult to assign to a given category.

Taxonomy: 9 over 41 families

Species belonging to 41 families were recorded during the surveys. Species in a given family were likely to be more similar in terms of trophic, morphologic and demographic features than species belonging to different families.

Only 9 families were retained for the analysis : Acanthuridae, Chaetodontidae, Labridae, Lethrinidae, Lutjanidae, Pomacentridae, Scaridae, Serranidae, Siganidae and others. These were selected either because they were important to fisheries, or because they were encountered at a large number of stations, and with non negligible abundances.

Feeding habits / diet

Species at a high trophic level were generally those targeted by fishermen, and were thus likely to be sensitive to the reserve status.

Feeding habits were expressed in percentage of food types in diet. Food types were categorized as *nekton*, *macroinvertebrates*, *macroalgae*, *microinvertebrates*, *microalgae*, *zooplankton*, *other plankton*, *coral and detritus*.

The analysis of species diets yielded 7 clusters, each cluster forming a *trophic group* (Table 2). Note that in each group, the mean diet included several food items. Groups were named on the basis of their mean diet composition.

Densities

Total fish density per transect ranged between 0.95 and 114 individuals/m², with a mean of 7.6 ind/m².

The largest densities observed occurred at one or two stations with large concentrations of Clupeidae. When this family was excluded from computations, total density per transect over the two years dropped to 2.9 ind/m^2 , with a mean of 4.0 ind/m^2 in1993 and 1.7 ind/m^2 in 1995.

A brief summary

• Area: 15 000 ha

• **Biodiversity:** some 374 species ; 41 families ;

7 trophic groups ; few functional groups but a lot of species within each group

• Catch pressure: very strong ; the biomass surplus accumulated in 3 years (from 1990 to 1993) has been fished in...15 days

A climatic impact on coral: the coral is a refuge for (small) fishes ; affected by cyclones destructions
Issues:

- Is there a *reserve effect*?
- How does *climate change* modify the previous assertions?

A DYNAMIC STATE MODEL

A mathematical approach toviable management offisheries and biodiversitythrough protected areas: the Abore reef reserve case – p. 22

Highly delicate modelling options

- Restriction to ... 4 *trophic groups* + habitat
- One "typical" species is selected within each group

These basic options lead to very difficult discussions between marine biologists and mathematicians

State: densities

- Coral/Habitat $x_0(t)$: percentage of covering;
- **Piscivors** $x_1(t)$: predators of fishes, target of fishermen (length 77 cm on average);
- Macrocarnivores x₂(t): predators of macroinvertebrates and of a few fishes (length 38 cm on average);
- Herbivors x₃(t): some are targets of fishermen (length from 24 to 39 cm);
- Other fishes (small) $x_4(t)$: sedentary and territorial organisms, microcarnivores (17 cm), coralivores (16 cm), zooplanctonophages (13 cm);

"Typical" species: a highly delicate choice...

- big grouper
- small grouper
- parrot fish
- damsel fish

A logistic habitat covering growth model

$$x_0(t+1) = x_0(t) \left(R_0 \left(1 - \frac{x_0(t)}{K_0} \right) \right)$$

The time unit $\Delta t = 1$ is to be fixed later. • R_0 is the intrinsic growth rate (for low covering). • K_0 is related to the so called *carrying capacity* x_0^{\sharp} solution of

$$1 = R_0 \left(1 - \frac{x_0^\sharp}{K_0} \right)$$

Cyclonic events occur randomly with probability p at every time step and bring the coral covering to 30 % of its last value.

A mathematical approach toviable management offisheries and biodiversitythrough protected areas: the Abore reef reserve case – p. 26

A Lotka-Volterra model

$$x_4(t+1) = x_4(t) \left(R_4 - \alpha_4^1(x_0(t))x_1(t) - \alpha_4^2(x_0(t))x_2(t) - \dots + \alpha_4^4(x_0(t))(E_4^4 - 1)x_4(t) + \alpha_4^4(x_0(t))(E_4^4 -$$

The time unit $\Delta t = 1$ is to be fixed later.

Details for trophic group 2

•

$$\frac{x_2(t+1)}{x_2(t)} = R_2$$

 $- \alpha_2^1(x_0(t))x_1(t)$

- $\alpha_2^2(x_0(t))x_2(t)$
- + $E_2^2 \alpha_2^2(x_0(t)) x_2(t)$

intrinsic growth rate
predator 1's catches rate
predator 2's catches rate
conversion of predator 2'
catches rate of prey 2

+ $E_4^2 \alpha_4^2(x_0(t)) x_4(t)$ conversion of predator 2^o catches rate of prey 4

- Intrinsic growth rate R_k includes mortality and recruitment of trophic group k due to external trophic groups.
- $\alpha_j^i(x_0)x_i$ is the proportion of prey *j* captured by x_i predators *i* in one time unit. It depends on coral covering through a refuge mechanism:

$$\alpha_j^i(x_0) = \gamma(x_0)\widehat{\alpha}_j^i = e^{(\beta - \lambda x_0)}\widehat{\alpha}_j^i$$

- E_j^i stands for the conversion factor of one unit of prey *j* density into growth of predator *i*.
- The matrices α and E are upper triangular.

To summarize the dynamics of the trophic groups, except the coral, we write in a matrix form

 $x_k(t+1) = x_k(t)(R_k + \widetilde{S}(x_0(t))x(t))_k, \quad k = 1, ..., N,$ with



A mathematical approach toviable management of fisheries and biodiversity through protected areas: the Abore reef reserve case – p. 30

THE DIFFICULTIES OF PARAMETER ESTIMATION FROM DATA

A mathematical approach toviable management offisheries and biodiversitythrough protected areas: the Abore reef reserve case - p. 31

The coral data

$$x_0(t+1) = \begin{cases} x_0(t) \left(R_0 \left(1 - \frac{x_0(t)}{K_0} \right) \right) & \text{prob. } (1-p) \\ 0.3 \times x_0(t) & \text{prob. } p \end{cases}$$

We identify the maximal value of 80 % with the carrying capacity $x_0^{\sharp} \stackrel{\text{def}}{=} \frac{R_0 - 1}{R_0} K_0 = 0.8$. After a cyclonic event, the coral grows by 10 % a year but not linearly: it takes 8 to 10 years to reach the initial covering. Probability occurence *p* corresponds to 1 cyclone every 5 to 6 years.

The case of coral Simulations give $R_0 = 1.002$ for $\Delta t = 1$ day.



Characteristic figures of the organisms

The *diet composition* $\operatorname{Stom}_{j}^{i}$ is the proportion of prey *j* in the stomach of predator *i*:

 $\mathrm{Stom}_{j}^{i} = \frac{biomass \ of \ prey \ j}{total \ biomass \ of \ preys \ in \ stomach \ of i}$

The matrix Stom is upper triangular.

Theoretically, all lines sum up to 1 in the matrix Stom $(\sum_{preys j} \text{Stom}_{j}^{i} = 1)$ but, as the predators do not only eat organisms mentioned in this model, the sums of lines may be less than 1.

Characteristic figures of the organisms

The stomachal capacity B_k is the maximum biomass that the stomach of the organism k can contain: we suppose that it represents 30 % of the organism mass.

The *average mass* W_k of the organism k is supposed to be given by

 $W = (0.5 \quad 0.5 \quad 0.7 \quad 0.1) \quad \text{kg}$

with typical species big grouper small grouper parrot fish damsel fish

Field data: abundances, densities

In 1995, *outside the Abore reserve, hence under fishing pressure*, the mean data were (except for coral)

 $(x_1 \ x_2 \ x_3 \ x_4) = (0.04 \ 0.48 \ 1.17 \ 0.49) \text{ ind/m}^2$

In the sequel, we shall assume that this vector represents densities at equilibrium, denoted by $(x_1^{\star} \ x_2^{\star} \ x_3^{\star} \ x_4^{\star}).$

Problem of coherency because data should not be under fishing pressure. This is a consequence of frequent changes in modelling options.
Diet composition estimation

The diet composition is evaluated to be Stom =!0.010.170.410.17!!0.0.020.050.02!!0.0.0.0.!!0.0.0.0.!

The lines should sum up to 1, but the predators eat other organisms like invertebrates, zooplankton, algae, etc. Line 2: macrocarnivores eat mostly invertebrates Lines 3: herbivors eat mostly algae Lines 4: other fishes (small) eat mostly zooplankton or coral Piscivors and macrocarnivors eat fish...*but the group is unknown*, so that the above matrix is the fruit of different assumptions:

- piscivors' diet is composed of 77 % fish, of all species, especially small ones, with canibalism
- macrocarnivors' diet is composed of 10 % fish, the rest being mostly invertebrates
- the proportions of diet composition by group is supposed to be the ambient proportions (perfect mixing and "opportunistic" behaviour assumptions)

A "stomachal cycle"

Suppose that the densities x_j^* are at equilibrium. During a "stomachal cycle", we have

- 1. Stom^{*i*}_{*j*}: proportion of biomass of prey *j* in the stomach of predator *i*.
- 2. $\operatorname{Stom}_{j}^{i} \times B_{i}$: biomass of prey j in the stomach of predator i. (should be a volume times a volumic mass)
- 3. $\operatorname{Stom}_{j}^{i} \times B_{i} \times x_{i}^{\star}$: biomass of preys j in x_{i}^{\star} stomachs of predator i.

Identification of α^i_j

During a time unit, we have

- 1. $\alpha_j^i x_j^{\star} x_i^{\star}$: number of preys *j* caught by x_i^{\star} predators *i*;
- 2. $\alpha_j^i x_j^{\star} x_i^{\star} \times W_j$: biomass of preys j in x_i^{\star} stomachs of predator i.

If the time unit coincides with one "stomachal cycle":

$$\operatorname{Stom}_{j}^{i}B_{i}x_{i}^{\star} = \alpha_{j}^{i}x_{j}^{\star}x_{i}^{\star}W_{j} \iff \alpha_{j}^{i} = \frac{1}{x_{j}^{\star}}\frac{\operatorname{Stom}_{j}^{i}B_{i}}{W_{j}}$$

$\Delta t = 1 \text{ day}$

Identification of α

!	0.106	0.106	0.076	0.53	!
!	0.	0.014	0.01	0.069	!
!	0.	0.	0.	0.	!
!	0.	0.	0.	0.	!

Identification of conversion factors E_{i}^{i}

 $E_j^i = \frac{number \ of \ individuals \ i \ produced}{number \ of \ idividuals \ j \ consumed} \,.$ Figures in the litterature (Arias Gonzales) indicate that

$$\widetilde{E}_{j}^{i} = \frac{biomass\ i\ produced}{biomass\ j\ consumed} \leq 0.3$$

with values of 0.12, 0.13 for piscivores and macrocarnivores, whatever the prey:

$$\widetilde{E}_{j}^{i} = 0.125, \quad j = 1, 2, \ i = 1, \dots, 4.$$

We deduce that

 $\widetilde{E}_{j}^{i} = \frac{number\ of\ individuals\ i\ produced\ \times W_{i}}{number\ of\ individuals\ j\ consumed\ \times W_{j}}$

and thus

Identification of \widetilde{S}



Identification of growth rates

By writing that the densities x_i^* are at equilibrium, we obtain the intrinsic growth rates

$$R_i = 1 - \sum_{j=1}^{4} \widetilde{S}_i^j x_j^{\star}, \quad i = 1, \dots, 4$$

Trajectories (1)



Trajectories (2)



A MATHEMATICAL MEASURE OF THE PROTECTED AREA EFFECT

Catches

• Catches on the piscivors $x_1(t)$, macrocarnivors $x_2(t)$ and herbivors $x_3(t)$:

$$C_i = e_i x_i$$
 with $e_4 = 0$

• Uncertainty scenarios for exploitation rates $e_i(\omega(t)) \in [\overline{e}_i - \sigma_i, \overline{e}_i + \sigma_i] \subset [0, 1]$

Exploited dynamics

$$\begin{aligned} x_0(t+1) &= (1 - \overbrace{\theta(\omega(t))}^{\theta=0: \text{ no cyclone.}} x_0(t) \overbrace{\left(R_0\left(1 - \frac{x_0(t)}{K_0}\right)\right)}^{\log i tic} \\ &+ \underbrace{\theta(\omega(t))}_{\theta=1: \text{ cyclone.}} \underbrace{0.3 \times x_0(t)}_{30 \text{ \% reduction}} \\ x_i(t) &= x_i^e(t) \left(R + S(x_0(t), \omega(t)) x^e(t)\right)_i \\ x_i^e(t+1) &= x_i(t)(1 - e_i(\omega(t))) \text{ catches} \end{aligned}$$

Exploited dynamics with reserve

- Model not spatially explicit: scalar 1 – A measures the size of protected area PA
 - (A = 0: full reserve; A = 1: no reserve)
- A fixed proportion A ∈ [0, 1] is open to harvesting so that catches are given by C_i(t) = e_i(ω(t))Ax_i(t)
- Exploited dynamics with a protected area: idem but $x^e \to x^A$ and

 $x_i^A(t+1) = x_i(t)(1 - Ae_i(\omega(t))), \quad i = 1, \dots, 4$

Sources of uncertainties

Scenarios $\omega(0), \omega(1), \ldots$ comprise uncertainties from • cyclonic events impacting coral:

 $\theta(\omega(t)) \sim \text{Bernoulli}(1,p)$

• catch effort:

 $e_i(\omega(t)) \sim \text{Uniform} \left[\overline{e}_i - \sigma_i, \overline{e}_i + \sigma_i \right]$

Assuming statistical independence, this gives a **probability** \mathbb{P} on scenarios $\omega \in \Omega$

Catches economic valueUtility function of catches:

$$U\left(C_1(t), C_2(t), C_3(t)\right)$$

• Substitutable and essential factors:

$$U(c_1, c_2, c_3) = c_1^{0.5} \times c_2^{0.5} \times c_3^{0.5}$$

Stochastic intertemporal decision

- Optimal discounted utility approach: $\max_{A} \mathbb{E}_{\omega} \left[\sum_{t=0}^{T} \rho^{t} U \left(C_{1}(t), C_{2}(t), C_{3}(t) \right) \right].$
- Maximin approach:
 - $\max_{A} \mathbb{E}_{\omega} \left| \min_{t=0,\dots,T} U \left(C_1(t), C_2(t), C_3(t) \right) \right|.$
- Viability and effectiveness approaches:

Conservation requirements: existence values

• Implicit Conservation with viability: $U(x(t)) \ge U(C(t)) \ge U_{\flat}$ \Longrightarrow

 $x_1(t) > 0, x_2(t) > 0, x_3(t) > 0$

• Explicit conservation:

 $x_3(t) \ge x_{3,\flat}$

A stochastic effectiveness analysis

An indicator of sustainability at confidence level $\beta \in [0, 1]$ is the sustainable kernel $\operatorname{Sust}_{\beta}(A) \stackrel{\text{def}}{=}$ $\left\{ x(0) \mid \mathbb{P}_{\omega} \left(U \left(C_{1}(t), C_{2}(t) \right) \geq U_{\flat} \text{ for all times} \right) \geq \beta \right\}$

It consists of initial states $x(0) = (x_0(0), \dots, x_4(0))$ such that the probability that a random trajectory starting from x(0) provides a utility from catches greater than U_{\flat} is at least β .

Global reserve effect definition

A particular case is the **robust kernel** Sust₁ = Sust: whatever the scenarios, a minimal utility U_{\flat} is ensured.

We say that **global reserve effect** holds if there exists A < 1 such that $\text{Sust}_{\beta}(1) \subsetneq \text{Sust}_{\beta}(A)$ (Global reserve effect holds true if the kernel is enlarged when fishing is restricted)

Optimal sustainable reserve size

Given an *initial condition* x = x(0):

- Maximal guaranteed use values is, for size A ∈ [0, 1]: U^{*}_◊(A, x, β) ^{def} = max(U_◊, x ∈ Sust_β(A)) The largest utility which can be ensured with probability β.

A reserve effect measure

- Reserve effect index: PAI_β(x) ^{def} = U^{*}_b(A^{*}_β(x), x) - U^{*}_b(1, x) Compares difference of utility witout and with (optimal) reserve
- **Definition:** reserve effect holds true for state x if $PAI_{\beta}(x) > 0$

Contribution values

- Contribution of trophic group *i*: compare the *sustainability kernel* Sust in two cases
 - 1. Sust_i without i, namely $x_i(t) \equiv 0$
 - 2. Sust with *i*, namely any $x_i(t) > 0$
- **Contribution index**: the difference $I_i \stackrel{\text{def}}{=} \text{Sust} \setminus \text{Sust}_i$
- A particular case: $Sust_i = \emptyset$

CONCLUSIONS

Conclusion

- Methodology: invariance, co-viability
 - The role of constraints
 - Multi-criteria: conservation and efficiency
 - Intergenerational equity
- Reserve problem:
 - Formalization of reserve effect
- Aboré reserve: a model
 - with calibrated trophic interactions
 - account for the climatic change through coral

Perspectives

- Robustness with respect to parameter changes
- Indicator of refuge function of coral
- Spatially explicit
- Biodiversity measures
- Non cooperative harvesting agents
- Age structure

To end with...

NEVER PREPARE A TALK FOR A CONFERENCE IN SEPTEMBER AT THE OTHER END OF THE WORLD WHEN YOUR SCIENTIFIC PARTNERS ARE IN AUGUST VACATIONS!

Contribution value for herbivors

If herbivors x_3 collapse, the whole ecosystem can disappear?

Conjecture 1 If $x_3 = 0$, the sustainability kernel is empty: $Sust_3(A) = \emptyset$

- \implies Strong contribution value of x_3
- $I_3 = \text{Sust} \setminus \text{Sust}_3 = \text{Sust}$

A co-viability analysis without global changes

- Assumption 1: No damage for coral: p = 0. Coral at equilibrium 80%
- Assumption 2: Robust approach: Confident rate $\beta = 1$
- A reserve effect with moderate harvesting:
 Conjecture 2 There exists a fishing effort threshold
 e[‡] such that
 - For any $\overline{e} \in (0; e^{\sharp})$, a PA effect.
 - For any $\overline{e} > e^{\sharp}$, no PA effect.



Figure 4: Reserve Effect Index PAI(u) at x(0) = (0.26; 1.7; 6.84; 0.8). Uncertainty $\sigma = 5\%$.

A reserve effect with moderate harvesting



(a) Guaranteed utility of captures $U_{\rm b}^{\star}(A)$

Figure 5: A reserve effect at x(0) = (0.26; 1.7; 6.84, 0.96) toviable management offisheries and biodiversely mrough protected dress: the effect reserve case - p. 68

A reserve effect with moderate harvesting



(a) x(t) without reserve MPA= (b) x(t) with optimal MPA = 94 0%

Figure 6: A reserve effect at x(0) =(0.26: 1.7: 6.84: 0.8) For the management of fisheries and biodiversity through protected afeas: the Abore reef reserve case - p. 69

No reserve effect for large exploitation rates



(a) Guaranteed utility of captures $U_{\rm b}^{\star}(A)$

Figure 7: No reserve effect at $x_0 = (0.26; 1.7; 6.84; 0.98c)$ to five margen learges a cophoritration are subset of the second secon

No reserve effect for large exploitation rate



(0.26:1.7:6.84:0.8) IOI a large have been and biodiversity through protected areas: the Abore corrective case - p. 71

A co-viability analysis with certain climatic changes

- Assumption: Certain damage for coral: p = 1.
 A stronger reserve effect !!!!
 Conjecture <u>3</u> There exists a threshold e^{\perp} such that
 - For any $\overline{e} \in]0; e^{\sharp}]$, a PA effect.
 - For any $\overline{e} > e^{\sharp}$, no PA effect.


Figure 9: With climatic change: Reserve Effect Index PAI(u).

A mathematical approach toviable management offisheries and biodiversitythrough protected areas: the Abore reef reserve case – p. 73